

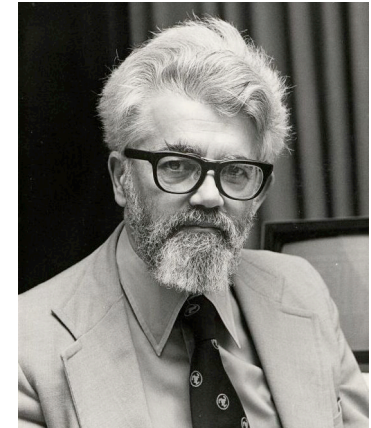
Introduction to Racket, a dialect of LISP: Expressions and Bindings



CS251 Programming Languages
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LISP: designed by John McCarthy, 1958
published 1960



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LISP: implemented by Steve Russell,
early 1960s



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LISP: LISt Processing

- McCarthy, MIT artificial intelligence, 1950s-60s
 - Advice Taker: represent logic as data, not just program
- Needed a language for:
 - Symbolic computation
 - Programming with logic
 - Artificial intelligence
 - Experimental programming
- So make one!

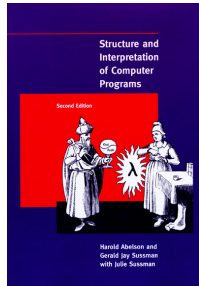
Emacs: M-x doctor

i.e., not just number crunching

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Scheme

- Gerald Jay Sussman and Guy Lewis Steele (mid 1970s)
- Lexically-scoped dialect of LISP that arose from trying to make an “actor” language.
- Described in amazing “Lambda the Ultimate” papers (<http://library.readscheme.org/page1.html>)
 - Lambda the Ultimate PL blog inspired by these: <http://lambda-the-ultimate.org>
- Led to Structure and Interpretation of Computer Programs (SICP) and MIT 6.001 (<https://mitpress.mit.edu/sicp/>)



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- Grandchild of LISP (variant of Scheme)
 - Some changes/improvements, quite similar
- Developed by the PLT group (<https://racket-lang.org/people.html>), the same folks who created DrJava.
- Why study Racket in CS251?
 - Clean slate, unfamiliar
 - Careful study of PL foundations (“PL mindset”)
 - Functional programming paradigm
 - Emphasis on functions and their composition
 - Immutable data (lists)
 - Beauty of minimalism
 - Observe design constraints/historical context

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Expressions, Values, and Bindings

- Entire language: these three things
- Expressions have *evaluation rules*:
 - How to determine the value denoted by an expression.
- For each structure we add to the language:
 - What is its **syntax**? How is it written?
 - What is its **evaluation rule**? How is it evaluated to a **value** (expression that cannot be evaluated further)?

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Values

- Values are expressions that cannot be evaluated further.
- Syntax:
 - Numbers: **251**, **240**, **301**
 - Booleans: **#t**, **#f**
 - There are more values we will meet soon (strings, symbols, lists, functions, ...)
- Evaluation rule:
 - Values evaluate to themselves.

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Addition expression: syntax

Adds two numbers together.

Syntax: $(+ e1 e2)$

Every parenthesis required; none may be omitted.

$e1$ and $e2$ stand in for *any expression*.

Note *prefix* notation.

Note recursive structure!

Examples:

$(+ 251 240)$

$(+ (+ 251 240) 301)$

$(+ \#t 251)$

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Addition expression: evaluation

Syntax: $(+ e1 e2)$

Evaluation rule:

Note recursive structure!

1. evaluate $e1$ to a value $v1$
2. evaluate $e2$ to a value $v2$
3. Return the arithmetic sum of $v1 + v2$.

Not quite!

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Addition: dynamic type checking

Syntax: $(+ e1 e2)$

Evaluation rule:

1. evaluate $e1$ to a value $v1$
2. evaluate $e2$ to a value $v2$
3. If $v1$ and $v2$ are both numbers then return the arithmetic sum of $v1 + v2$.
4. Otherwise, a **type error** occurs.

Still not quite!
More later ...

Dynamic type-checking

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Evaluation Assertions Formalize Evaluation

The **evaluation assertion** notation $e \Downarrow v$ means “ e evaluates to v ”.

Our evaluation rules so far:

- *value rule*: $v \Downarrow v$ (where v is a number or boolean)
- *addition rule*:
if $e1 \Downarrow v1$ and $e2 \Downarrow v2$
and $v1$ and $v2$ are both numbers
and v is the sum of $v1$ and $v2$
then $(+ e1 e2) \Downarrow v$

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Evaluation Derivation in English

An **evaluation derivation** is a “proof” that an expression evaluates to a value using the evaluation rules.

