



CS 240

Foundations of Computer Systems



x86 Control Flow

(Part A, Part B)

Condition codes, comparisons, and tests

[Un]Conditional jumps and conditional moves

Translating if-else, loops, and switch statements

Conditionals and Control Flow

Two key pieces

1. Comparisons and tests: check conditions
2. Transfer control: choose next instruction

Familiar C constructs

- if else
- while
- do while
- for
- break
- continue

Processor Control-Flow State

Condition codes (a.k.a. *flags*)

1-bit registers hold flags set by last ALU operation

ZF	Zero Flag	result == 0
SF	Sign Flag	result < 0
CF	Carry Flag	carry-out/unsigned overflow
OF	Overflow Flag	two's complement overflow

%rip

Instruction pointer
(a.k.a. *program counter*)
register holds address of next instruction to execute

1. Compare and test: conditions

`cmpq b,a` computes $a - b$, sets flags, discards result

Which flags indicate that $a < b$? (signed? unsigned?)

`testq b,a` computes $a \& b$, sets flags, discards result

Common pattern:

`testq %rax, %rax`

What do ZF and SF indicate?

(Aside) Saving conditions as Boolean values

→ **setg**: set if greater

stores byte:

0x01 if $\sim(SF \wedge OF) \& \sim ZF$

0x00 otherwise

```
long gt(int x, int y) {  
    return x > y;  
}
```

```
gt:  
    cmpq %rsi,%rdi      # compare: x - y  
    setg %al             # al = x > y  
    movzbq %al,%rax     # zero rest of %rax  
    retq
```

Zero-extend from **Byte** (8 bits) to **Quadword** (64 bits)



set_ comes in same flavors
as j_ (next slide)

2. Jump: choose next instruction

Jump/branch to different part of code by setting `%rip`.

Unconditional
jump



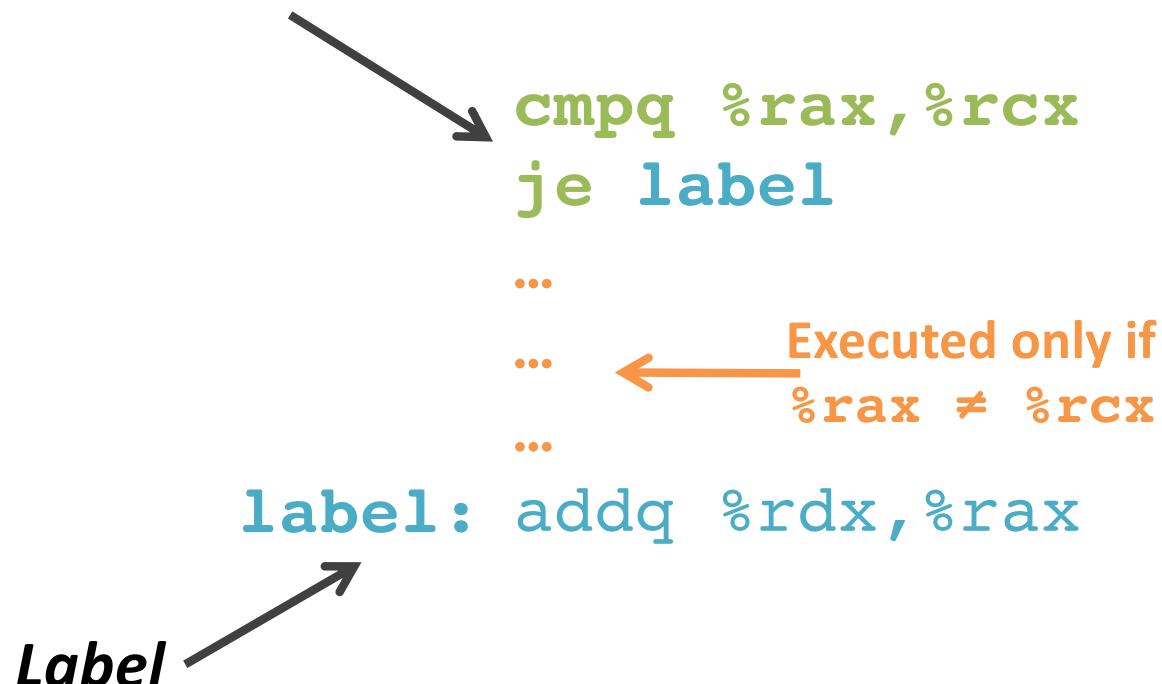
Conditional
jumps

<code>j__</code>	Condition	Description
<code>jmp</code>	1	Unconditional
<code>je</code>	<code>ZF</code>	Equal / Zero
<code>jne</code>	$\sim ZF$	Not Equal / Not Zero
<code>js</code>	<code>SF</code>	Negative
<code>jns</code>	$\sim SF$	Nonnegative
<code>jg</code>	$\sim (SF \wedge OF) \& \sim ZF$	Greater (Signed)
<code>jge</code>	$\sim (SF \wedge OF)$	Greater or Equal (Signed)
<code>jl</code>	$(SF \wedge OF)$	Less (Signed)
<code>jle</code>	$(SF \wedge OF) \mid ZF$	Less or Equal (Signed)
<code>ja</code>	$\sim CF \& \sim ZF$	Above (unsigned)
<code>jb</code>	<code>CF</code>	Below (unsigned)

Jump for control flow

Jump immediately follows comparison/test.

