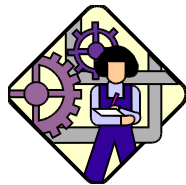


Building your own Functions



CS112 Scientific Computation

Department of Computer Science
Wellesley College

Built-in MATLAB functions

math: `sum, prod, mean, std, abs, sqrt, sin, cos, abs,`
 `exp, min, max`

logical: `any, all, & | ~`

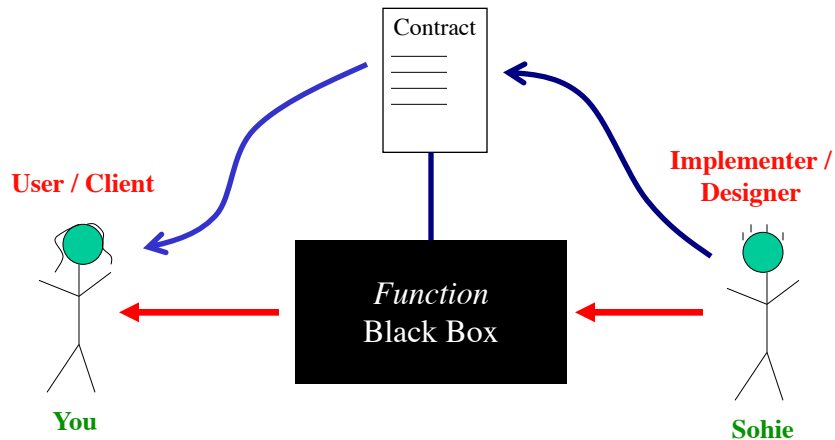
creation: `linspace, :, ones, zeros`

dimensions: `size, length`

graph/display: `plot, figure, subplot, xlabel, ylabel,`
 `title, axis, legend, imshow, imtool`

input/output: `input, disp`

Big idea: Abstraction



8-3

The other side of the contract

We've been using functions built by others - let's try writing a few of our own

Implement a **myMean** function that returns a single value representing the average value of a *vector or matrix*



8-4

Rules of the road

```
keyword → function avg = myMean (data) ← input parameter
           % avg = myMean(data)
           % returns the average of all of the values
           % in data, which may be a vector or matrix
local
variable* → dims = size(data);
            if (min(dims) == 1)
assign      → avg = sum(data)/length(data);
output      → else
            → avg = sum(sum(data))/prod(dims);
            → end
```

function name
(stored in file myMean.m)

help
comments
contract

function
body

* Local variables only exist during the execution of the function

8-5

Calling the new myMean function

```
>> nums = [3 9 6 2 8];
>> meanVal = myMean(nums)
meanVal =
    5.6000
>> nums = [3 4 7; 2 8 6]
nums =
     3     4     7
     2     8     6
>> meanVal = myMean(nums)
meanVal =
    5.0000
```



8-6

Executing a function

MATLAB workspace

Execution land

```
>>
```

8-7

Create **nums** vector

MATLAB workspace

nums

3	9	6	2	8
---	---	---	---	---

Execution land

```
>> nums = [3 9 6 2 8];
```

8-8

Invoke **myMean** function

MATLAB workspace

nums [3 9 6 2 8]

myMean local workspace

Execution land

```
>> nums = [3 9 6 2 8];  
>> meanVal = myMean(nums)
```

```
function avg = myMean(data)  
    dims = size(data);  
    if (min(dims) == 1)  
        avg = sum(data)/length(data);  
    else  
        avg = sum(sum(data))/prod(dims);  
    end
```

8-9

Create variable for input parameter **data** and copy value of **nums** to **data**

MATLAB workspace

nums [3 9 6 2 8]

myMean local workspace

data [3 9 6 2 8]

Execution land

```
>> nums = [3 9 6 2 8];  
>> meanVal = myMean(nums)
```

```
function avg = myMean(data)  
    dims = size(data);  
    if (min(dims) == 1)  
        avg = sum(data)/length(data);  
    else  
        avg = sum(sum(data))/prod(dims);  
    end
```

8-10

Execute body of function

MATLAB workspace

nums [3 9 6 2 8]

myMean local workspace

data [3 9 6 2 8]

dims [1 5]

Execution land

```
>> nums = [3 9 6 2 8];  
>> meanVal = myMean(nums)
```

```
function avg = myMean(data)  
    dims = size(data);  
    if (min(dims) == 1)  
        avg = sum(data)/length(data);  
    else  
        avg = sum(sum(data))/prod(dims);  
    end
```

8-11

Is min(dims) == 1?

