Wellesley CollegeCS301 Compiler Design
Handout #10 (Revised)November 9, 2000

THE BOBCAT REFERENCE MANUAL

Important changes from the initial draft:

- In addition to being well-typed, a legal Bobcat program must not define the same global variable or function name twice (see Section 3). This constraint considerably simplifies the interpretation and compilation of Bobcat programs.
- error expressions now carry an explicit type. This significantly simplifies type checking. See the modified form for error in the grammar of Fig. 1 and the typing rules of Fig.2.
- The [relop] rule in Figure 2 has changed to allow comparison of two values at any base type (see Section 3 for a discussion). This obviates previously presented standard library functions for comparing characters (charLt, charLeq, charGeq, charGt).
- The return type of a function can be any expression type. This includes base types (as before) but also includes the new void type keyword (new). Function declarations not declaring an explicit return type effectively desugar into ones with a void return type (see Section 2.3).
- The previous typing rules were missing a rule for a top level program. This has now been added (the [globalLet] rule of Fig. 3), along with some text in Section 3 explaining it.
- The grammar for the top-level (program) let construct has been extended to allow multiple semi-colon separated expressions in the body. The previously posted grammar was also missing an end keyword.
- An ambiguity in the specification of the parsing of if, while, for, and assignment expressions has been resolved in Section 2.2.
- A new desugaring for top-level programs is given in Section 2.3. This supersedes the desugaring presented in the previous version of the Bobcat reference manual.

1. Overview

Bobcat is an extension to Kitty that supports global, first-order, mutually recursive functions and three primitive data types (booleans, characters, and integers). The key differences between Bobcat and Kitty are as follows:

- 1. Whereas all Kitty values are integers, Bobcat supports three types of values: booleans, characters, and integers. It is illegal to use values of one type in a context where a value of another type is expected. This property is enforced by static type checking rules (see Section 3), which can be used to reject ill-typed programs at compile-time. Only the semantics of well-typed programs are defined.
- 2. Bobcat allows the definition of collections of mutually recursive functions that can refer to global variables. Function parameters and results have explicitly declared types.
- 3. Bobcat supports a library of standard functions that subsume and extend Kitty's nullary and unary operators.
- 4. Bobcat has a simple construct for aborting the program upon encountering an error.

Like Kitty, Bobcat is essentially a subset of Appel's Tiger language.¹ The key features of Tiger not supported by Kitty are (1) record and array datatypes and (2) block structured function declarations.

¹ We say "essentially" because while Bobcat's functions are take from Tiger, Bobcat has a few features that Tiger does not have. In particular: Bobcat supports characters as a disintct datatype, which Tiger does not; (2) Bobcat has

We will use Bobcat as our source language in our second pass at exploring the stages of compilation. Once we complete this second pass, we will consider extensions to Bobcat that support additional Tiger features.

2. Syntax

2.1 Lexical Conventions

The lexical conventions for Bobcat are exactly the same as those of the Kitty language. See the Kitty Reference Manual for details.

2.2. Grammar

Syntactically well-formed core Kitty programs are those derivable from the grammar in Figure 1. We use the following conventions in the grammar:

- Bold unitalicized names are terminal symbols that stand for classes of tokens.
- Plain unitalicized names are terminal symbols that stand for single tokens with those names.
- Italicized names are non-terminal symbols in the grammar, whose meanings are defined by productions.
- Italicized annotations following the hash mark (#) are comments and not part of the grammar.
- If toks is a sequence of tokens, then {toks} stands for zero or more repetitions of toks.
- If toka1 and toka2 are sequences of tokens, then {toks1 [toks2]} stands for zero or more repetitions of toks1 that are separated by toka2.

Note that Bobcat variable and function declarations are not separate by semi-colons.²

The grammar in Figure 1 is ambiguous. The ambiguities are removed by the following rules, which are the same as those in Kitty³:

Precedence: The precedence of operators from highest to lowest is as follows (operators on the same line have the same precedence):

```
unary minus (negation)
*, /, %
+, -
<, <=, =, <>, >=, >
&
|
```

Associativity: The operators *, \backslash , *, +, -, &, and | are all *left-associative*. E.g., 1 - 2 + 3 is parsed as if it were written (1 - 2) + 3. The relational <, <=, =, <>, >=, and > are all *non-associative*. E.g., 1 < 2 = 3 is not a legal expression, even though the explicitly grouped versions (1 < 2) = 3 and 1 < (2 = 3) are legal expressions.

several standard library functions not suported by Tiger; (3) Bobcat's error construct does not appear in Tiger; (4) Bobcat's program syntax is more lenient than Kitty's; and (5) Bobcat inherits from Kitty a few non-Tiger features (constants, writes).

