

List Processing in SML

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Reading: Paulson's *ML for the Working Programmer*, Chap. 3

CS235 Languages and Automata

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Consing Elements into Lists

```
- val nums = 9 :: 4 :: 7 :: [];  
val nums = [9,4,7] : int list  
  
- 5 :: nums;  
val it =          : int list  
  
- nums;  
val it =          : int list (* nums is unchanged *)  
  
- (1+2) :: (3*4) :: (5-6) :: [];  
val it =          : int list  
  
- [1+2, 3*4, 5-6];  
val it = [3,12,~1] : int list  
  
- [1=2, 3 < 4, false];  
val it =          : bool list  
  
- ["I", "do", String.substring ("note",0,3), "li" ^ "ke"];  
val it =          : string list  
  
- [(#"a", 8), (#"z", 5)];  
val it = [(#"a",8),(#"z",5)] : (char * int) list  
  
- [[7,2,5], [6], 9::[3,4]];  
val it = [[7,2,5],[6],[9,3,4]] : int list list
```

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The Type of Cons

```
- 1 :: [2,3,4];  
val it = [1,2,3,4] : int list  
  
- op:: (1, [2,3,4]); (* op:: is prefix version of infix :: *)  
val it = [1,2,3,4] : int list  
  
-op:: ;  
val it = fn : 'a * 'a list -> 'a list  
  
- "a" :: [1,2,3];  
stdIn:1.1-8.3 Error: operator and operand don't agree [literal]  
operator domain: string * string list  
operand:         string * int list  
in expression:  
"a" :: 1 :: 2 :: 3 :: nil  
  
-[1,2] :: [3,4,5];  
stdIn:9.1-9.17 Error: operator and operand don't agree [literal]  
operator domain: int list * int list list  
operand:         int list * int list  
in expression:  
(1 :: 2 :: nil) :: 3 :: 4 :: 5 :: nil
```

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Creating Lists Recursively: range Example

```
(* range: int * int -> int list *)  
fun range (lo, hi) =
```

```
- range (0,3);  
val it = [0,1,2,3] : int list  
  
- range (5,7);  
val it = [5,6,7] : int list  
  
- range (7,7);  
val it = [7] : int list  
  
- range (7,5);  
val it = [] : int list
```

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Some Simple List Operations

```
- List.length [7,3,6,1];
val it = 4 : int

- List.hd [7,3,6,1];
val it = 7 : int

- List.tl [7,3,6,1];
val it = [3,6,1] : int list

- List.take ([7,3,6,1],2);
val it = [7,3] : int list

- List.take ([7,3,6,1],3);
val it = [7,3,6] : int list

- List.drop ([7,3,6,1],2);
val it = [6,1] : int list

- List.drop ([7,3,6,1],3);
val it = [1] : int list

- List.nth ([7,3,6,1],0);
val it = 7 : int

- List.nth ([7,3,6,1],1);
val it = 3 : int

- List.nth ([7,3,6,1],2);
val it = 6 : int

- List.null [7,3,6,1];
val it = false : bool

- List.null [];
val it = true : bool

- [7,3,6,1] = [];
val it = false : bool

- List.rev [7,3,6,1];
val it = [1,6,3,7] : int list
```

```
(* An API for all SMLNJ String operations can be found at:
http://www.standardml.org/Basis/list.html *)
```

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Appending Lists

```
- [7,2] @ [8,1,6];
val it = [7,2,8,1,6] : int list

- [7,2] @ [8,1,6] @ [9] @ [];
val it = [7,2,8,1,6,9] : int list

(* Appending is different than consing! *)
- [7,2] :: [8,1,6] :: [9] :: [];
val it = [[7,2],[8,1,6],[9]] : int list list

- op::; (* prefix cons function *)
val it = fn : 'a * 'a list -> 'a list

- op@; (* prefix append function *)
val it = fn : 'a list * 'a list -> 'a list

(* List.concat appends all elts in a list of lists *)
- List.concat [[7,2],[8,1,6],[9]];
val it = [7,2,8,1,6,9] : int list

- List.concat;
val it = fn : 'a list list -> 'a list
```

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Pattern Matching on Lists

```
(* matchtest : (int * int) list -> (int * int) list *)
fun matchtest xs =
  case xs of
    [] => []
  | [(a,b)] => [(b,a)]
  | (a,b) :: (c,d) :: zs => (a+c,b*d) :: (c,d) :: zs
```

```
- matchtest [];
val it = : (int * int) list

- matchtest [(1,2)];
val it = : (int * int) list

- matchtest [(1,2),(3,4)];
val it = : (int * int) list

- matchtest [(1,2),(3,4),(5,6)];
val it = : (int * int) list
```