MATLAB workspace

nums [3 9 6 2 8]

myMean local workspace

data [3 9 6 2 8]

dims [1 5]

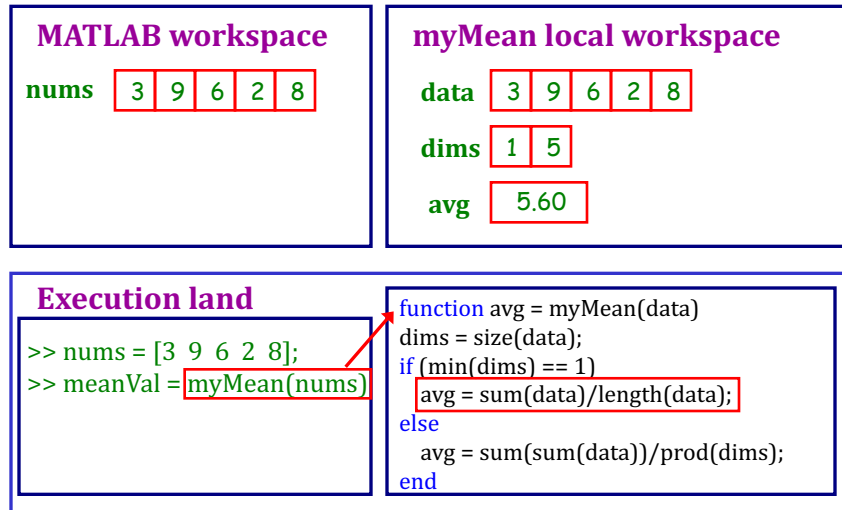
Execution land

```
>> nums = [3 9 6 2 8];  
>> meanVal = myMean(nums)
```

```
function avg = myMean(data)  
    dims = size(data);  
    if (min(dims) == 1)  
        avg = sum(data)/length(data);  
    else  
        avg = sum(sum(data))/prod(dims);  
    end
```

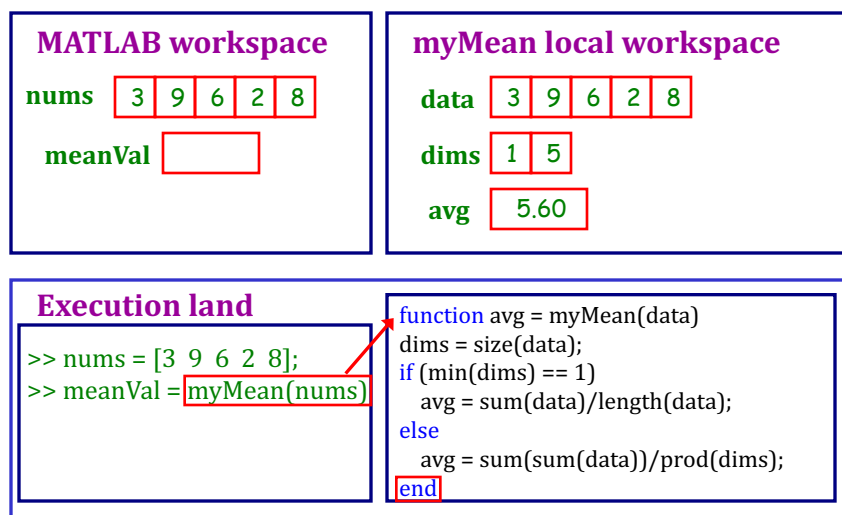
8-12

Yes, so we do 'then' clause



8-13

Return value stored in output variable



8-14

And the local workspace goes away

MATLAB workspace

nums [3 9 6 2 8]
meanVal 5.60

Execution land

```
>> nums = [3 9 6 2 8];  
>> meanVal = myMean(nums)  
meanVal =  
    5.6000
```