 $^{^{2}}$ Kitty declarations *were* separated by semi-colons, but this was a mistake on my part based on a misreading of the Tiger grammar. Tiger declarations are *not* separated by any symbols, either.

³ The Kitty reference manual did not list the weak precedence of keywords rule, but it should have!

```
# Prog derives Bobcat expressions
Prog let {GlobalDecl} in {Exp[;]} end # top-level program
# The following expressions are inherited from Kitty
# Exp derives Bobcat expressions
      () # the literal for "no value"
Exp
      intlit # as specified by the lexical conventions for integer literals
Exp
      charlit # as specified by the lexical conventions for character literals
Exp
      id # as specified by the lexical conventions for identifiers
Exp
Exp
      Const
      -Exp # unary minus operator
Exp
      writes (stringlit)
Exp
      Exp Binop Exp
Exp
      id := Exp # assignment
Exp
Exp if Exp then Exp else Exp
     if Exp then Exp
Exp
      let {VarDecl} in {Exp [;]} end
Exp
      while Exp do Exp
Exp
      for ident := Exp to Exp do Exp
Exp
    (Exp ; {Exp[;]}) # sequence expression, parentheses required
Exp
      (Exp) # grouping via optional parentheses
Exp
# The following expressions are new to Bobcat
      id ({Exp [,]}) function application
Exp
      error ExpTy stringlit
Exp
# VarDecl derives variable declarations
VarDecl var id := Exp
VarDecl var id : BaseType := Exp
# VarDecl derives variable declarations
FunDecl
         function id ({Formal[,]}) : ExpType = Exp
FunDecl function id ({Formal[,]}) = Exp
# Formal derives formal
                                     # Binop derives binary operators
# argument declarations
                                    Binop
                                             Arithop
Formal id : BaseType
                                    Binop
                                             Relop
                                    Binop
                                             Logop
# GlobalDecl derives global
# variable or function decls
                                    Arithop
                                               +
GlobalDecl VarDecl
                                    Arithop
                                               _
                                               *
GlobalDecl FunDecl
                                    Arithop
                                    Arithop / # integer division
                                    Arithop % # integer modulus
# ExpType derives expr. types
ExpType BaseType
ExpType void
                                    Relop
                                             <
                                    Relop
                                             <=
# BaseType derives base types
                                    Binop
                                             =
BaseType bool
                                    Binop
                                             <> # not equals
BaseType
           char
                                    Relop
                                             >=
           int
BaseType
                                    Relop
                                             >
                                             & # short circuit and
# Const derives constants
                                   Logop
Const minint
                                    Logop # short circuit or
Const maxint
Const true
Const false
```

Figure 1: Bobcat Grammar

Dangling Else: The presence of both if-then and if-then-else expressions in a language introduces an ambiguity as to which if expression an else clause belongs. The Kitty convention (as in many other languages) is that an else clause belongs to the innermost if expression enclosing it. Thus, the expression

if E_1 then if E_2 then E_3 else E_4

is parsed as if it were written

if E_1 then (if E_2 then E_3 else E_4)

Weak precedence of keyword expressions: It is assumed that keyword expressions (if, while, for) bind less tightly than binary operator expressions. In other words, the final expression of a keyword expression should be interpreted as extending as far right as possible. For these purposes, assignment is considered a keyword expression. For example:

Expression	parses as	and not as
if <i>E1</i> then <i>E2</i> + <i>E3</i>	if <i>E1</i> then (<i>E2</i> + <i>E3</i>)	(if <i>E1</i> then <i>E2</i>) + <i>E3</i>
if <i>E1</i> then <i>E2</i>	if <i>E1</i> then <i>E2</i>	(if <i>E1</i> then <i>E2</i>
else <i>E3</i> + <i>E4</i>	else (<i>E3</i> + <i>E4</i>)	else <i>E3</i>) + <i>E4</i>
x := E1 + E2	x := (E1 + E2)	(x := E1) + E2
while E1 do x $:= E2 + E3$	while E1 do x $:= (E2+E3)$	(while $E1$ do x := $E2$)+ $E3$
for i := $E1$ to $E2$ do	for i := $E1$ to $E2$ do	(for i := <i>E1</i> to <i>E2</i> do
x := E3 + E4	x := (E3 + E4)	x := E3) + E4