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Other Pattern-Matching Notations

```
fun matchtest2 xs =
  case xs of
    [] => []
  | [(a,b)] => [(b,a)]
  | (a,b) :: (ys as ((c,d) :: zs)) => (a+c,b*d) :: ys
  (* subpatterns can be named with "as" *)
```

```
fun matchtest3 [] = []
  | matchtest3 [(a,b)] = [(b,a)]
  | matchtest3 ((a,b) :: (ys as ((c,d) :: zs)))
    = (a+c,b*d) :: ys
  (* parens around pattern necessary above *)
```

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List Accumulation

```
(* Recursively sum a list of integers *)
(* sumListRec : int list -> int *)
fun sumListRec [] =
  | sumListRec (x::xs) =
```

```
- sumListRec [];
val it = 0 : int

- sumListRec [5,2,4];
val it = 11 : int
```

```
(* Iterative (tail-recursive) summation *)
fun sumListIter xs =
  let fun loop [] sum =
        | loop (y::ys) sum =
      in loop xs 0
  end
```

```
- sumListIter [5,2,4];
val it = 11 : int
```

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Instance of the Mapping Idiom

```
(* incList : int list -> int list *)
fun incList [] =
  | incList (x::xs) =
```

```
- incList [5,2,4];
val it = [6,3,5] : int list
```

```
- incList [];
val it = [] : int list
```

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Abstracting Over the Mapping Idiom

```
(* map : ('a -> 'b) -> 'a list -> 'b list *)
fun map f [] = []
  | map f (x::xs) = (f x)::(map f xs)
```

```
- map (fn x => x + 1) [5,2,4];
val it =          : int list
```

```
- map (fn y => y * 2) [5,2,4];
val it =          : int list
```

```
- map (fn z => z > 3) [5,2,4];
val it =          : bool list
```

```
- map (fn a => (a, (a mod 2) = 0)) [5,2,4];
val it =          : (int * bool) list
```

```
- map (fn s => s ^ "side") ["in", "out", "under"];
val it =          : string list
```

```
- map (fn xs => 6::xs) [[7,2],[3],[8,4,5]];
val it =          : int list list
```

(* SML/NJ supplies map at top-level and as List.map *)

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Cartesian Products of Lists

```
(* 'a list -> 'b list -> ('a * 'b) list *)
fun listProd xs ys =
  List.concat (List.map
              xs)
```

```
- listProd ["a", "b"] [1,2,3];
val it = [("a",1), ("a",2), ("a",3), ("b",1), ("b",2), ("b",3)]
```

```
- listProd [1,2,3] ["a", "b"];
val it = [(1,"a"), (1,"b"), (2,"a"), (2,"b"), (3,"a"), (3,"b")]
```

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Zippping: A Different Kind of List Product

```
(* 'a list * 'b list -> ('a * 'b) list *)
- ListPair.zip (["a","b","c"], [1,2,3,4]);
val it = (["a",1], ("b",2), ("c",3)) : (string * int) list

(* ('a * 'b) list -> 'a list * 'b list *)
- ListPair.unzip (["a",1], ("b",2), ("c",3));
val it = (["a","b","c"], [1,2,3]) : string list * int list
```

(* An API for all SMLNJ String operations can be found at:
<http://www.standardml.org/Basis/list-pair.html> *)

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Powersets (well, bags really) of Lists

```
(* 'a list -> 'a list list *)
fun powerBag [] =
  | powerBag (x::xs) =
```

```
- powerBag [1];
val it = [[],[1]] : int list list
```

```
- powerBag [2,1];
val it = [[],[1],[2],[2,1]] : int list list
```

```
- powerBag [3,2,1];
val it = [[],[1],[2],[2,1],[3],[3,1],[3,2],[3,2,1]] : int list list
```

```
- powerBag [1,2,1];
val it = [[],[1],[2],[2,1],[1],[1,1],[1,2],[1,2,1]] : int list list
```

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Instance of the Filtering Idiom

```
fun filterPos [] =
  | filterPos (x::xs) =
```

```
- filterPos [3, ~7, ~6, 8, 5];
val it = [3,8,5] : int list
```

```
- filterPos [];
val it = [] : int list
```

