

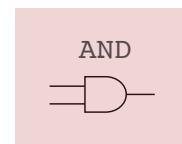


# Arithmetic Logic

adders  
Arithmetic Logic Unit

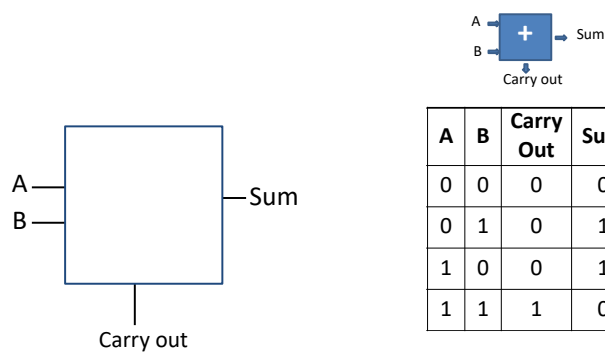
## Motivation: how do we go from **code** to **gates**?

```
int count_odds(int array[10]) {  
    int count = 0;  
    for (int i = 0; i < 10; i++) {  
        count += array[i] & 0x1;  
    }  
    return count;  
}
```



## Addition: 1-bit **half** adder

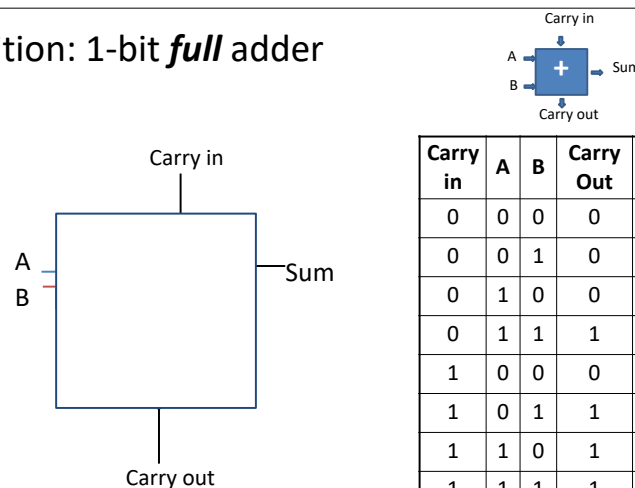
ex



A	B	Carry Out	Sum
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

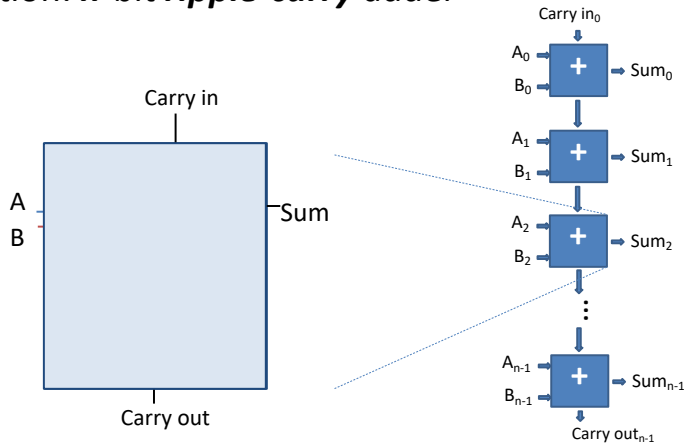
Hint: the smallest solution uses 2 gates from: AND, OR, XOR, NOT, NAND, NOR

## Addition: 1-bit **full** adder



Carry in	A	B	Carry Out	Sum
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

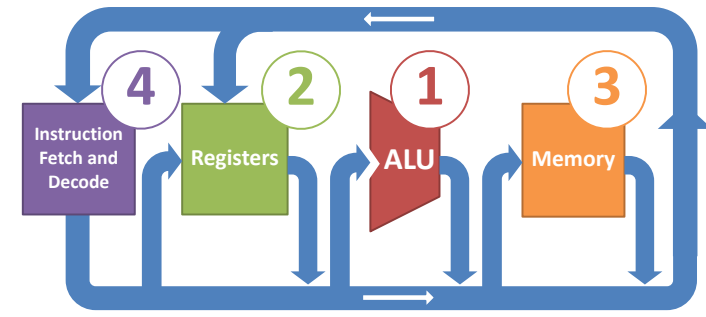
## Addition: $n$ -bit *ripple-carry* adder



There are faster, more complicated ways too...

