

# Binocular Stereo Vision

Properties of human stereo processing  
Marr-Poggio-Grimson multi-resolution  
stereo algorithm

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**CS332 Visual Processing**  
Department of Computer Science  
Wellesley College

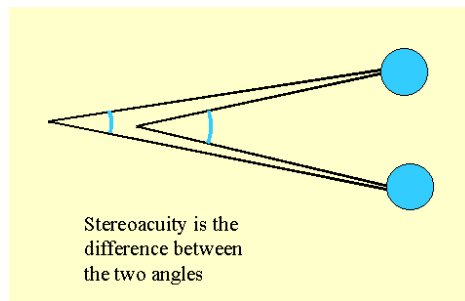
## Properties of human stereo processing



Use features for stereo matching  
whose position and disparity can be  
measured *very precisely*

*Stereoacuity* is only a few  
seconds of visual angle

difference in depth  $\approx 0.01$  cm  
at a viewing distance of 30 cm



## Properties of human stereo processing

Matching features must appear *similar* in the left and right images



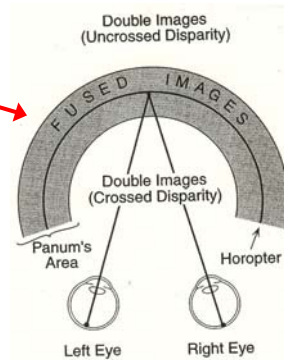
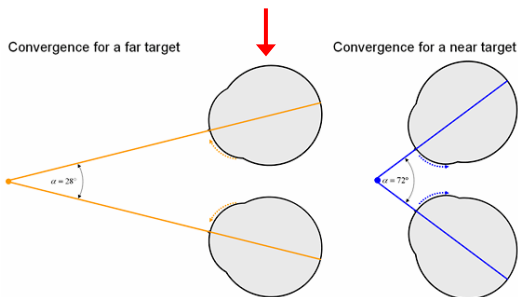
For example, we can't fuse a left stereo image with a negative of the right image...

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## Properties of human stereo processing

Only "fuse" objects within a limited range of depth around the fixation distance

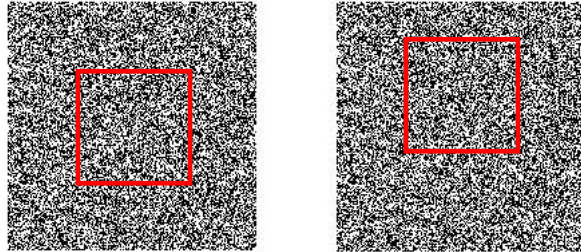
*Vergence eye movements* are needed to fuse objects over larger range of depths



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## Properties of human stereo vision

We can only tolerate small amounts of *vertical disparity* at a single eye position



Vertical eye movements are needed to handle large vertical disparities

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## Properties of human stereo processing



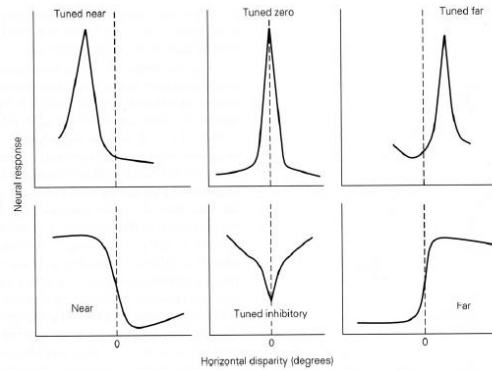
In the early stages of visual processing, the image is analyzed at *multiple spatial scales*...