8-15

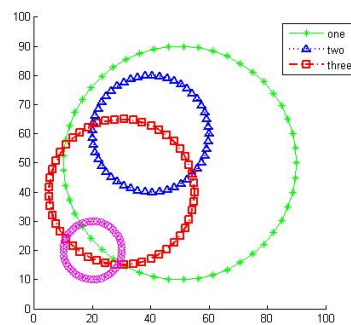
Try another one?

Write a function to draw a circle

Think first about the contract:

use inputs to control appearance:
radius, location, color, markers,
line style, line width

Call the new function **drawCircle**
and store it in an M-File named
drawCircle.m



8-16

Getting started

```
function drawCircle (radius, xcenter, ycenter, properties, width)
% drawCircle(radius, xcenter, ycenter, properties, width)
% draws circle with the specified radius, centered on location
% (xcenter, ycenter) with the specified properties and width
```

← don't forget
contract
comments!

8-17

Filling in the function body

```
function drawCircle (radius, xcenter, ycenter, properties, width)
% drawCircle(radius, xcenter, ycenter, properties, width)
% draws circle with the specified radius, centered on location
% (xcenter, ycenter) with the specified properties and width

angles = linspace(0, 2*pi, 50);
xcoords = xcenter + radius * cos(angles);
ycoords = ycenter + radius * sin(angles);
plot(xcoords, ycoords, properties, 'LineWidth', width);
```

8-18

Executing drawCircle function

MATLAB workspace

Execution land

```
>> drawCircle(40, 50, 50, 'g-*', 1);
```

Functions

8-19

Create input parameter variables ...

MATLAB workspace

Execution land

```
>> drawCircle(40, 50, 50, 'g-*', 1);
```

```
function drawCircle (radius, xcenter, ycenter, ...  
                    properties, width)  
    angles = linspace(0, 2*pi, 50);  
    xcoords = xcenter + radius * cos(angles);  
    ycoords = ycenter + radius * sin(angles);  
    plot(xcoords, ycoords, properties, ...  
         'LineWidth', width);
```

drawCircle
local workspace

radius

xcenter

ycenter

properties

width

8-20

... and fill them in from call statement

MATLAB workspace

Execution land

```
>> drawCircle(40, 50, 50, 'g-*', 1);
```

```
function drawCircle (radius, xcenter, ycenter, ...  
                    properties, width)  
    angles = linspace(0, 2*pi, 50);  
    xcoords = xcenter + radius * cos(angles);  
    ycoords = ycenter + radius * sin(angles);  
    plot(xcoords, ycoords, properties, ...  
         'LineWidth', width);
```

**drawCircle
local workspace**

radius 40

xcenter 50

ycenter 50

properties 'g-*

width 1

8-21

Execute body of function

MATLAB workspace

Execution land

```
>> drawCircle(40, 50, 50, 'g-*', 1);
```

```
function drawCircle (radius, xcenter, ycenter, ...  
                    properties, width)  
    angles = linspace(0, 2*pi, 50);  
    xcoords = xcenter + radius * cos(angles);  
    ycoords = ycenter + radius * sin(angles);  
    plot(xcoords, ycoords, properties, ...  
         'LineWidth', width);
```

**drawCircle
local workspace**

radius 40

xcenter 50

ycenter 50

properties g-*

width 1

angles ...

8-22

Next statement

MATLAB workspace

Execution land

```
>> drawCircle(40, 50, 50, 'g-*', 1);
```

```
function drawCircle (radius, xcenter, ycenter, ...  
                    properties, width)  
    angles = linspace(0, 2*pi, 50);  
    xcoords = xcenter + radius * cos(angles);  
    ycoords = ycenter + radius * sin(angles);  
    plot(xcoords, ycoords, properties, ...  
         'LineWidth', width);
```

**drawCircle
local workspace**

radius 40

xcenter 50

ycenter 50

properties g-*

width 1

angles ...

xcoords ...

