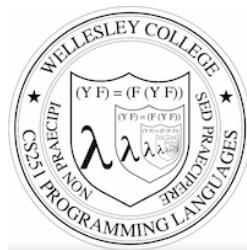


# Interpreting and Compiling Intex

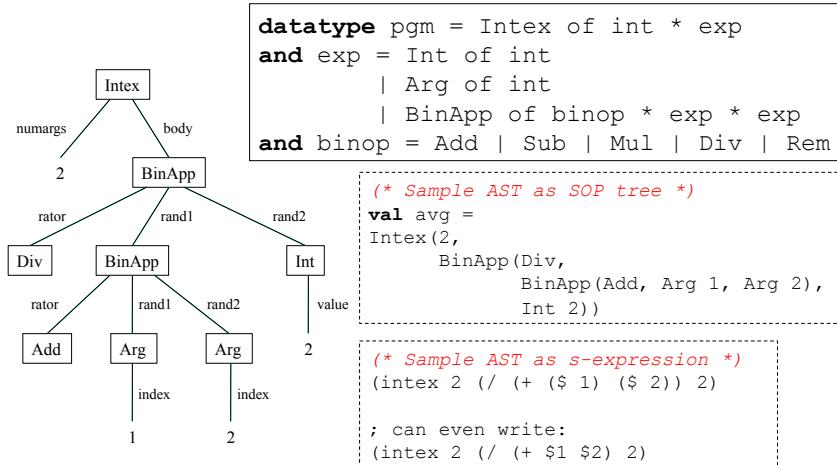
## SOLUTIONS



CS251 Programming Languages  
Spring 2018, Lyn Turbak

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### Intex Syntax Trees & Syntactic Data Types



Intex 3

### A New Mini-Language: Intex

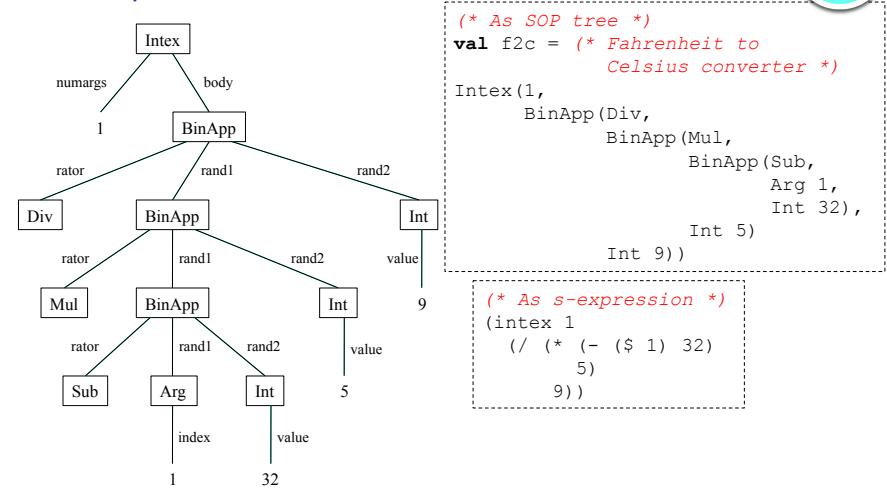
Intex programs are simple arithmetic expressions on integers that can refer to integer arguments.

Intex is the first in a sequence of mini-languages that can be extended to culminate in something that is similar to Racket. At each step along the way, we can add features that allow us to study different programming language dimensions.

- **Intex**: integer expressions, positional program arguments
- **Bindex**: Intex + named arguments & local naming
- **Valex**: Bindex + conditionals, multiple kinds of values (booleans, strings, lists), dynamic type checking, and syntactic sugar
- **HOFL** (Racket-like language): Valex + first-class functions
- **HOFLEC**: HOFL + SML-like mutable cells

Intex 2

How do we write this Intex program as SML SOP tree?  
As s-expression?