2.3. Desugaring

It is inconvenient to write an explicit let ... in ... end for every top-level Bobcat program. Following the conventions of the C programming language, Bobcat supports the following desugaring for Bobcat programs:

 $GlobalDecl_1 \dots GlobalDecl_n$ let $GlobalDecl_1 \dots GlobalDecl_n$ in main() end

That is, a Bobcat program can be written as a *non-empty* sequence of declarations, one of which is assumed to be a declaration of a function main of type () void. Executing the program is equivalent to invoking main with no arguments. It is also convenient to be able to process single Kitty expressions as if they were Bobcat programs. For this reason, Bobcat also supports the following desugaring for top-level expressions into Bobcat programs: *Exp* let in *Exp* end

Several of the Bobcat expressions in Figure 1 can be viewed as desugaring into other expressions, as illustrated in the following table:

Source language expression	Expression after desugaring
for $I_1 := E_1$ to E_2 in E_3	let var $I_1 := E_1$
	var I_2 := E_2 (* Assume I_2 fresh *)
	in while $(I_1 \le I_2)$ do
	$(E_3; I_1 := I_1 + 1)$
	end
if E_1 then E_2	if E_1 then E_2 else ()
E_1 & E_2	if E_1 then E_2 else false
$E_1 \mid E_2$	if E_1 then true else E_2
$-E_1$	$0 - E_1$
<pre>writes("abc")</pre>	(writec('\a');
	<pre>writec('\b');</pre>
	<pre>writec('\c');</pre>
)

Note that the desugaring for $E_1 | E_2$ is different than that used in Kitty. This is because the operands of | in Kitty are integers, while the operands of | in Bobcat must be boolean. For example, 2 | 3 is a legal Kitty program that should evaluate to 2, but it is an illegal Bobcat program.

Unlike Tiger, Bobcat allows the void expression type to be explicitly written in a program. Because of this, the function declarations that do not list an explicit return type, e.g., those of the form

id (id₁: $BaseType_1$, ..., id_n : $BaseType_n$),

effectively desugar into declarations with void as an explicit return type:

id (id₁: $BaseType_1$, ..., id_n : $BaseType_n$) : void

3. Static Semantics

The *static semantics* of a language describes those properties that can be determined at compiletime – i.e., without executing the program. A Bobcat program has to satisfy two static properties in order to be considered *valid*:

- The global variable and function names in a program must be pairwise distinct and also distinct from any standard library function name. For instance, the name f cannot be declared twice as a global variable and/or function, nor can the name abs be declared as a global variable or function (because it is already in the standard library).
- A program must be well-typed according to the typing rules shown in Figures 2 and 3. These are explained further below.

The typing rules for Bobcat refer to types in the following domains:

BT BaseTy = {bool, int, char} ET ExpTy = BaseTy {void} FT FunTy = BaseTy * × ExpTy

The metavariables BT, ET, and FT will be used to range over elements of these types. The notation (BT_1, \dots, BT_n) ET will be used to stand for a function type in FunTy.

The typing rules use type environments, which are finite partial mappings from variable names to *BaseType* FunctionType. If A is a type environment, then the notation A(x) refers to the base type or function type associated with variable x in the environment (if there is such a type). The notation $A[x_i := T_1, ..., x_n := T_n]$ denotes a type environment that, for all *i* in the range [1...n] binds x_i to T_i (a base type or function type) and binds every y not in the set { $x_1, ..., x_n$ } to A(y).

The typing rules involve four different kinds of judgements:

- The judgement *Prog* claims that program *Prog* is statically valid in terms of its types.
- The judgement $A \triangleright Exp$: *ET* claims that expression *Exp* has type *ET* with respect to type environment *A*..

- The judgement $A \quad Decl_1 \quad \dots \quad Decl_n \quad A'$ claims that type environment A can be extended to type environment A' by processing a sequence of declarations, where each $Decl_1$ is either a single variable declaration or a mutually recursive set of function declarations.
- The judgement A Decl A' claims that A can be extended to A' by processing a "single" declaration Decl (which may be a single variable declaration or a mutually recursive set of function declarations).

The "claims" made by judgements are not necessarily true. For instance, the following is a well-formed judgement that is false: {} $\triangleright 1$: bool. (Here, {} stands for the empty type environment.) A judgement is considered true if and only if there is derivation (i.e., a finite proof tree) consisting of instantiations of the typing rules in which every hypothesis of a rule instantiation is the conclusion of some other rule instantiation. An expression *Exp* is said to *be well-typed with respect to a type environment A* if there exists an expression type *ET* such that the judgement $A \triangleright E : ET$ can be derived from instantiations of the typing rules. A program *Prog* is said to be *well-typed* if the judgement *Prog* can be derived from instantiations of the typing rules.