$(+ 3 (+ 5 4)) \downarrow 12$ by the addition rule because:

- $3 \downarrow 3$ by the value rule
- $(+ 5 4) \downarrow 9$ by the addition rule because:
 - $5 \downarrow 5$ by the value rule
 - $4 \downarrow 4$ by the value rule
 - 5 and 4 are both numbers
 - 9 is the sum of 5 and 4
- 3 and 9 are both numbers
- 12 is the sum of 3 and 9

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More Compact Derivation Notation

$v \downarrow v$ (value rule)

where v is a value
(number, boolean, etc.)

$\frac{e1 \downarrow v1 \quad e2 \downarrow v2}{(+ e1 e2) \downarrow v}$ (addition rule)

side conditions of rules

Where $v1$ and $v2$ are numbers and v is the sum of $v1$ and $v2$.

$\frac{\frac{\frac{3 \downarrow 3 \text{ (value)}}{5 \downarrow 5 \text{ (value)}}{4 \downarrow 4 \text{ (value)}}}{(+ 5 4) \downarrow 9 \text{ (addition)}}}{(+ 3 (+ 5 4)) \downarrow 12 \text{ (addition)}}$

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Errors Modeled by “Stuck” Derivations

How to evaluate
 $(+ \#t (+ 5 4))$?

$\frac{\frac{\frac{\#t \downarrow \#t \text{ (value)}}{5 \downarrow 5 \text{ (value)}}{4 \downarrow 4 \text{ (value)}}}{(+ 5 4) \downarrow 9 \text{ (addition)}}$

Stuck here. Can't apply
(addition) rule because
 $\#t$ is not a number

How to evaluate
 $(+ 3 (+ 5 \#f))$?

$\frac{\frac{\frac{3 \downarrow 3 \text{ (value)}}{5 \downarrow 5 \text{ (value)}}{\#f \downarrow \#f \text{ (value)}}$

Stuck here. Can't apply
(addition) rule because
 $\#f$ is not a number

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Special Cases for Addition

The addition operator $+$ can take any number of operands.

- For now, treat $(+ e1 e2 \dots en)$ as $(+ (+ e1 e2) \dots en)$
E.g., treat $(+ 7 2 -5 8)$ as $(+ (+ (+ 7 2) -5) 8)$
- Treat $(+ e)$ as e
- Treat $(+)$ as 0 (or say $(+) \downarrow 0$)

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Other Arithmetic Operators

Similar syntax and evaluation for

`- * / quotient remainder`

except:

- Second argument of `/`, `quotient`, `remainder` must be nonzero
- Result of `/` is a rational number (fraction)
- `quotient` and `remainder` take exactly two arguments; anything else is an error.
- `(- e)` is treated as `(- 0 e)`
- `(/ e)` is treated as `(/ 1 e)`
- `(*)` evaluates to 1.
- `(/)` and `(-)` are errors.

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Relation Operators

The following relational operators on numbers return booleans: `< <= = >= >`

For example:

$$\frac{e1 \downarrow v1}{e2 \downarrow v2} \quad (\text{less than rule})$$

$$(< e1 e2) \downarrow v$$

Where $v1$ and $v2$ are numbers and v is #f if $v1$ is less than $v2$ or #t if $v1$ is not less than $v2$

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Conditional (if) expressions

Syntax: `(if e1 e2 e3)`

Evaluation rule:

1. Evaluate `e1` to a value `v1`.
2. If `v` is not the value `#f` then return the result of evaluating `e2` otherwise return the result of evaluating `e3`

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Conditional (if) expressions

$$\frac{e1 \downarrow v1}{e2 \downarrow v2} \quad (\text{if nonfalse})$$

$$(\text{if } e1 e2 e3) \downarrow v2$$

where $v1$ is not #f

e3 not evaluated!

$$\frac{e1 \downarrow \#f}{e3 \downarrow v3} \quad (\text{if false})$$

$$(\text{if } e1 e2 e3) \downarrow v3$$

e2 not evaluated!

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Your turn

Use evaluation derivations to evaluate the following expressions

```
(if (< 8 2) (+ #f 5) (+ 3 4))
```

```
(if (+ 1 2) (- 3 7) (/ 9 0))
```

```
(+ (if (< 1 2) (* 3 4) (/ 5 6)) 7)
```

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Expressions vs. statements

If expressions can go anywhere an expression is expected:

```
(if (< 9 (- 251 240))
    (* 3 (+ 4 5))
    (+ 6 (* 7 8)))
```

```
(+ 4 (* (if (< 9 (- 251 240)) 2 3) 5))
```

Note: this is an *expression*, not a *statement*. Do other languages you know have conditional expressions in addition to conditional statements? (Many do! Java, JavaScript, Python, ...)

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If expressions: careful!