Intex 4



## Intex Implementation #1: Intex Interpreter in SML

Given an avg-in-Intex program, how can we execute it?

```
avg machine (I)
  □ avg-in-Intex program
  □ Intex interpreter machine (I)
    ♦ Intex-in-SML-interpreter program
    ♦ SML interpreter machine in wx VM (ignore details)
```

Intex 5

## Intex Interpreter Without Error Checking: Solution

```
(* Intex.pgm -> int list -> int *)
fun run (Intex(numargs, exp)) args =
  eval exp args

(* Intex.exp -> int list -> int *)
and eval (Int i) args = i
  | eval (Arg index) args = List.nth(args, index-1)
  | eval (BinApp(binop, exp1, exp2)) args =
    (binopToFun binop) (eval exp1 args, eval exp2 args)

(* Intex.binop -> int * int -> int *)
and binopToFun Add = op+
  | binopToFun Mul = op*
  | binopToFun Sub = op-
  | binopToFun Div = (fn(x,y) => x div y)
  | binopToFun Rem = (fn(x,y) => x mod y)
```

Intex 6

## Intex Interpreter With Error Checking

```
exception EvalError of string

(* Intex.pgm -> int list -> int *)
fun run (Intex(numargs, exp)) args =
  if numargs <> length args
  then raise EvalError
      "Mismatch between expected and actual number of args"
  else eval exp args

(* Intex.exp -> int list -> int *)
and eval (Int i) args = i
  | eval (Arg index) args =
    if (index <= 0) orelse (index > length args)
    then raise EvalError "Arg index out of bounds"
    else List.nth(args, index-1)
  | eval (BinApp(binop, exp1, exp2)) args =
    let val i1 = eval exp1 args
        val i2 = eval exp2 args
    in (case (binop, i2) of
        (Div, 0) => raise EvalError "Division by 0"
        | (Rem, 0) => raise EvalError "Remainder by 0"
        | _ => (binopToFun binop) (i1, i2))
    end
```

Intex 7

## Try it out

```
- run (Intex(1, BinApp(Mul, Arg 1, Arg 1))) [5];
val it = 25 : int

- run (Intex(1, BinApp(Div, Arg 1, Arg 1))) [5];
val it = 1 : int

- run (Intex(1, BinApp(Div, Arg 1, Arg 1))) [0];
uncaught exception EvalError

- run avg [5,15];
val it = 10 : int

- map (run f2c) [[~40], [0], [32], [98], [212]];
val it = [~40, ~18, 0, 36, 100] : int list
```

Intex 8

## Handling Errors

```
(* Intex.pgm -> int list -> string *)
fun testRun pgm args =
  Int.toString (run pgm args) (* Convert to string so
same type as error messages below *)
  handle EvalError msg => "EvalError: " ^ msg
  | other => "Unknown exception: " ^ (exnMessage other)
```

```
- testRun (Intex(1, BinApp(Div, Arg 1, Arg 1))) [5];
val it = "1" : string

- testRun (Intex(1, BinApp(Div, Arg 1, Arg 1))) [0];
val it = "EvalError: Division by 0" : string

- map (testRun f2c) [[~40], [0], [32], [98], [212]];
val it = ["~40", "~18", "0", "36", "100"] : string list
```

Intex 9

## Intex programs as S-expression strings

Intex(1, BinApp(Mul, Arg 1, Arg 1))

"(intex 1 (\* (\$ 1) (\$ 1)))"

Intex(2,
BinApp(Div,
BinApp(Add, Arg 1, Arg 2),
Int 2))

"(intex 2 (/ (+ (\$ 1) (\$ 2)) 2))"

Intex(1,
BinApp(Div,
BinApp(Mul,
BinApp(Sub, Arg 1, Int 32),
Int 5),
Int 9))

"(intex 1 (/ (\* (- (\$ 1) 32) 5) 9))"