Together, they make a decision:
"if `%rcx == %rax` then jump to label."



Label
Name for address of
following item.

Conditional branch example

```
long absdiff(long x, long y) {  
    long result;  
    if (x > y) {  
        result = x-y;  
    } else {  
        result = y-x;  
    }  
    return result;  
}
```

Labels →
Name for address of
following item.

absdiff:

```
    cmpq    %rsi, %rdi  
    jle     .L7  
    subq    %rsi, %rdi  
    movq    %rdi, %rax
```

.L8:

```
    retq
```

.L7:

```
    subq    %rdi, %rsi  
    movq    %rsi, %rax  
    jmp     .L8
```

How did the compiler create this?

Control-Flow Graph

Code flowchart/directed graph.

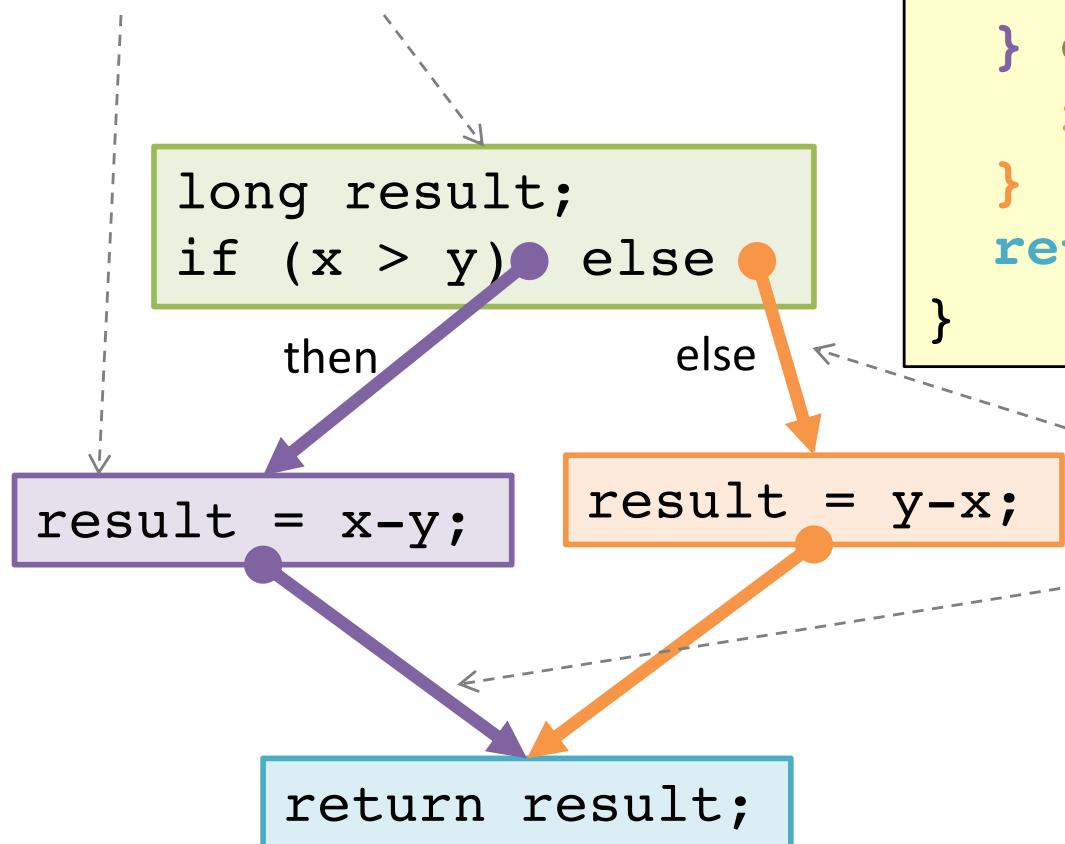
Introduced by Fran Allen, et al.

Won the 2006 Turing Award
for her work on compilers.



Nodes = **Basic Blocks**:

