CS 240 Foundations of Computer Systems Representing Data with Bits	positional number representation $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
Representing Data with Dits	2 1 0 <i>position</i>
bits, bytes, numbers, and notation	Base determines: Maximum digit (base – 1). Minimum digit is 0. Weight of each position. Each position holds a digit.
	Represented value = sum of all position values Position value = digit value x base ^{position}
https://cs.wellesley.edu/~cs240/ Data as Bits 1	Data as Bits 2
binary = base 2	Powers of 2: memorize up to ≥ 2 ¹⁰ (in base ten)
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
When ambiguous, subscript with base: 101 ₁₀ Dalmatians (movie) 101 ₂ -Second Rule (folk wisdom for food safety)	
liony	

Show powers, strategies. conversion and ar	rithmetic ex	byte = 8 bits	What do you call 4 bits?
19 ₁₀ = ? ₂	1001 ₂ = ? ₁₀	Smallest unit of data used by a typical modern computer	$\frac{1}{1}$ $\frac{1}{1}$ $\frac{1}{1}$ $\frac{1}{1}$ $\frac{1}{1}$
240 ₁₀ = ? ₂	11010011 ₂ = ? ₁₀	Binary $00000000_2 - 11111111_2$ Decimal $000_{10} - 255_{10}$ Hexadecimal $00_{16} - FF_{16}$ Byte = 2 hex digits!	$\begin{array}{c ccccc} 2 & 2 & 0010 \\ \hline 3 & 3 & 0011 \\ \hline 4 & 4 & 0100 \\ \hline 5 & 5 & 0101 \\ \hline 6 & 6 & 0110 \\ \hline 7 & 7 & 0111 \\ \hline 8 & 8 & 1000 \end{array}$
$101_2 + 1011_2 = ?_2$	1001011 ₂ x 2 ₁₀ = ? ₂	Programmer's hex notation (C, etc.): $0 \times B4 = B4_{16}$ Octal (base 8) also useful.	9 9 1001 A 10 1010 B 11 1011 C 12 1100 D 13 1101 F 14 1110
	Data as Bits 6		F 15 1111 Data as Bits 8
Hex encoding prac	ctice	char: representing character A C-style string is represented by a series of byte – One-byte ASCII codes for each character. – ASCII = American Standard Code for Information In	es (chars). terchange
	Data as Bits 9	32 space 48 0 64 $@$ 80 P 96 33 ! 49 1 65 A 81 Q 97 34 " 50 2 66 B 82 R 98 35 # 51 3 67 C 83 S 99 36 $$5$ 52 4 68 D 84 T 100 37 % 53 5 69 E 85 U 101 38 $&$ 54 6 70 F 86 V 102 39 ' 55 7 71 G 87 W 103 40 (56 8 72 H 88 X 104 41) 57 9 73 I 89 Y 105 42 * 58 : 74 J 90 Z 106 43 + 59 ; 75 K 91 $[I$ 107 44 , 60 < 76 L 92 V 108 45 - 61 = 77 M 93 $]$ 109 46 . 62 > 78 N 94 A 110 47 / 63 ? 79 0 95 111	` 112 p a 113 q b 114 r c 115 s d 116 t e 117 u f 118 v g 119 w h 120 x I 121 y j 123 { I 124 m 125 } n 126 ~ o 127 del



bitwise operators in C

0x69 & 0x55 =

0x69 | 0x55 =

Many bit-twiddling puzzles in upcoming assignment

Data as Bits 15

ex

Encode playing cards.

52 cards in 4 suits

How do we encode suits, face cards?

What operations should be easy to implement?

Get and compare rank

Get and compare suit



Image: Structure of the st

Data as Bits 16

Two possible representations

52 cards – 52 bits with bit corresponding to card set to 1

52 bits in 2 x 32-bit words

"One-hot" encoding Hard to compare values and suits independently

Not space efficient

4 bits for suit, 13 bits for card value – 17 bits with two set to

Pair of one-hot encoded values

Easier to compare suits and values independently Smaller, but still not space efficient

Two better representations	Compare Card Suits mask: a bit vector that, when bitwise
Binary encoding of all 52 cards – only 6 bits needed	ANDed with another bit vector v, turns all but the bits of interest in v to 0 #define SUIT MASK 0x30
Number cards uniquely from 0Iow-order 6 bits of a byteSmaller than one-hot encodings.Hard to compare value and suit	<pre>int sameSuit(char card1, char card2) { return !((card1 & SUIT_MASK) ^ (card2 & SUIT_MASK)); //same as (card1 & SUIT_MASK) == (card2 & SUIT_MASK);</pre>
Binary encoding of suit (2 bits) and value (4 bits) separately	}
Number each value uniquely suit value Still small Easy suit, value comparisons Still small	<pre>char hand[5]; // represents a 5-card hand char card1, card2; // two cards to compare if (sameSuit(hand[0], hand[1])) { }</pre>
Data as Bits 19	Data as Bits 20
Data as Bits 19 Compare Card Values Image: a bit vector that, when bitwise Make: a bit vector that, when bitwise Image: a bit vector that, when bitwise Make: a bit vector that, when bitwise Image: a bit vector that, when bitwise Make: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bit vector that, when bitwise Image: a bitwise Image: a bitwise Image: a bitwise Image: a bitwise Image: a bitwise Image: a bitwise Image: a bitwise	Data as Bits 20 Bit shifting x x 10011001 x 10011001 x <<2 1001100100 lose bits on left fill with zeroes on right

Shift gotchas

Logical or arithmetic shift right: how do we tell?

C: compiler chooses Usually based on type: rain check!

Java: >> is arithmetic, >>> is logical

Shift an *n*-bit type by at least 0 and no more than n-1. C: other shift distances are undefined.

anything could happen

Java: shift distance is used modulo number of bits in shifted type

Given int x: x << 34 == x << 2

Data as Bits 23

Shift and mask: extract a bit field

Write a C function that extracts the 2nd most significant byte from its 32-bit integer argument.

Example behavior:

argument: 0b 01100001 01100010 01100011 01100100 expected result: 0b 0000000 0000000 0000000 01100010

All other bits are zero. Desired bits in least significant byte.

int get2ndMSB(int x) {

Data as Bits 24

ex