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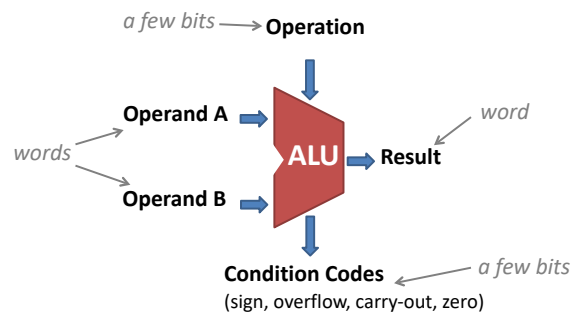
## Processor Components



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## Arithmetic Logic Unit (ALU)

1



Hardware unit for arithmetic and bitwise operations.

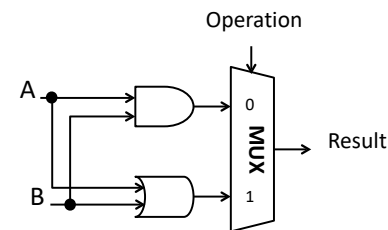
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## 1-bit ALU for bitwise operations

We will use  $n$  1-bit ALUs to build an  $n$ -bit ALU.

Each bit  $i$  in the result is computed from the corresponding bit  $i$  in the two inputs.

An example (simplified) 1-bit ALU

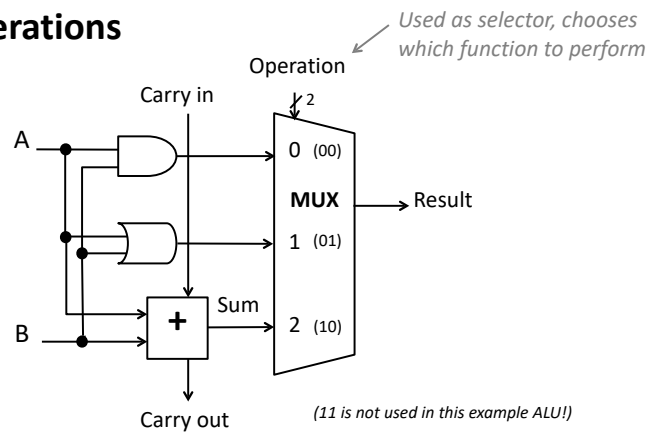


Op	A	B	Result
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

ex

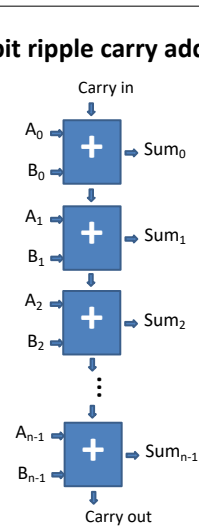
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## 1-bit ALU: 3 operations

