## Digital Logic (Part 2) + Integer Representation (Part 1)

1. For the following circuit:

a. Write the truth table:

| A | B | C | output |
| :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 0 |
| 1 | 1 | 1 | 1 |

b. Derive the boolean expression in sum-of-products form:

## $A B C+A^{\prime} B C+A B^{\prime} C$

c. Simplify your answer from part b using the boolean algebra laws, and write the corresponding law next to each step.

| $A B C+A^{\prime} B C+A B^{\prime} C$ | (original) |
| :--- | :--- |
| $\left(A+A^{\prime}\right) B C+A B^{\prime} C$ | Distributive |
| $B C+A B^{\prime} C$ | Inverse/Complements, Identity |
| $\left(B+A B^{\prime}\right) C$ | Distributive |
| $(B+A)\left(B+B^{\prime}\right) C$ | Distributive |
| $(B+A) C$ | Inverse/Complements, Identity |
| $(A+B) C$ | Commutative |

2. For the following circuit, derive the boolean expression and simplify it (with the laws you used written next to each step).


| $\left(\left(A^{\prime}+B^{\prime}\right)(B+C) A\right)^{\prime}$ |  |
| :--- | :--- |
| $\left(\left(A^{\prime}(B+C)+B^{\prime}(B+C)\right) A\right)^{\prime}$ | Distributive |
| $\left(A^{\prime}(B+C) A+B^{\prime}(B+C) A\right)^{\prime}$ | Distributive |
| $\left(A A^{\prime}(B+C)+B^{\prime}(B+C) A\right)^{\prime}$ | Commutative |
| $\left(B^{\prime}(B+C) A\right)^{\prime}$ | Inverse/Complements, Identity |
| $\left(B^{\prime} B A+B^{\prime} C A\right)^{\prime}$ | Distributive |
| $\left(B^{\prime} C A\right)^{\prime}$ | Inverse/Complements, Identity |
| $\left(A B^{\prime} C\right)^{\prime}$ | Commutative |

3. What's 156 (in base 10) in binary?

10011100
a. What is it it in hexadecimal?

0x9C
b. What is $\mathbf{1 5 6}_{\mathbf{1 0}} \mathbf{+ \mathbf { 0 0 1 1 1 0 1 1 } _ { \mathbf { 2 } } \text { in binary form? }}$
(i.e. Don't use the base 10 number or convert the binary number into base 10...)
$\mathbf{1 0 0 1 1 1 0 0}_{\mathbf{2}} \mathbf{+} \mathbf{0 0 1 1 1 0 1 1}_{\mathbf{2}}=\mathbf{1 1 0 1 0 1 1 1}_{2}$
4. What is $\mathbf{2 5 6}$ in hexadecimal?
$0 \times 100$
a. What is it in binary?
$0 \times 100000000$
5. What is $\mathbf{1 1 1 1}$ in hexadecimal?

0xF

