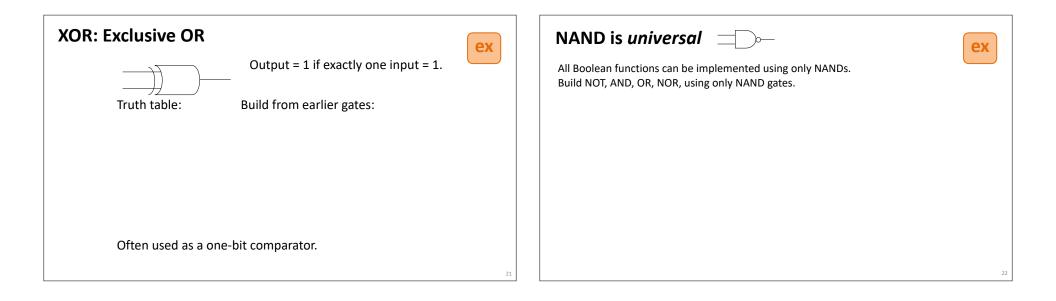
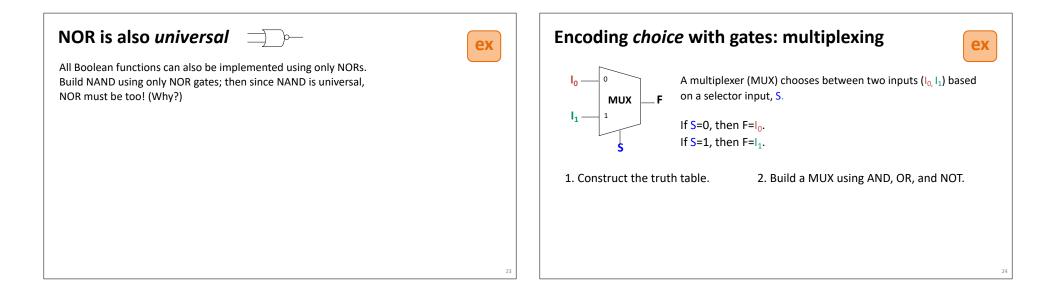


Boolean Algebra: more laws

Boolean algebra laws can be proven by truth tables and used to show equivalences.

Distributive	A + BC = (A + B)(A + C)	A(B+C) = AB + AC
Null (or Null Element)	$0^*A = 0$ (the Zero Law)	1 + A = 1 (the One Law)
Idempotent	A + A = A	AA = A
Associativity	(AB)C = A(BC)	(A+B)+C=A+(B+C)
Commutativity	A+B = B+A	AB = BA
Inverse (or Complements)	$A\overline{A} = 0$	$A + \overline{A} = 1$
Identity	0+A = A	1*A = A
Involution (or double negation)	$\overline{\overline{A}} = A$	none
Name of Law / Theorem	Form	Equivalent/Dual form (interchange AND and OR, and 0 and 1







Computers

Manual calculations powered all early US **space** missions. Facilitated transition to digital computers.

Katherine Johnson Supported Mercury, Apollo, Space Shuttle, ...

Dorothy Vaughn

· First black supervisor within NACA Early self-taught FORTRAN programmer for NASA move to digital computers.



Early pioneers in reliable computing



Katherine Johnson Calculated first US human space flight trajectories Mercury, Apollo 11, Space Shuttle, ... Reputation for accuracy in manual calculations, verified early code Called to verify results of code for launch

calculations for first US human in orbit Backup calculations helped save Apollo 13 Presidential Medal of Freedom 2015

Margaret Hamilton

Led software team for Apollo 11 Guidance Computer, averted mission abort on first moon landing. Coined "software engineering", developed techniques for correctness and reliability. Presidential Medal of Freedom 2016



Wellesley Connection: Mary Allen Wilkes '59



Created LAP operating system at MIT Lincoln Labs for Wesley A. Clark's LINC computer, widely regarded as the first personal computer (designed for interactive use in bio labs). Work done 1961-1965.



Created first interactive keyboard-based text editor on 256 character display. LINC had only 2K 12-bit words; (parts of) editor code fit in 1K section; document in other 1K.

In 1965, she developed LAP6 with LINC in Baltimore living room. First home PC user!



Early versions of LAP developed using LINC simulator on MIT TX2 compute, famous for GUI/PL work done by Ivan and Bert Sutherland at MIT.



Later earned Harvard law degree and headed Economic Crime and Consumer Protection Division in Middlesex (MA) County District Attorney's office.

optional



optional