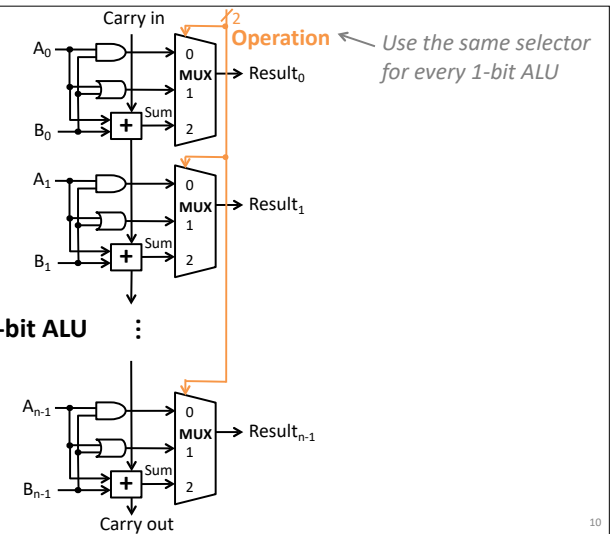


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## n-bit ripple carry adder



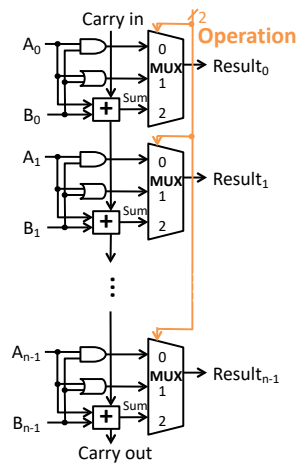
## n-bit ALU



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## Controlling the ALU

ALU control lines	Function
00	AND
01	OR
10	add



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## Include subtraction

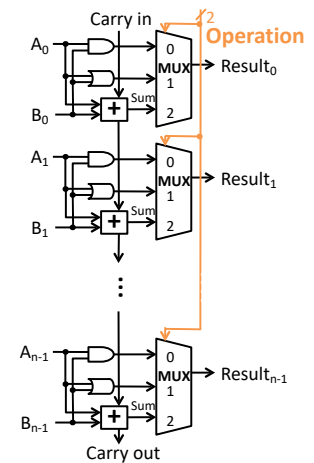
How can we control ALU inputs or add minimal new logic to **also compute  $A - B$** ?

### Recall:

$$A - B = A + (-B) \\ = A + (\sim B + 1)$$

### Plan:

Feed bitwise-not B into the adder  
Add an extra 1: how?



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## Include subtraction

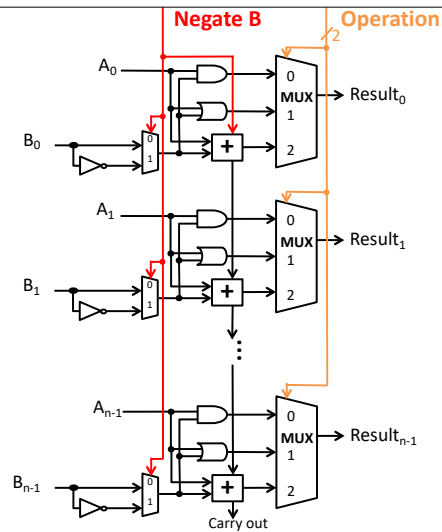
**Plan to compute  $A-B$ :**

1. Feed bitwise-not B into the adder
2. Add an extra 1

**Key insight:**

The *same* selector bit (0 or 1) can be used for both!

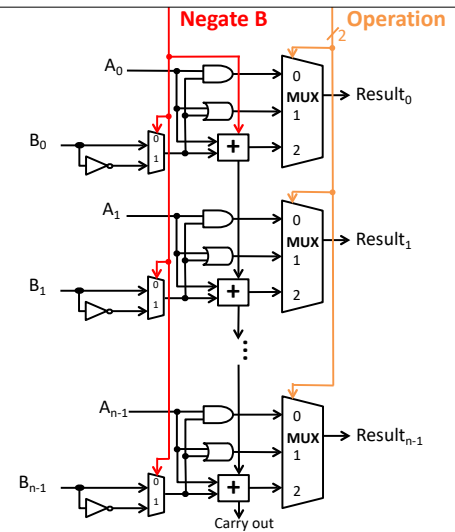
1. Feed the selector into a new 2:1 mux to choose B or  $\sim B$
2. Feed the selector in as the carry in to the least significant bit



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## Include subtraction

ALU control lines	Function
000	AND
001	OR
010	add
110	subtract
...	...