The complete typing rules for Bobcat appear in Figures 2 and 3. The figures show typing rules only for "core" expressions; expressions that can be derived by desugaring are first assigned to be desugared before they are type-checked. The [group] rule is included for completeness only because all the other rules are expressed in terms of the concrete syntax of Bobcat. There would be no need for the [group] rule in the abstract syntax for Bobcat.

The [relop] rule specifies that the Bobcat relational operators can be used to compare any two values that have the same base type. For instance, all of the following expressions are legal in a well-typed Bobcat program: 5 < 3, 'h' < 'q', true < false. However, any attempt to compare values of different types, as in 5 < 'q', false < 'q', or true < 3, is a type error. Such operators, which have different meanings at different types, are said to be *overloaded*.

Some of the typing rules have side conditions, which are conditions that must be true in order for the rule to be applicable. The use of a metavariable in a side condition implies that the side condition is only true if the metavariable can be properly instantiated. For example, the following side condition appears in the [varRef] and [assign] rules:

where A(id) = BT

This side condition means that the type associated with **id** in the type environment A must be a base type, and that this base type will be named *BT* when used elsewhere in the rule.

[nothing] ------ [intLit] ----- [charLit] ------ $A \triangleright ()$: void A ▷ **intlit** : int A ▷ **charlit** : char [trueConst] ----- [falseConst] -----A ▷ true : bool $A \triangleright false : bool$ [maxintConst] ------ [minintConst] -------A ▷ maxint : int $A \triangleright minit : int$ $A \triangleright Exp_1$: int ; $A \triangleright Exp_2$: int [arithop] ------ $A \triangleright Exp_1$ Arithop Exp_2 : int $\textbf{A} \vartriangleright \textit{Exp}_1 : \textit{BT}; \textit{A} \vartriangleright \textit{Exp}_2 : \textit{BT}$ [relop] ------ $A \triangleright Exp_1 Relop Exp_2$: bool [varRef] ----- where A(id) = BT $A \triangleright id : BT$ $A \triangleright Exp : BT$ [assign] ----- where A(id) = BT $A \triangleright id := Exp : void$ $A \triangleright Exp_1$: bool ; $A \triangleright Exp_2$: ET ; $A \triangleright Exp_3$: ET [if] -----_____ $A \triangleright if Exp_1$ then Exp_2 else Exp_3 : ET $A \triangleright Exp_1$: bool ; $A \triangleright Exp_2$: void [while] ------ $A \triangleright$ while Exp_1 do Exp_2 : void i [1..n] . A \triangleright Exp $_i$: ET $_i$ [seq] ------ $A \triangleright (Exp_1; \ldots; Exp_n) : ET_n$ $A \quad VarDecl_1 \dots VarDecl_k \quad A'; \quad i [1..n] \quad A' \triangleright Exp_i : ET_i$ [localLet] ------ $A \triangleright \text{let } VarDecl_1 \dots VarDecl_k \text{ in } Exp_1, \dots, Exp_n \text{ end } : ET_n$ i [1..n] . A $\triangleright Exp_i$: BT_i [funApp] ----- where $A(id) = (BT_1, \ldots, BT_n)$ ET $A \triangleright id (Exp_1, \ldots, Exp_n) : ET$ $A \triangleright Exp : ET$ [group] ------ [error] ------ $A \triangleright \text{error } ET \quad (\text{stringlit}) : ET$ $A \triangleright (Exp) : ET$

Figure 2: Typing Rules, Part 1

$$i [1..n] \cdot A_{i-1} \quad GlobalDecl_i \quad A_i$$

$$[decls] \quad \dots \quad A_0 \quad GlobalDecl_1 \quad \dots \quad GlobalDecl_n \quad A_n$$

$$[varDeclUntyped] \quad \dots \quad A \quad var \quad id := Exp \quad A[id := BT]$$

$$[varDeclTyped] \quad \dots \quad A \quad var \quad id := Exp \quad A[id := BT]$$

$$[varDeclTyped] \quad \dots \quad A \quad var \quad id : BT := Exp \quad A[id := BT]$$