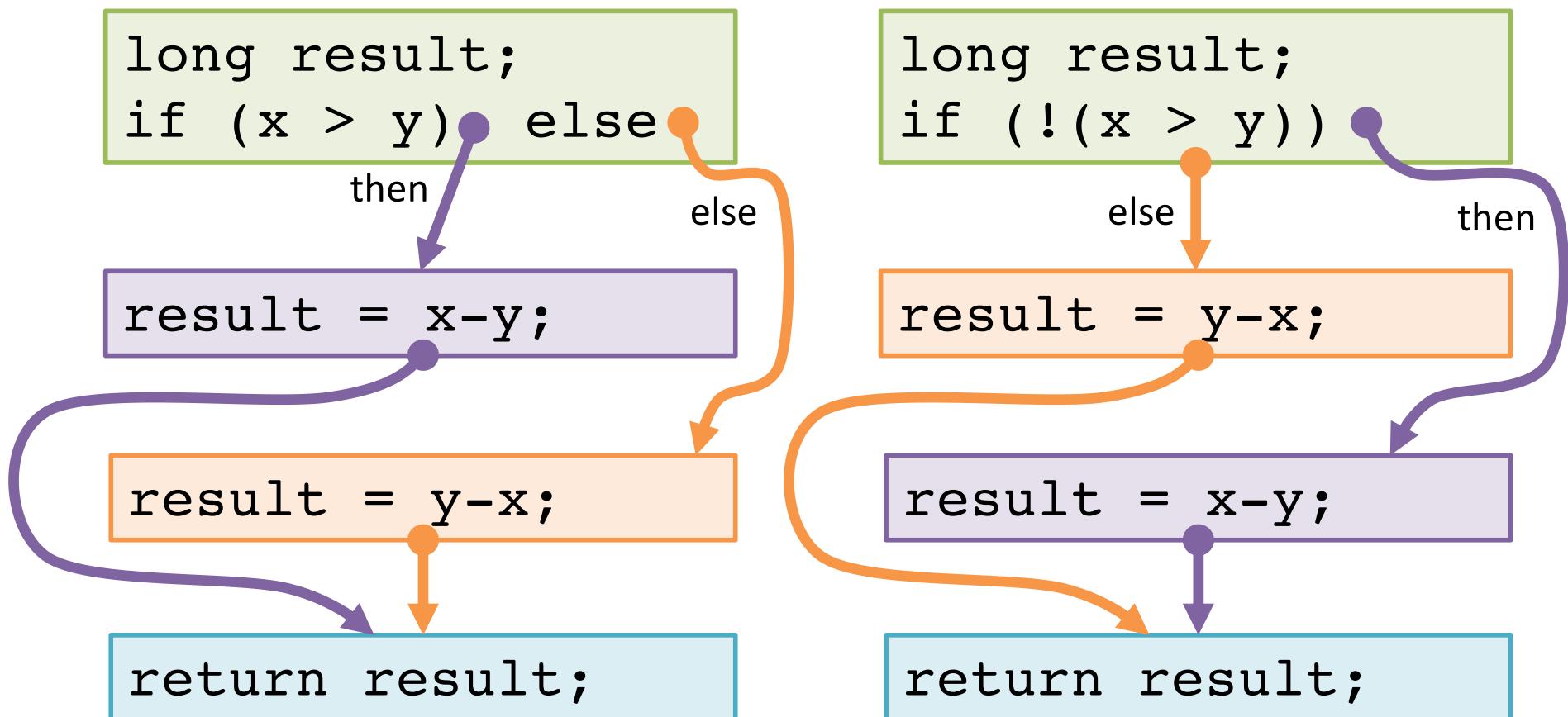
Straight-line code always
executed together in order.



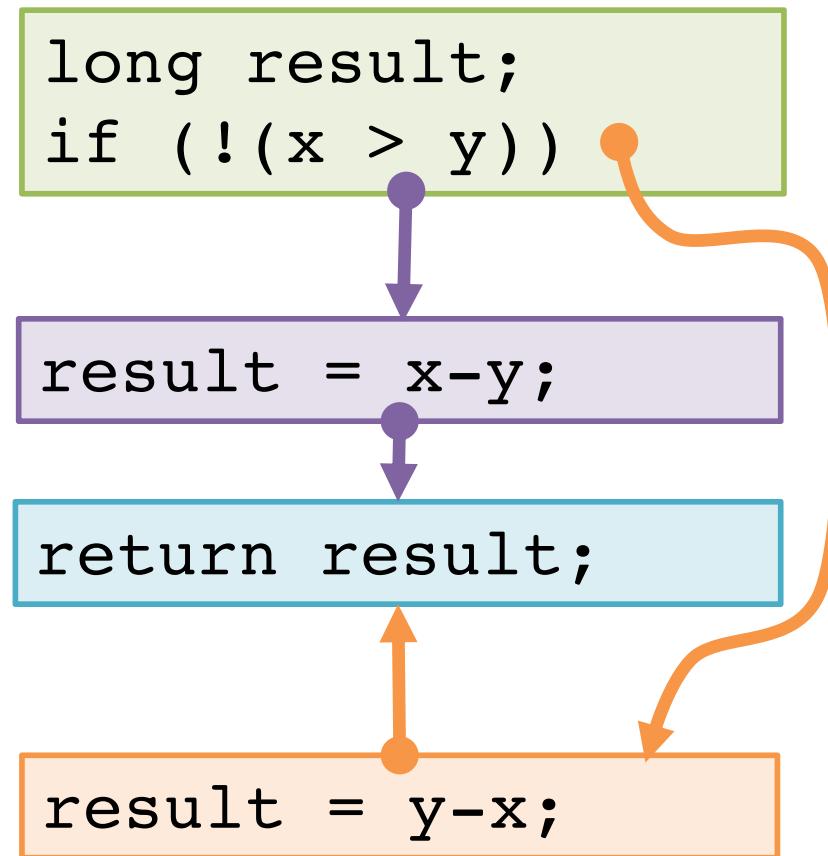
```
long absdiff(long x, long y){  
    long result;  
    if (x > y) {  
        result = x-y;  
    } else {  
        result = y-x;  
    }  
    return result;  
}
```

Edges = **Control Flow**:
Which basic block executes
next (under what condition).

Choose a linear order of basic blocks.