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**A NAND B**

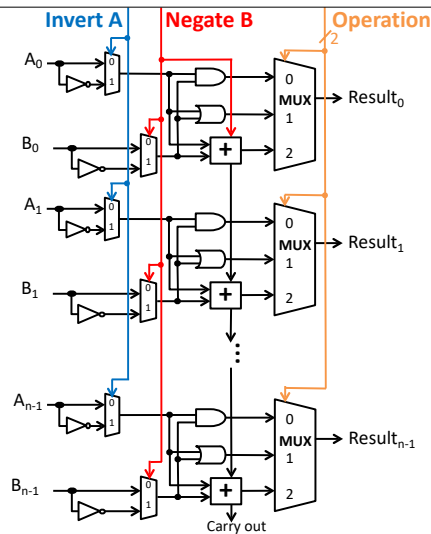
**A NOR B**

**A<B**

**A==B**

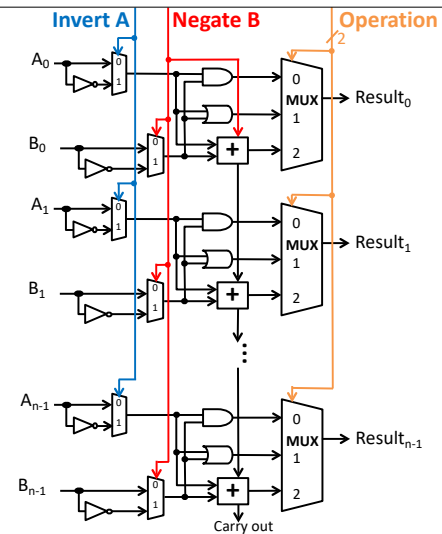
How can we control ALU inputs or add minimal new logic to compute each?

*You will implement some of these in the Arch Assignment!*



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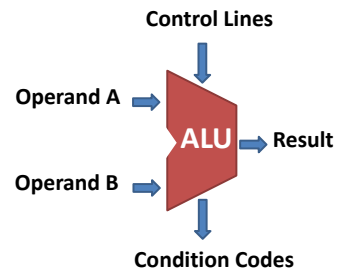
ALU control lines	Function
0000	AND
0001	OR
0010	add
0110	subtract
????	NAND
????	NOR
????	less than
????	equals



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## Controlling the ALU

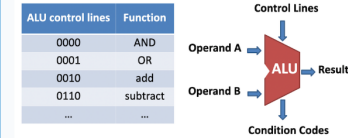
ALU control lines	Function
0000	AND
0001	OR
0010	add
0110	subtract
...	...



Abstraction!

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How many different functions (operations) could this ALU theoretically perform?



4

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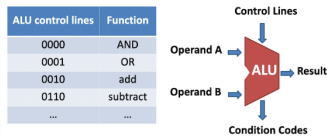
16

32

None of the above

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How many different functions (operations) could this ALU theoretically perform?



4

0%

8

0%

16

0%

32

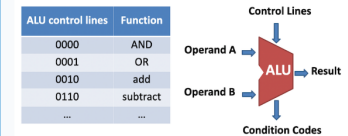
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None of the above

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Start the presentation to see live content. For screen share software, share the entire screen. Get help at [pollev.com/app](https://pollev.com/app)

How many different functions (operations) could this ALU theoretically perform?



4

0%

8

0%

16

0%

32

0%

None of the above

0%

Start the presentation to see live content. For screen share software, share the entire screen. Get help at [pollev.com/app](https://pollev.com/app)

## ALU conditions (additional outputs)

### Extra ALU outputs

describing properties of result.

#### Zero Flag:

1 if result is 00...0 else 0

#### Sign Flag:

1 if result is negative else 0

#### Carry Flag:

1 if carry out else 0

#### (Signed) Overflow Flag:

1 if signed overflow else 0

*You will implement these in the Arch Assignment!*