Stereo information at multiple scales can be processed independently

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## Neural mechanisms for stereo processing



zero disparity: at fixation distance  
near: in front of point of fixation  
far: behind point of fixation

G. Poggio & colleagues:

complex cells in area V1 of primate visual cortex are selective for stereo disparity

neurons that are selective for a larger disparity range have larger receptive fields

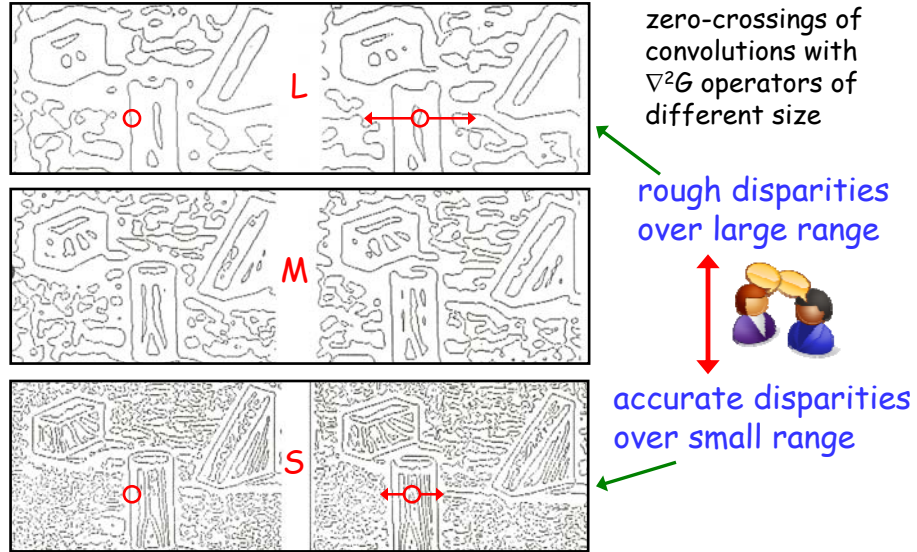
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## In summary, some key points...

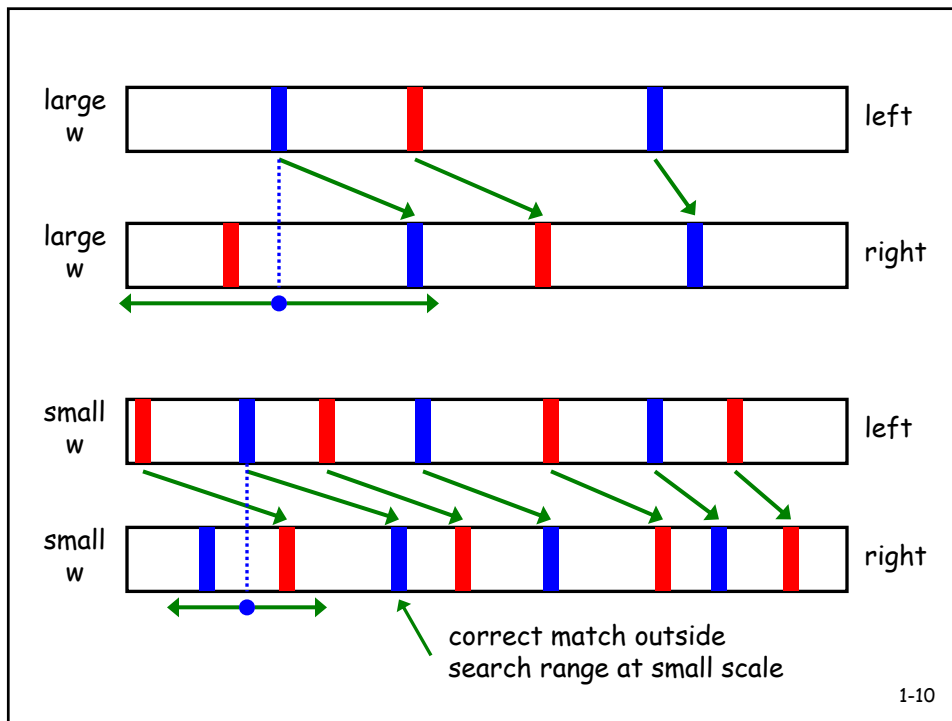
- Image features used for matching:  
simple, precise locations, multiple scales, similar between left/right images
- At single fixation position, match features over a limited range of horizontal & vertical disparity
- Eye movements used to match features over larger range of disparity
- Neural mechanisms selective for particular ranges of stereo disparity