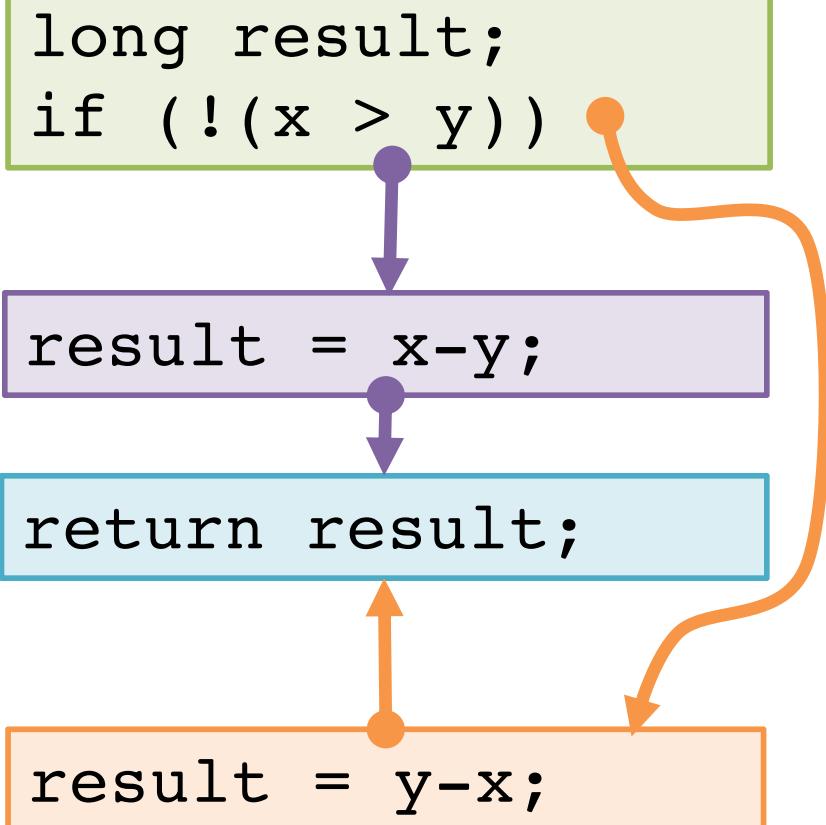


Choose a linear order of basic blocks.



Why might the compiler choose this basic block order instead of another valid order?

Translate basic blocks with jumps + labels



```
cmpq    %rsi, %rdi  
jle     Else
```

```
subq    %rsi, %rdi  
movq    %rdi, %rax
```

End:

```
retq
```

Else:

```
subq    %rdi, %rsi  
movq    %rsi, %rax  
jmp    End
```

Why might the compiler choose this basic block order instead of another valid order?

Execute absdiff

```
cmpq    %rsi, %rdi  
jle     Else
```

```
subq    %rsi, %rdi  
movq    %rdi, %rax
```

End:

```
retq
```

Else:

```
subq    %rdi, %rsi  
movq    %rsi, %rax  
jmp End
```

Registers

%rax	
%rdi	5
%rsi	3

Execute absdiff

```
cmpq    %rsi, %rdi  
jle     Else
```

```
subq    %rsi, %rdi  
movq    %rdi, %rax
```

End:

```
retq
```

Else:

```
subq    %rdi, %rsi  
movq    %rsi, %rax  
jmp End
```

Registers

%rax	
%rdi	4
%rsi	7

Note: CSAPP shows translation with goto

```
long absdiff(long x,long y){  
    int result;  
    if (x > y) {  
        result = x-y;  
    } else {  
        result = y-x;  
    }  
    return result;  
}
```

```
long goto_ad(long x,long y){  
    int result;  
    if (x <= y) goto Else;  
    result = x-y;  
End:  
    return result;  
Else:  
    result = y-x;  
    goto End;  
}
```

Note: CSAPP shows translation with goto

```
long goto_ad(long x, long y){  
    long result;  
    if (x <= y) goto Else;  
    result = x-y;  
End:  
    return result;  
Else:  
    result = y-x;  
    goto End;  
}
```

absdiff:

```
cmpq    %rsi, %rdi  
jle     Else
```

```
subq    %rsi, %rdi  
movq    %rdi, %rax
```

End:

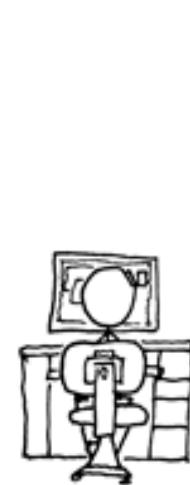
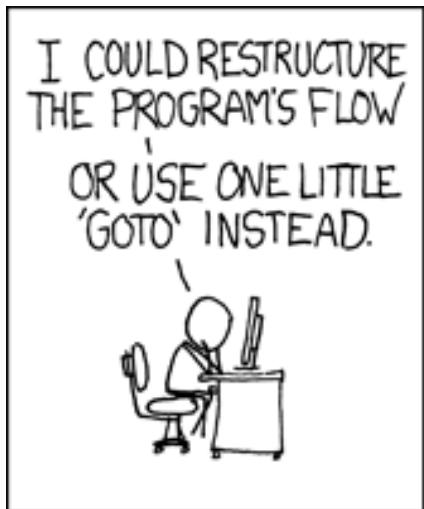
```
retq
```

Else:

```
subq    %rdi, %rsi  
movq    %rsi, %rax  
jmp    End
```

Close to assembly code.