Unlike earlier expressions, not all subexpressions of if expressions are evaluated!

```
(if (> 251 240) 251 (/ 251 0))
```

```
(if #f (+ #t 251) 251)
```

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Environments: Motivation

Want to be able to name values so can refer to them later by name. E.g.;

```
(define x (+ 1 2))
```

```
(define y (* 4 x))
```

```
(define diff (- y x))
```

```
(define test (< x diff))
```

```
(if test (+ (* x y) diff) 17)
```

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Environments: Definition

- An **environment** is a sequence of bindings that associate identifiers (variable names) with values.
 - Concrete example:
num → 17, absoluteZero → -273, true → #t
 - Abstract Example (use *id* to range over identifiers):
id1 → *v1*, *id2* → *v2*, ..., *idn* → *vn*
 - Empty environment: ∅
- An environment serves as a context for evaluating expressions that contain identifiers.
- “Second argument” to evaluation, which takes both an expression and an environment.

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Addition: evaluation *with environment*

Syntax: (+ *e1* *e2*)

Evaluation rule:

1. evaluate *e1* **in the current environment** to a value *v1*
2. evaluate *e2* **in the current environment** to a value *v2*
3. If *v1* and *v2* are both numbers then return the arithmetic sum of *v1* + *v2*.
4. Otherwise, a **type error** occurs.

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Variable references

Syntax: *id*

id: any identifier

Evaluation rule:

Look up and return the value to which *id* is bound in the current environment.

- Look-up proceeds by searching from the most-recently added bindings to the least-recently added bindings (front to back in our representation)

Examples:

- Suppose *env* is num → 17, absoluteZero → -273, true → #t
- In *env*, num evaluates to 17, absoluteZero evaluates to -273, and true evaluates to #t

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define bindings

Syntax: (define *id* *e*)

define: keyword

id: any identifier

e: any expression

Evaluation rule:

1. Evaluate *e* to a value *v* **in the current environment**.
2. Produce a new environment that is identical to the current environment, with the additional binding *id* → *v* at the front.

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Environments: Example

$env0 = \emptyset$

`(define x (+ 1 2))`

$env1 = x \rightarrow 3, \emptyset$ (abbreviated $x \rightarrow 3$, can write as $x \rightarrow 3, \dots$ in text)

`(define y (* 4 x))`

$env2 = y \rightarrow 12, x \rightarrow 3$ (most recent binding first)

`(define diff (- y x))`

$env3 = diff \rightarrow 9, y \rightarrow 12, x \rightarrow 3$

`(define test (< x diff))`

$env4 = test \rightarrow \#t, diff \rightarrow 9, y \rightarrow 12, x \rightarrow 3$

`(if test (+ (* x 5) diff) 17)`

Environment here is still $env4$

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Evaluation Assertions & Rules with Environments

The **evaluation assertion** notation $e \# env \downarrow v$ means “Evaluating e in environment env yields value v ”.

$id \# env \downarrow v$ (varref)

where id is an identifier and $id \rightarrow v$ is the first binding in env for id . Only this rule actually uses env ; others just pass it along.

$v \# env \downarrow v$ (value)

where v is a value (number, boolean, etc.)

$e1 \# env \downarrow \#f$
 $e3 \# env \downarrow v3$ (if false)
 $(if e1 e2 e3) \# env \downarrow v3$

$e1 \# env \downarrow v1$
 $e2 \# env \downarrow v2$ (addition)
 $(+ e1 e2) \# env \downarrow v$

Where $v1$ and $v2$ are numbers and v is the sum of $v1$ and $v2$.

$e1 \# env \downarrow v1$
 $e2 \# env \downarrow v2$ (if nonfalse)
 $(if e1 e2 e3) \# env \downarrow v2$

where $v1$ is not $\#f$

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Example Derivation with Environments

Suppose $env4 = test \rightarrow \#t, diff \rightarrow 9, y \rightarrow 12, x \rightarrow 3$

$test \# env4 \downarrow \#t$ (varref)
| $x \# env4 \downarrow 3$ (varref)
| $5 \# env4 \downarrow 5$ (value)
| $(* x 5) \# env4 \downarrow 15$ (multiplication)
| $diff \# env4 \downarrow 9$ (varref)
| $(+ (* x 5) diff) \# env4 \downarrow 24$ (addition)
| $(if test (+ (* x 5) diff) 17) \# env4 \downarrow 24$ (if nonfalse)

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Racket Identifiers

- Racket identifiers are case sensitive. The following are four different identifiers: ABC, Abc, aBc, abc
- Unlike most languages, Racket is very liberal with its definition of legal identifiers. Pretty much any character sequence is allowed as identifier with the following exceptions:
 - Can't contain whitespace
 - Can't contain special characters `()[]{}"',`&#;`
 - Can't have same syntax as a number
- This means variable names can use (and even begin with) digits and characters like `!@$_%^&*.-+<=>?/`. E.g.:
 - `myLongName`, `my_long_name`, `my-long-name`
 - `is_a+b<c*d-e?`
 - `76Trombones`
- Why are other languages less liberal with legal identifiers?

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Formalizing Definitions and Environments

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Can't Redefine a Variable in Racket

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Other Racket Operators

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Racket Documentation

Racket Guide:

<https://docs.racket-lang.org/guide/>

Racket Reference:

<https://docs.racket-lang.org/reference>

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