
From image motion, compute:

- observer translation

$$
\left(\mathrm{T}_{\mathrm{x}} \mathrm{~T}_{\mathrm{y}} \mathrm{~T}_{\mathrm{z}}\right)
$$

- observer rotation

$$
\left(\mathrm{R}_{\mathrm{x}} \mathrm{R}_{\mathrm{y}} \mathrm{R}_{\mathrm{z}}\right)
$$

- depth at every location Z(x, y)


## Observer just translates toward FOE



Directions of velocity vectors intersect at FOE

But... simple strategy doesn't work if observer also rotates

Observer motion problem, revisited

pure translation

translation + rotation

pure rotation

From image motion, compute:

- Observer translation

$$
\left(\mathrm{T}_{\mathrm{x}} \mathrm{~T}_{\mathrm{y}} \mathrm{~T}_{\mathrm{z}}\right)
$$

- Observer rotation
$\left(R_{x} R_{y} R_{z}\right)$
- Depth at every location $Z(x, y)$

Observer undergoes both translation + rotation

## Equations of observer motion

| Translation $\left(T_{x}, T_{y}, T_{z}\right)$ | $\begin{aligned} & \text { Rotation } \\ & \left(\mathbf{R}_{\mathbf{x}}, \mathbf{R}_{\mathbf{y}}, \mathbf{R}_{\mathrm{z}}\right) \end{aligned}$ | $\begin{aligned} & \text { Depth } \\ & \mathbf{Z}(\mathbf{x}, \mathbf{y}) \end{aligned}$ |
| :---: | :---: | :---: |
| $\begin{aligned} & \mathbf{V}_{\mathbf{x}}=\left(-\mathrm{T}_{\mathbf{x}}+\mathbf{x} \mathrm{T}_{\mathbf{Z}}\right) / \mathbf{Z} \\ & \mathbf{V}_{\mathbf{y}}=\left(-\mathrm{T}_{\mathbf{y}}+\mathbf{y} \mathrm{T}_{\mathrm{z}}\right) / \mathbf{Z} \end{aligned}++$ | $\mathbf{R}_{\mathrm{X}} \mathrm{xy}-\mathrm{R}_{\mathbf{y}}\left(\mathrm{x}^{2}+1\right)+\mathrm{R}_{\mathrm{z}} \mathrm{y}$ $\mathbf{R}_{\mathrm{x}}\left(\mathrm{y}^{2}+1\right)-\mathrm{R}_{\mathbf{y}} \mathbf{x y}-\mathbf{R}_{\mathbf{z}} \mathrm{x}$ |  |
| Component |  |  |

## Longuet-Higgins \& Prazdny



- Along a depth discontinuity, velocity differences depend only on observer translation
- Velocity differences point to the focus of expansion



## Alignment methods

best match the viewed image
V viewed object (image)
$\mathrm{M}_{\mathrm{i}} \quad$ object models
$\mathrm{T}_{\mathrm{ij}} \quad$ allowable transformations between viewed object and models

F measure of fit between $V$ and the expected appearance of model $\mathrm{M}_{\mathrm{i}}$ under the transformation $\mathrm{T}_{\mathrm{ij}}$
GOAL: Find a combination of $\mathrm{M}_{\mathrm{i}}$ and $\mathrm{T}_{\mathrm{ij}}$ that maximizes the fit $F$


## Alignment method: recognition process

(1) Find best transformation $T_{i j}$ for each model $M_{i}$ (optimizing over possible views)
(2) Find $M_{i}$ whose best $T_{i j}$ gives the best match to image V


Eigenfaces for recognition (Turk \& Pentland) Principal Components Analysis (PCA)

Goal: reduce the dimensionality of the data while retaining as much information as possible in the original dataset
PCA allows us to compute a linear transformation that maps data from a high dimensional space to a lower dimensional subspace


## Eigenfaces for recognition (Turk \& Pentland)



Perform PCA on a large set of training images, to create a set of eigenfaces, $\mathrm{E}_{\mathrm{i}}(\mathrm{x}, \mathrm{y})$, that span the data set

First components capture most of the variation across the data set, later components capture subtle variations
$\Psi(\mathrm{x}, \mathrm{y}):$ average face (across all faces)
http://vismod.media.mit.edu/vismod/demos/facerec/basic.html
Each face image $F(x, y)$ can be expressed as a weighted combination of the eigenfaces $E_{i}(x, y)$ :

$$
\mathrm{F}(\mathrm{x}, \mathrm{y})=\Psi(\mathrm{x}, \mathrm{y})+\Sigma_{\mathrm{i}} \mathrm{w}_{\mathrm{i}}{ }^{*} \mathrm{E}_{\mathrm{i}}(\mathrm{x}, \mathrm{y})
$$

## Face detection: Viola \& Jones

Multiple view-based classifiers based on simple features that best discriminate faces vs. non-faces

Most discriminating features learned from thousands of samples of face and non-face image windows

## Attentional mechanism:

cascade of increasingly discriminating classifiers improves performance


## Representing individual faces

Each face image $\mathrm{F}(\mathrm{x}, \mathrm{y})$ can be expressed as a weighted combination of the eigenfaces $\mathrm{E}_{\mathrm{i}}(\mathrm{x}, \mathrm{y})$ :

$$
\mathrm{F}(\mathrm{x}, \mathrm{y})=\Psi(\mathrm{x}, \mathrm{y})+\Sigma_{\mathrm{i}} \mathrm{w}_{\mathrm{i}}{ }^{*} \mathrm{E}_{\mathrm{i}}(\mathrm{x}, \mathrm{y})
$$



## Recognition process:

(1) Compute weights $w_{i}$ for novel face image
(2) Find image $m$ in face database with most similar weights, e.g.
$\min \sum_{i=1}^{k}\left(w_{i}-w_{i}^{m}\right)^{2}$

## Viola \& Jones use simple features

Use simple rectangle features:
$\sum \mathrm{I}(\mathrm{x}, \mathrm{y})$ in gray area $-\sum \mathrm{I}(\mathrm{x}, \mathrm{y})$ in white area
within $24 \times 24$ image sub-windows

- Initially consider 160,000 potential features per sub-window!
- features computed very efficiently


Which features best distinguish face vs. non-face?


Learn most discriminating features from thousands of samples of face and nonface image windows

## Learning the best features

\(\left.$$
\begin{array}{l}\text { weak classifier using one feature: } \\
h(x, f, p, \theta)= \begin{cases}1 & \text { if } p f(x)<p \theta \\
0 & \text { otherwise }\end{cases} \\
\hline \begin{array}{l}f=\text { feage wind }\end{array}
$$ <br>

p=+1 or-1\end{array}\right\}\)| $\theta=$ threshold |
| :--- |



## "Attentional cascade" of increasingly discriminating classifiers



Early classifiers use a few highly discriminating features, low threshold

- $1^{\text {st }}$ classifier uses two features, removes 50\% non-face windows

- later classifiers distinguish harder examples
- Increases efficiency
- Allows use of many more features
$\rightarrow$ Cascade of 38 classifiers, using $\sim 6000$ features

The power of averages, Burton et al. (2005)


What is an artificial neural network?


Human recognition of average faces


Burton et al. (2005)

Performance: shape-free images


Performance: texture + shape images



-

How does each unit integrate its inputs to produce an output? sum of weighted inputs $\rightarrow$ sigmoid function $\rightarrow$ output between 0 and 1