$$[funDecls] \quad \dots \quad I[1..n] \cdot A' \triangleright Exp_i : ET_i$$

$$function \quad id_i(id_{(1,1)}:BT_{(1,1)}, \dots, id_{(1,k1)}:BT_{(1,k1)}):ET_i = Exp_n \quad A'$$

$$where \quad A' = A[id_1 := (BT_{(1,1)}, \dots, BT_{(1,k1)}) \quad ET_i,$$

$$id_n := (BT_{(n,1)}, \dots, BT_{(n,kn)}) \quad ET_n]$$

$$[gloabalLet] \quad \dots \quad GlobalDecl_i \quad \dots \quad GlobalDecl_k \quad A'; A' \triangleright Exp : void$$

$$[gloabalLet] \quad \dots \quad Dcomposition \quad Dc$$

where A_{stdlib} is a type environment for the Bobcat standard library

Figure 3: Typing Rules, Part 2

4. Dynamic Semantics

The *dynamic semantics* of a language describes the run-time meaning of phrases in the language. The dynamic semantics of Bobcat is similar to that of Kitty, except for the following differences:

- Meaning is only ascribed to valid Bobcat programs. In contrast, every Kitty expression has a meaning. This simplifies the implementation of Bobcat interpreters and compilers, which may be predicated on the assumption that only valid programs will be interpreted/compiled. For example, when adding two values, a Bobcat interpreter need not check that both are integers, since this fact has already been proven by the type checker.
- A Bobcat expression can denote one of four kinds of values: a boolean, a character, an integer, or "no value". In contrast, a Kitty program can only denote two kinds of values: an integer or "no value".

- Bobcat supports the declaration and application of global, mutually recursive functions. The meaning of a function application $id(E_1, \ldots, E_n)$ is determined via the following steps:
 - 1. Evaluate the actual parameters E_1, \ldots, E_n from left to right into values v_1, \ldots, v_n . (In a valid program, it is guaranteed all such values will be of base type.)
 - 2. Suppose that there is a corresponding global function declaration

function $\mathbf{id}(\mathbf{id}_1:E_1, \ldots, \mathbf{id}_n:E_n): T = E_{body}$

(In a valid program, it is guaranteed that there is such a declaration, and it is unique.) Evaluate the body expression E_{body} in a context where the formal parameters id_1 , ..., id_n stand for the actual parameter values v_1, \ldots, v_n and any non-shadowed global variables stand for their global value. In the case where T is a base type, the result of the evaluation of body will be a value of type T, and this value should be returned as the value of the function application. In the case where T is void, both the body and the function application will have no value.

- The Bobcat standard I/O library readc function (see Section 5) always returns a character. In contrast, the Kitty readc unary operator returns an integer, where an integer in the range 0-255 is interpreted as a character with that ASCII value and -1 is interpreted as indicating the end-of-file. Since there is no end-of-file character, Bobcat needs a separate standard I/O library function eof() to detect the end-of-file condition.
- For any Kitty expression *E*, if the Bobcat program let in *E* end is valid, then this program has the same behavior as the Kitty expression as long as *E* does not contain an invocation of readc().

5. Standard Library Functions

Top-level Bobcat programs are assumed to be type-checked and executed relative to an "toplevel environment" that includes bindings for functions in a standard library. Separating the specification for the standard library from that of the core language simplifies both the description and implementation of the language. It also provides a modular way to extend the language with new library functions without having to change the specification or implementation of the core language.

This section documents the functions in the Bobcat standard library. They are loosely organized into categories of related functions:

Mathematical Functions

abs (x: int): int Returns the absolute value of x.

expt (base: int, power: int): int Returns the result of raising base to power. Signals an error if power < 0.</pre>

sqr (x: int): int Returns the result of squaring x.

Logic Functions

not (b: bool): bool Returns the logical negation of b.

and (b1: bool, b2: bool): bool Returns the logical conjunction of b1 and b2. Unlike the short-circuit conjunction operator &, and always evaluates both arguments.

or (b1: bool, b2: bool): bool Returns the logical disjunction of b1 and b2. Unlike the short-circuit disjunction operator |, or always evaluates both arguments.

boolToInt (b: bool): int
Returns 0 for true and 1 for false.

intToBool (i: int): bool
Returns true for 0 and false for any other integer.