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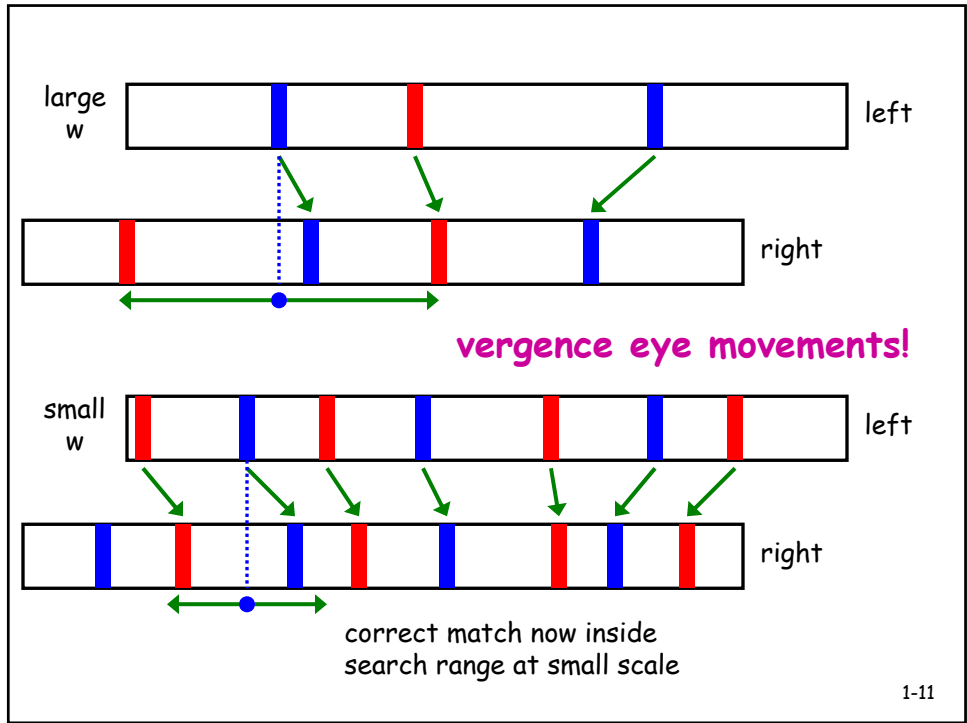
## Matching features for the MPG stereo algorithm



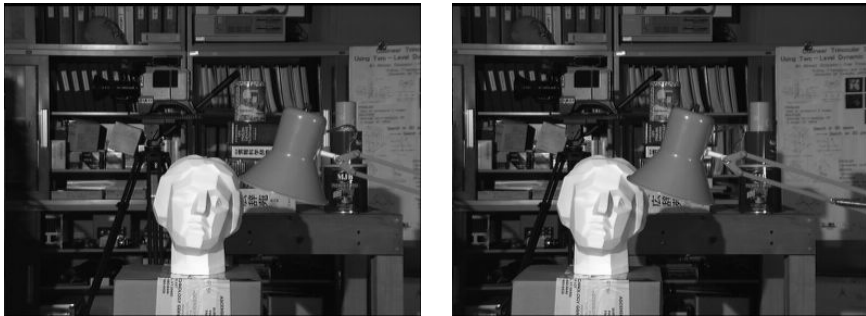
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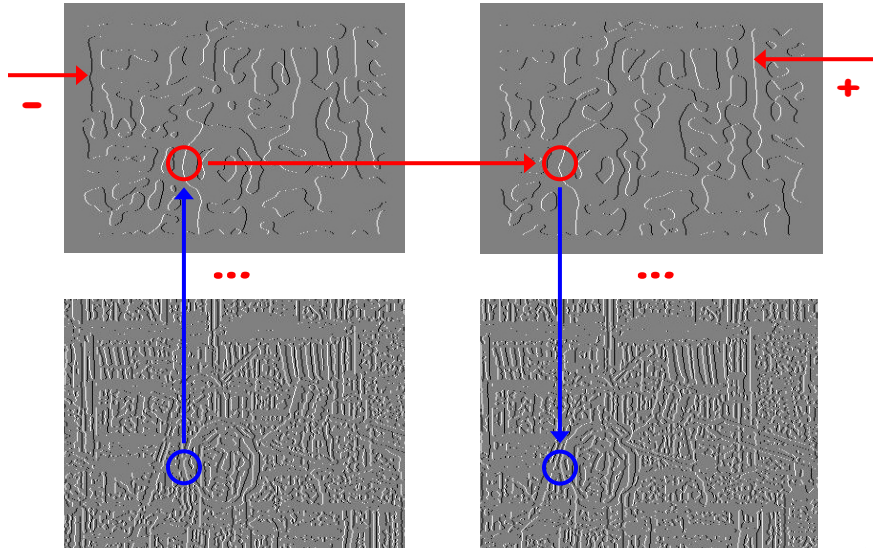
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## Stereo images (Tsukuba, CMU)