But never use goto in your source code!



<http://xkcd.com/292/>

Compile if-else

ex

```
long wacky(long x, long y){  
    long result;  
    if (x + y > 7) {  
        result = x;  
    } else {  
        result = y + 2;  
    }  
    return result;  
}
```

wacky:

Assume x is available in %rdi,
y is available in %rsi.

Place result in %rax for return.

Compile if-else (solution #1)

ex

```
long wacky(long x, long y){  
    long result;  
    if (x + y > 7) {  
        result = x;  
    } else {  
        result = y + 2;  
    }  
    return result;  
}
```

Assume x is available in %rdi,
y is available in %rsi.

Place result in %rax for return.

wacky:

```
    movq %rdi, %rdx  
    addq %rsi, %rdx  
    cmpq $7, %rdx  
    jle Else
```

```
    movq %rdi, %rax
```

End:

```
    retq
```

Else:

```
    addq $2, %rsi  
    movq %rsi, %rax  
    jmp End
```

Compile if-else (solution #2)

ex

```
long wacky(long x, long y){  
    long result;  
    if (x + y > 7) {  
        result = x;  
    } else {  
        result = y + 2;  
    }  
    return result;  
}
```

Assume x is available in %rdi,
y is available in %rsi.

Place result in %rax for return.

wacky:

```
    leaq (%rdi, %rsi), %rdx  
    cmpq $7, %rdx  
    jle Else
```

```
    movq %rdi, %rax
```

End:

```
    retq
```

Else:

```
    leaq 2(%rsi), %rax  
    jmp End
```

Encoding jumps: PC-relative addressing

0x100	cmpq %rax, %rbx	0x1000
0x102	je 0x70	0x1002
0x104	...	0x1004
...
0x174	addq %rax, %rbx	0x1074

PC-relative *offsets* support relocatable code.
Absolute branches do not (or it's hard).



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x86 Control Flow

(Part A, Part B)