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Abstracting over the Filtering Idiom

```
(* filter : ('a -> bool) -> 'a list -> 'a list *)
fun filter pred [] = []
  | filter pred (x::xs) =
    if (pred x) then
      x :: (filter pred xs)
    else
      (filter pred xs)
```

```
- filter (fn x => x > 0) [3, ~7, ~6, 8, 5];
val it =           : int list
```

```
- filter (fn y => (y mod 2) = 0) [5,2,4,1];
val it =           : int list
```

```
- filter (fn s => (String.size s) <= 3)
= ["I","do","not","like","green","eggs","and","ham"];
val it =           : string list
```

```
- filter (fn xs => (sumListRec xs > 10)) [[7,2],[3],[8,4,5]];
val it =           : int list list
```

(* SML/NJ supplies this function as List.filter *)

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Some Other Higher-Order List Ops

```
(* List.partition : ('a -> bool) -> 'a list -> 'a list * 'a list
  splits a list into two: those elements that satisfy the
  predicate, and those that don't *)
- List.partition (fn x => x > 0) [3, ~7, ~6, 8, 5];
val it = ([3,8,5],[~7,~6]) : int list * int list

- List.partition (fn y => (y mod 2) = 0) [5,2,4,1];
val it = ([2,4],[5,1]) : int list * int list

(* List.all : ('a -> bool) -> 'a list -> bool returns true iff
  the predicate is true for all elements in the list. *)
- List.all (fn x => x > 0) [5,2,4,1];
val it = true : bool

- List.all (fn y => (y mod 2) = 0) [5,2,4,1];
val it = false : bool

(* List.exists : ('a -> bool) -> 'a list -> bool returns true iff
  the predicate is true for at least one element in the list. *)
- List.exists (fn y => (y mod 2) = 0) [5,2,4,1];
val it = true : bool

- List.exists (fn z => z < 0) [5,2,4,1];
val it = false : bool
```

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Options and List.find

```
- fun into_100 n = if (n = 0) then NONE else SOME (100 div n);
val into_100 = fn : int -> int option

- List.map into_100 [5, 3, 0, 10];
val it = [SOME 20,SOME 33,NONE,SOME 10] : int option list

- fun addOptions (SOME x) (SOME y) = SOME (x + y)
  = | addOptions (SOME x) NONE = NONE
  = | addOptions NONE (SOME y) = NONE
  = | addOptions NONE NONE = NONE;
val addOptions = fn : int option -> int option -> int option

- addOptions (into_100 5) (into_100 10);
val it = SOME 30 : int option

- addOptions (into_100 5) (into_100 0);
val it = NONE : int option

(* List.find : ('a -> bool) -> 'a list -> 'a option *)
- List.find (fn y => (y mod 2) = 0) [5,2,4,1];
val it = SOME 2 : int option

- List.find (fn z => z < 0) [5,2,4,1];
val it = NONE : int option
```

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foldr : The Mother of All List Recursive Functions

```
- List.foldr;
val it = fn : ('a * 'b -> 'b) -> 'b -> 'a list -> 'b

- List.foldr (fn (x,y) => x + y) 0 [5,2,4];
val it =      : int

- List.foldr op+ 0 [5,2,4];
val it =      : int

- List.foldr (fn (x,y) => x * y) 1 [5,2,4];
val it =      : int

- List.foldr (fn (x,y) => x andalso y) true [true,false,true];
val it =      : bool

- List.foldr (fn (x,y) => x andalso y) true [true,true,true];
val it =      : bool

- List.foldr (fn (x,y) => x orelse y) false [true,false,true];
val it =      : bool

- List.foldr (fn (x,y) => (x > 0) andalso y) true [5,2,4];
val it =      : bool

- List.foldr (fn (x,y) => (x < 0) orelse y) false [5,2,4];
val it =      : bool
```

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Strings of Chars

```
- String.explode "foobar";
val it = [#"f",#"o",#"o",#"b",#"a",#"r"] : char list

- String.implode [#"1",#"0",#"0",#"1",#"1",#"0"];
val it = "100110" : string
```

Define the following functions:

```
all_1s: char list -> bool
```

Returns true iff the given list contains only 1s.

```
all_10s: char list -> bool
```

Returns true iff the given list consists of alternating 1s and 0s.

```
isInL: string -> bool
```

Returns true iff the string consists of all 1s or repeated 10s.

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