Character Functions

chr (i: int): char Returns the character corresponding to ASCII value i.

ord (c: char): int Returns the ASCII value of character c.

digitToInt (d: char): int If d is a digit character, returns the numerical value of the digit; otherwise signals an error.

intToDigit (i: int): char If i is a number in the range [0..9], returns the digit character corresponding to the number; otherwise, signals an error.

isDigit (c: char): bool
Returns true if c is a digit, and false otherwise.

isLetter (c: char): bool
Returns true if c is a letter, and false otherwise.

isLowercase (c: char): bool Returns true if c is a lowercase letter, and false otherwise.

isUppercase (c: char): bool Returns true if c is an uppercase letter, and false otherwise.

isWhitespace (c: char): bool Returns true if c is a whitespace character, and false otherwise.

lowercase (c: char): char If c is an uppercase character returns the corresponding lowercase character; otherwise returns c.

uppercase (c: char): char If c is a lowercase character returns the corresponding uppercase character; otherwise returns c.

Input/Output Functions

eof : () bool

Returns true if the standard input stream is empty (i.e., if performing readc would signal an error) and returns false otherwise.

readc : () char Consumes and returns the next character from standard input stream. Signals an error if standard input is empty.

readi : (int) int

readi(default) first consumes any whitespace characters (spaces, tabs, and newlines) in the standard input stream. If the first non-whitespace character is a digit, or a minus sign followed by a digit, the maximal sequence of characters interpretable as an integer is consumed, and the integer represented by these characters is returned. However, if the first non-whitespace character is not the first character of an integer representation, it is not consumed, and the value default is returned. Thus, default serves as an indication of the failure of readi to read an integer. It is helpful to parameterize over this value because different failure values are suitable in different contexts.⁴ For instance, 0, -1, minint, and maxint are all typical values of the argument to readi.

writec : (char) void
writec(c) writes character c to standard output stream.

writei : (int) void
writei(i) writes a string representation of integer I to standard output stream.

6. Examples

6.1 Count

Here is a Bobcat program that counts the number of characters in the standard input stream:

```
let
  var count := 0
  function inc() = count := count + 1
in
  while not(eof()) do (readc(); inc());
  writei(count)
end
```

By the program desugaring in Section 2.3, this can also be written as:

```
var count := 0
function inc() = count := count + 1
function main () : void =
  (while not(eof()) do (readc(); inc());
  writei(count))
```

⁴ Of course, any attempt to encode a failure value as an integer necessarily means that there can be an ambiguity between actually reading that integer and reading no integer. In more advanced languages, this problem can be dealt with by either returning a compound data structure (such as ML's int option) that can represent failure as a value distinct from the integers, or by raising an exception when no integer is read.

Since mutually recursive functions can be in any order, this can be rewritten as:

```
var count := 0
function main () : void =
  (while not(eof()) do (readc(); inc());
  writei(count))
function inc() = count := count + 1
```

However, both of the following are invalid: the first because inc is unbound in the body of main, due to the fact that the count variable declaration breaks up the mutual recursion between main and inc; and the second because the variable count is unbound in the bound of inc.

```
/* Invalid program 1 */
function main () : void =
   (while not(eof()) do (readc(); inc());
   writei(count))
var count := 0
function inc() = count := count + 1
/* Invalid program 2 */
function main () : void =
   (while not(eof()) do (readc(); inc());
   writei(count))
function inc() = count := count + 1
var count := 0
```

6.2 Even/Odd

Here is a program that uses the classic mutually recursive definitions of functions that compute the evenness and oddness of an integer:

```
function main() = writei(test())
function test (): int =
  let var sum := 0
   in for i := 0 to 3 do
          sum := sum + expt(10,2*i) * boolToInt(even(2*i))
                     + expt(10,2*i+1) * boolToInt(even(2*i+1));
      sum
  end
function even (n: int): bool =
  if n = 0 then
    true
  else
    odd(n-1)
function odd (n: int): bool =
  if n = 0 then
    false
  else
    even(n-1)
```

6.3 Chartable

Below is a program that prints a table of the characters whose ASCII values are between 1 and 128.

```
function isSpecial(c: char): bool =
  c = ' t' | c = ' n' | c = ' '' | c = ' ''
function specialToChar (c: char): char =
  if c = ' \setminus t' then 't'
  else if c = ' \setminus n' then 'n'
  else if c = ' \setminus '' then '\''
else if c = ' \setminus '' then '\''
  else (writec(c); error char "is not a special")
function writeChar (c: char): void =
  (writec('\'');
   if isSpecial(c) then
       (writec('\\'); writec(specialToChar(c)))
   else
      writec(c);
   writec('\'')
   )
function main () =
  for i := 0 to 127 do
    (writeChar(chr(i));
     if (i \$ 8) = 7 then writec('\n') else writec('\t')
     )
```