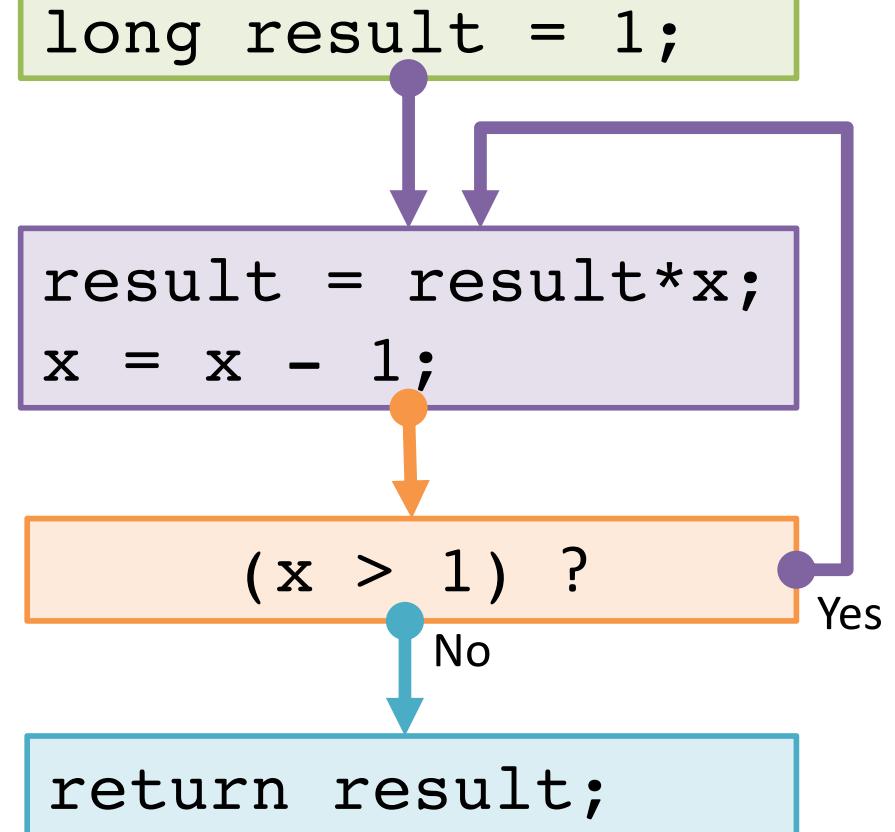
Condition codes, comparisons, and tests

[Un]Conditional jumps and **conditional moves**

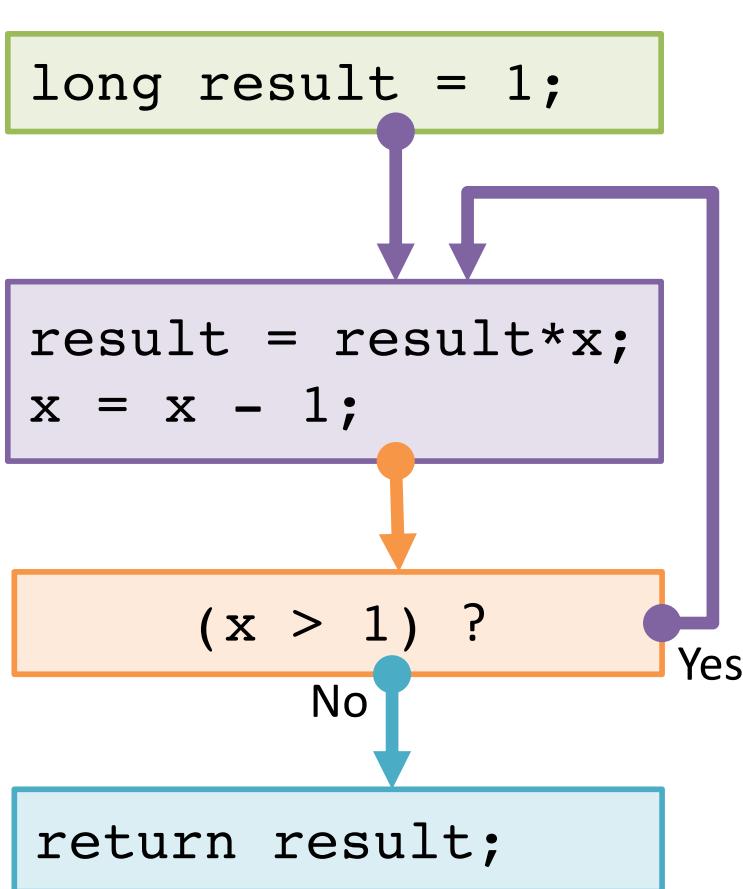
Translating if-else, loops, and switch statements

do while loop

```
long fact_do(long x) {  
    long result = 1;  
    do {  
        result = result * x;  
        x = x - 1;  
    } while (x > 1);  
    return result;  
}
```



do while loop



fact_do:

movq \$1,%rax

.L11:

imulq %rdi,%rax
decq %rdi

cmpq \$1,%rdi
jg .L11

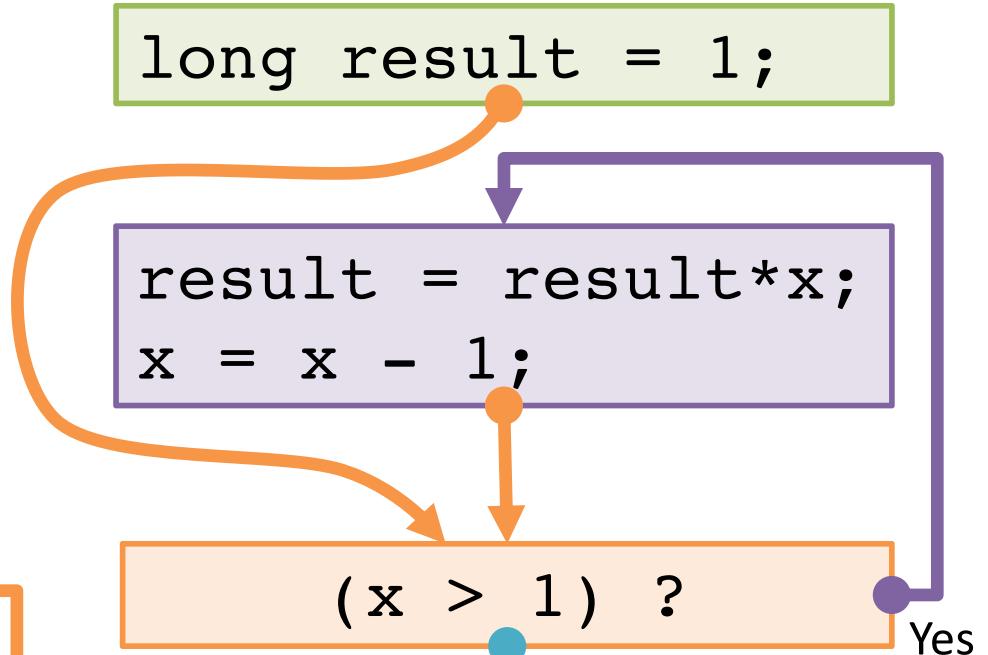
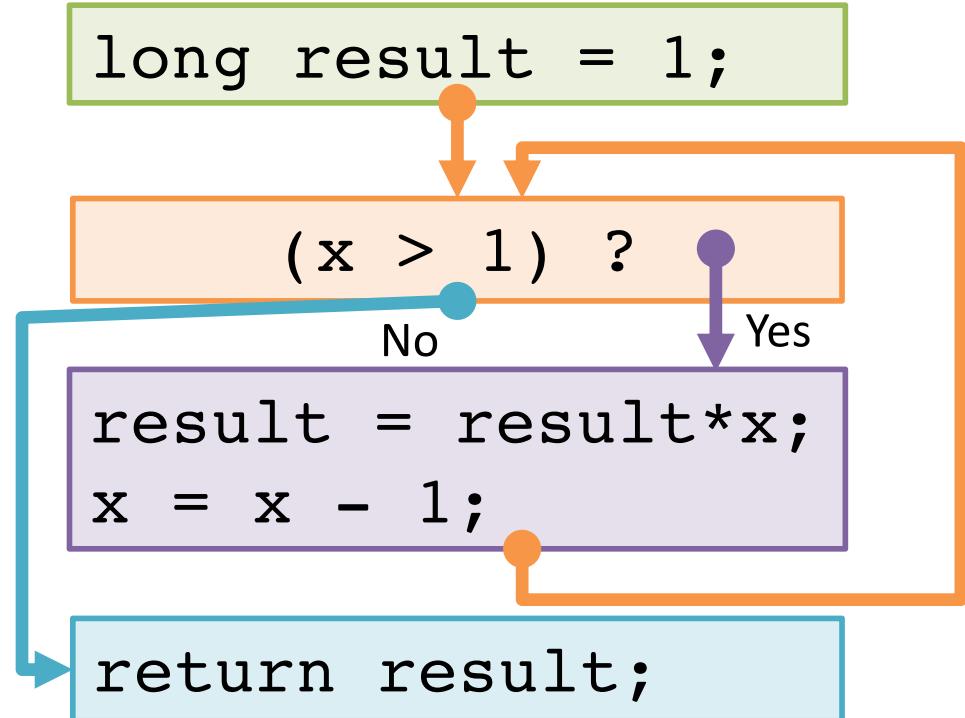
retq