Intex 10

## Running Intex programs as S-expression strings

```
(* string -> string -> string *)
fun testRun' pgmSexpString argsSexpString =
  testRun (stringToPgm pgmSexpString)
  (sexpStringToIntList argsSexpString)
  handle SexpError (msg, sexp) =>
    ("SexpError: " ^ msg ^ " " ^ (Sexp.sexpToString sexp))
  | Sexp.IllFormedSexp msg =>
    ("SexpError: Ill-formed sexp " ^ msg)
  | other => "Unknown exception: " ^ (exnMessage other)
```

```
- testRun' "(intex 2 (/ (+ ($ 1) ($ 2)) 2))" "(5 15)";
val it = "10" : string

- map (testRun' "(intex 1 (/ (* (- ($ 1) 32) 5) 9)))"
=  ["(~40)", "(0)", "(32)", "(98)", "(212)"];
val it = ["~40", "~18", "0", "36", "100"] : string list

- map (testRun' "(intex 1 (/ ($ 1) ($ 1))))"
=  ["(~17)", "(0)", "(42)"];
val it = ["1", "EvalError: Division by 0", "1"] : string list
```

Intex 11

## A Read-Eval-Print Loop (REPL) in Intex

```
- repl();
intex> (+ 1 2)
3

intex> (#args 6 7)

intex> (+ ($ 1) ($ 2))
13

intex> (* $1 $2)
42

intex> (#run (intex 2 (/ (+ ($ 1) ($ 2)) 2)) 5 15)
10

intex> (#run "avg.itx" 5 15)
10

intex> (#run avg.itx 5 15)
10

intex> (#quit)
Moriturus te saluto!
```

Intex 12

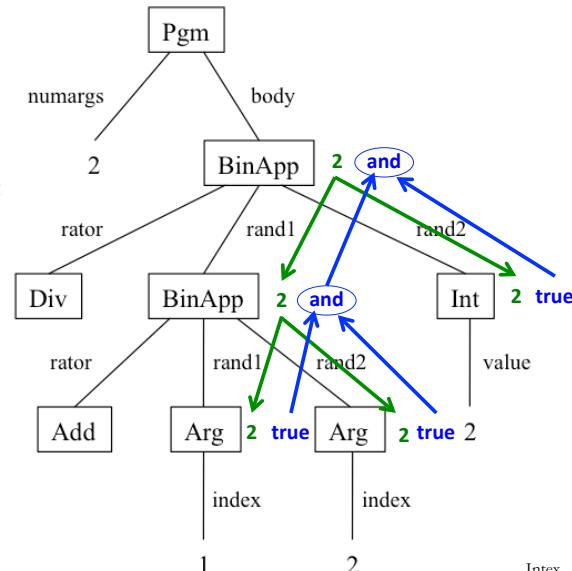
## What do we know about this program?

```
val test = Intex(2,
                 BinApp(Sub,
                         BinApp(Mul, Arg 1, Arg 3),
                         Arg 2))
```

Intex 13

## Static Arg Index Checking: Top Down (PS9)

1. In top-down phase, pass numargs to every subexpression in program.
2. Check numargs against every Arg index.
- 2a. Return **true** for Arg indices that pass test and subexprs without arg indices
- 2b. Return **false** if any Arg index fails test.



Intex 15

## Dynamic vs. Static Checking: Arg Indices

### Dynamic check (at runtime) :

```
| eval (Arg index) args =
  if (index <= 0) orelse (index > length args)
  then raise EvalError "Arg index out of bounds"
  else List.nth(args, index-1)
```

### Static check (at compile time or checking time, before runtime) :

*Idea:* We know numargs from program, so can use this to check all argument references without running the program.

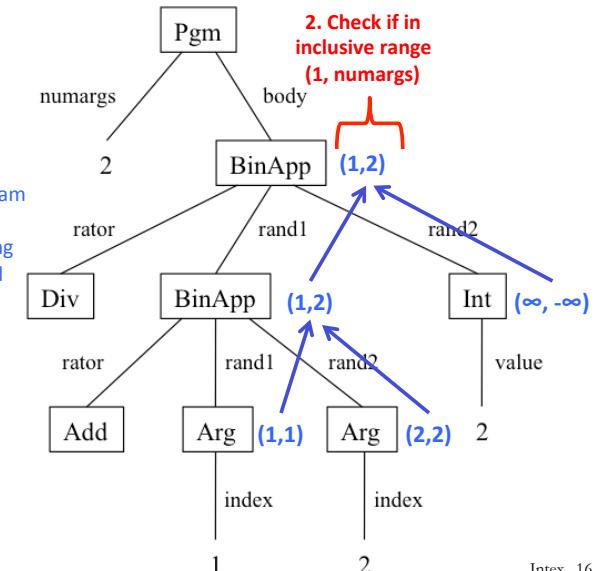
Such checks are done by examining the program syntax tree. Often there is a choice between a *bottom-up* and *top-down* approach to processing the tree.