8-23

Next statement

MATLAB workspace

Execution land

```
>> drawCircle(40, 50, 50, 'g-*', 1);
```

```
function drawCircle (radius, xcenter, ycenter, ...  
                    properties, width)  
    angles = linspace(0, 2*pi, 50);  
    xcoords = xcenter + radius * cos(angles);  
    ycoords = ycenter + radius * sin(angles);  
    plot(xcoords, ycoords, properties, ...  
         'LineWidth', width);
```

**drawCircle
local workspace**

radius 40

xcenter 50

ycenter 50

properties g-*

width 1

angles ...

xcoords ...

ycoords ...

8-24

And we draw the circle

MATLAB workspace

Execution land

```
>> drawCircle(40, 50, 50, 'g-*', 1);
```

```
function drawCircle (radius, xcenter, ycenter, ...  
                    properties, width)  
    angles = linspace(0, 2*pi, 50);  
    xcoords = xcenter + radius * cos(angles);  
    ycoords = ycenter + radius * sin(angles);  
    plot(xcoords, ycoords, properties, ...  
         'LineWidth', width);
```

**drawCircle
local workspace**

radius 40

xcenter 50

ycenter 50

properties g-*

width 1

angles ...

xcoords ...

ycoords ...

8-25

Where'd everybody go?

MATLAB workspace

Execution land

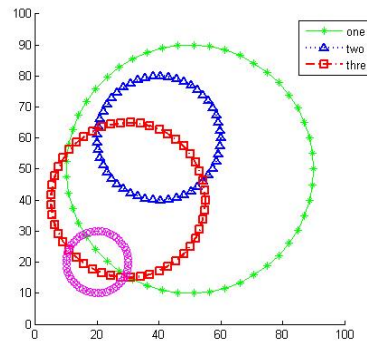
```
>> drawCircle(40, 50, 50, 'g-*', 1);
```

8-26

A thorough test

% testCircle.m
% tests the drawCircle function

```
hold on
drawCircle(40, 50, 50, 'g-*', 1);
drawCircle(20, 40, 60, 'b:^', 2);
drawCircle(25, 30, 40, 'r-.s', 2);
legend('one', 'two', 'three');
drawCircle(10, 20, 20, 'm--o', 1);
axis equal
axis([0 100 0 100])
hold off
```



8-27

Functions with multiple outputs

Suppose we'd like to write a variation of **myMean** that returns both the *arithmetic mean* and *geometric mean*

Given n numbers:

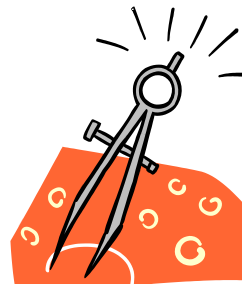
$$a_1, a_2 \dots a_n$$

arithmetic mean:

$$(a_1 + a_2 + \dots + a_n)/n$$

geometric mean:

$$\sqrt[n]{a_1 * a_2 * \dots * a_n}$$



8-28

Consider first ...

Some built-in functions can return one or more values,
depending on how the function is called

For example, consider the `min` function:

```
>> nums = [3 9 6 2 8];  
>> minVal = min(nums)  
minVal =  
    2  
>> [minVal minIndex] = min(nums)  
minVal =  
    2  
minIndex =  
    4
```

8-29

New lean mean machine

```
function [arith geom] = myMean2(data)  
% [arith geom] = myMean2(data)  
% returns both the arithmetic and geometric mean of  
% the values in data, which may be a vector or matrix  
  
dims = size(data);  
if (min(dims) == 1)  
    arith = sum(data)/length(data);  
    geom = nthroot(prod(data), length(data));  
else  
    arith = sum(sum(data))/prod(dims);  
    geom = nthroot(prod(prod(data)), prod(dims));  
end
```



8-30