Register	Variable
%rdi	
%rax	

Why put the loop condition at the end?

while loop

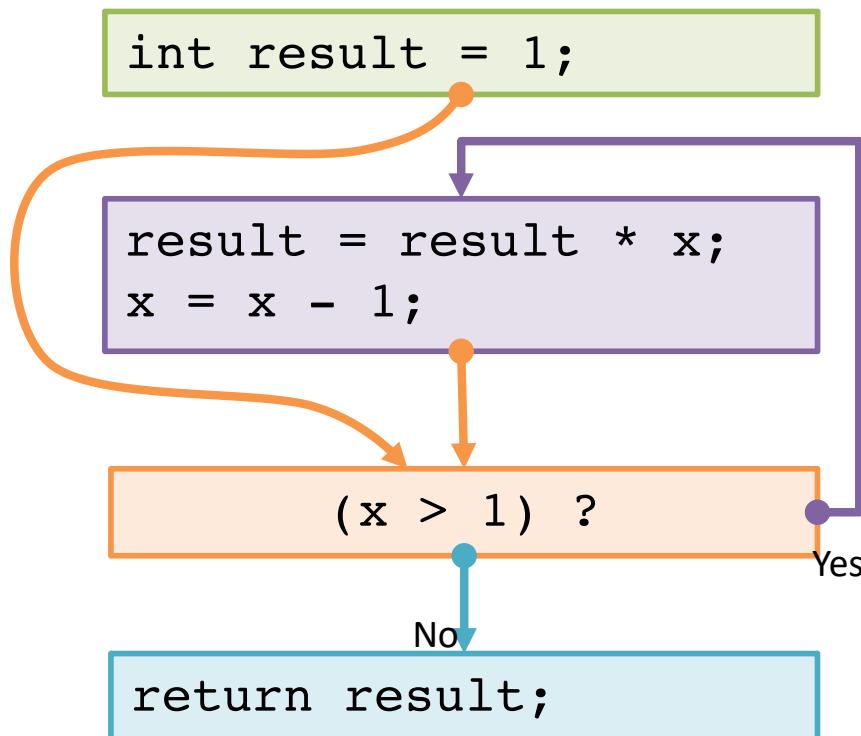
```
long fact_while(long x){  
    long result = 1;  
    while (x > 1) {  
        result = result * x;  
        x = x - 1;  
    }  
    return result;  
}
```



This order is used by GCC for x86-64. Why?

while loop

```
long fact_while(long x){  
    long result = 1;  
    while (x > 1) {  
        result = result * x;  
        x = x - 1;  
    }  
    return result;  
}
```



`fact_while:`

```
    movq $1, %rax  
    jmp .L34
```

`.L35:`

```
    imulq %rdi, %rax  
    decq %rdi
```

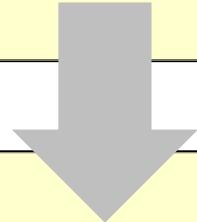
`.L34:`

```
    cmpq $1, %rdi  
    jg .L35
```

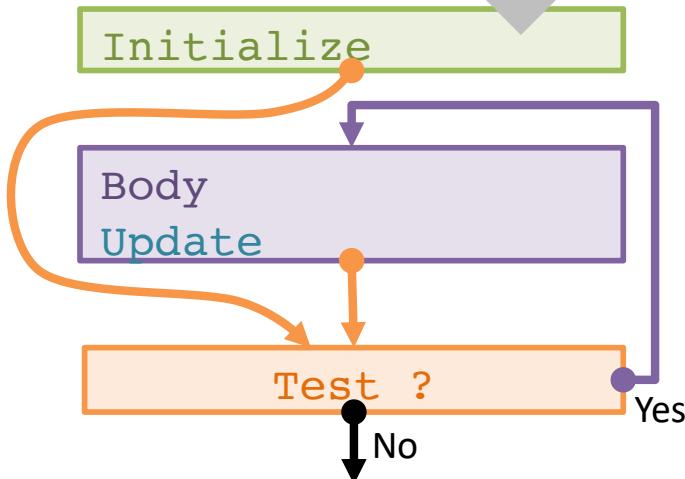
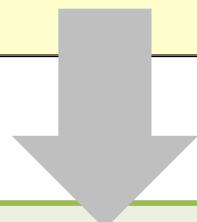
`retq`