You will do both approaches for Arg index checking in PS9.

Intex 14

## Static Arg Index Checking: Bottom Up (PS9)

1. Calculate (min,max) index value for every subexpression in tree in bottom-up fashion
2. Compare (min,max) value at root of program body expression to (1, numargs), returning **true** if a subrange and **false** otherwise



Intex 16



## Intex Implementation #2: Intex-to-Postfix-compiler in SML

Given an avg-in-Intex program, how can we execute it?

```
avg machine (I)
  avg-in-PostFix program
    avg-in-Intex program
    Intex-to-PostFix-compiler machine
      Intex-to-PostFix-compiler-in-SML program
      SML interpreter machine in wx VM (ignore details)
  PostFix interpreter machine (I)
    PostFix-in-SML-interpreter program
    SML interpreter machine in wx VM (ignore details)
```

Intex 17

## Can we automate this process?

Yes! We can define an `intexToPostFix` function with type `Intex.pgm -> PostFix.pgm` and then use it like this:

```
fun translateString intexPgmString =
  PostFix.pgmToString
  (intexToPostFix (Intex.stringToPgm intexPgmString))

- translateString "intex 1 (* ($ 1) ($ 1))";
val it = "(postfix 1 1 nget 2 nget mul)" : string

- translateString "intex 2 (/ (+ ($ 1) ($ 2)) 2))";
val it = "(postfix 2 1 nget 3 nget add 2 div)" : string

- translateString "intex 4 (* (- ($ 1) ($ 2)) (/ ($ 3) ($ 4))))";
val it = "(postfix 4 1 nget 3 nget sub 4 nget 6 nget div mul)" : string
```

Intex 19

## Hand-Compiling Intex to PostFix

Manually translate the following Intex programs to equivalent PostFix programs:

```
(intex 0 (* (- 7 4) (/ 8 2)))
(intex 4 (* (- $1 $2) (/ $3 $4)))
```

Solutions:

```
(postfix 0 7 4 sub 8 2 div mul)

(postfix 4 1 nget ; $1
  3 nget ; $2, know that $1 on stack
  sub ; (- $1 $2)
  4 nget ; $3, know that (- $1 $2) on stack
  6 nget ; $4, know that $3 and (- $1 $2) on stack
  div ; (/ $3 $4)
  mul ; (* (- $1 $2) (/ $3 $4)))
```

**Reflection:** How did you figure out how to translate  
Intex Arg indices into PostFix Nget indices?

Intex 18



## intexToPostFix Solution

```
(* val intexToPostFix: Intex.pgm -> PostFix.pgm *)
fun intexToPostFix (Intex.Intex(numargs, exp)) =
  PostFix.PostFix(numargs, expToCmds exp 0)
(* 0 is the initial depth argument *)

(* val expToCmds: Intex.exp -> PostFix.cmd list *)
(* depth arg statically tracks how many values are on stack
   above the program arguments *)
and expToCmds (Intex.Int i) depth = [PostFix.Int i]
| expToCmds (Intex.Arg index) depth =
  [PostFix.Int (index + depth), PostFix.Nget]
  (* specified argument is on stack at index + depth *)
| expToCmds (Intex.BinApp(binop,expl,exp2)) depth =
  (expToCmds expl depth)
  (* 1st rand is at same depth as whole binapp *)
  @ (expToCmds exp2 (depth + 1))
  (* for 2nd rand, add 1 to depth to account for 1st rand *)
  @ [PostFix.Arithop (binopToArithop binop)]

and binopToArithop Intex.Add = PostFix.Add
| binopToArithop Intex.Sub = PostFix.Sub
| binopToArithop Intex.Mul = PostFix.Mul
| binopToArithop Intex.Div = PostFix.Div
| binopToArithop Intex.Rem = PostFix.Rem
```

Intex 20