## Zero-crossings for stereo matching



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## Simplified MPG algorithm, Part 1

To determine initial correspondence:

- (1) Find zero-crossings using a  $\nabla^2 G$  operator with central positive width  $w$
- (2) For each horizontal slice:
  - (2.1) Find the nearest neighbors in the right image for each zero-crossing fragment in the left image
  - (2.2) Find the nearest neighbors in the left image for each zero-crossing fragment in the right image
  - (2.3) For each pair of zero-crossing fragments that are closest neighbors of one another, let the right fragment be separated by  $\delta_{\text{initial}}$  from the left. Determine whether  $\delta_{\text{initial}}$  is within the matching tolerance,  $m$ . If so, consider the zero-crossing fragments matched with disparity  $\delta_{\text{initial}}$

$$m = w/2$$

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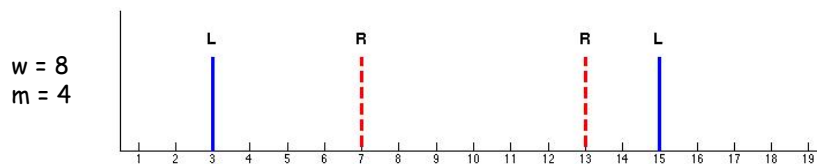
## Simplified MPG algorithm, Part 2

To determine final correspondence:

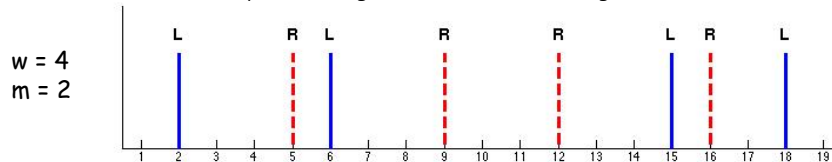
- (1) Find zero-crossings using a  $\nabla^2 G$  operator with reduced width  $w/2$
- (2) For each horizontal slice:
  - (2.1) For each zero-crossing in the left image:
    - (2.1.1) Determine the nearest zero-crossing fragment in the left image that matched when the  $\nabla^2 G$  operator width was  $w$
    - (2.1.2) Offset the zero-crossing fragment by a distance  $\delta_{\text{initial}}$ , the disparity of the nearest matching zero-crossing fragment found at the lower resolution with operator width  $w$
  - (2.2) Find the nearest neighbors in the right image for each zero-crossing fragment in the left image
  - (2.3) Find the nearest neighbors in the left image for each zero-crossing fragment in the right image
  - (2.4) For each pair of zero-crossing fragments that are closest neighbors of one another, let the right fragment be separated by  $\delta_{\text{new}}$  from the left. Determine whether  $\delta_{\text{new}}$  is within the reduced matching tolerance,  $m/2$ . If so, consider the zero-crossing fragments matched with disparity  $\delta_{\text{final}} = \delta_{\text{new}} + \delta_{\text{initial}}$

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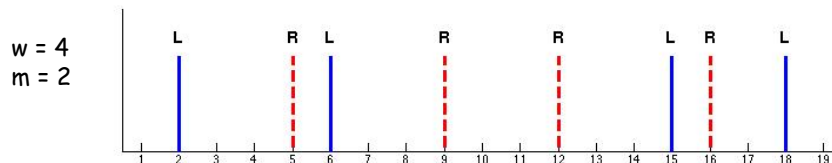
Coarse-scale zero-crossings:



Use coarse-scale disparities to guide fine-scale matching:



Ignore coarse-scale disparities:



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