for loop translation

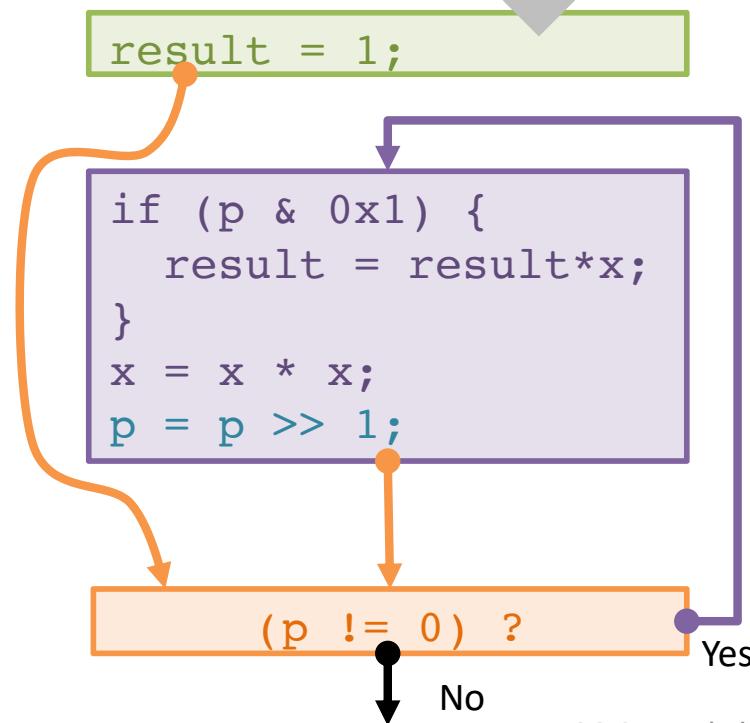
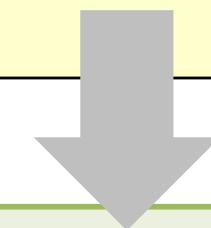
```
for (Initialize; Test; Update) {
    Body
}
```



```
Initialize;
while (Test) {
    Body;
    Update;
}
```



```
for (result = 1; p != 0; p = p>>1) {
    if (p & 0x1) {
        result = result * x;
    }
    x = x * x;
}
```



optional

for loop: square-and-multiply

```
/* Compute x raised to nonnegative power p */
int power(int x, unsigned int p) {
    int result;
    for (result = 1; p != 0; p = p>>1) {
        if (p & 0x1) {
            result = result * x;
        }
        x = x*x;
    }
    return result;
}
```

$$x^m * x^n = \mathbf{x^{m+n}}$$

$$\underset{0}{1} \underset{\dots}{2^{31}} \underset{0}{\dots} \underset{1}{2^{16}} \underset{0}{\dots} \underset{1}{2^8} \underset{0}{\dots} \underset{1}{2^4} \underset{0}{\dots} \underset{1}{2^2} \underset{0}{\dots} \underset{1}{2^1} = 11$$

$$\underset{1 = x^0}{1} \underset{x = x^1}{2^{31}} * \dots * \underset{1 = x^0}{2^{16}} * \underset{x = x^1}{2^8} * \underset{1 = x^0}{2^4} * \underset{x = x^1}{2^2} * \underset{1 = x^0}{2^1} = x^{11}$$

Algorithm

Exploit bit representation: $p = p_0 + 2p_1 + 2^2p_2 + \dots + 2^{n-1}p_{n-1}$

Gives: $x^p = z_0 \cdot z_1^2 \cdot (z_2^2)^2 \cdot \dots \cdot (\underbrace{\dots ((z_{n-1}^2)^2)}_{n-1 \text{ times}} \dots)^2$

$z_i = 1$ when $p_i = 0$

$z_i = x$ when $p_i = 1$

Complexity $O(\log p) = O(\text{sizeof}(p))$

Example

$$\begin{aligned} 3^{11} &= 3^1 * 3^2 * 3^8 \\ &= 3^1 * 3^2 * ((3^2)^2)^2 \end{aligned}$$

optional

for loop: power iterations

```
/* Compute x raised to nonnegative power p */
int power(int x, unsigned int p) {
    int result;
    for (result = 1; p != 0; p = p>>1) {
        if (p & 0x1) {
            result = result * x;
        }
        x = x*x;
    }
    return result;
}
```

iterations	result	x	p
0	1	3	$11 = 1011_2$
1	3	9	$5 = 101_2$
2	27	81	$2 = 10_2$
3	27	6561	$1 = 1_2$
4	177147	43046721	0_2

(Aside) Conditional Move

Why? Branch prediction in pipelined/OoO processors.

`cmove_ src, dest`
if (*Test*) *Dest* \leftarrow *Src*

```
long absdiff(long x, long y) {  
    return x>y ? x-y : y-x;  
}
```

```
long absdiff(long x, long y) {  
    long result;  
    if (x > y) {  
        result = x - y;  
    } else {  
        result = y - x;  
    }  
    return result;  
}
```

`absdiff:`

```
    movq    %rdi, %rax  
    subq    %rsi, %rax  
    movq    %rsi, %rdx  
    subq    %rdi, %rdx  
    cmpq    %rsi, %rdi  
    cmovle %rdx, %rax  
    ret
```

(Aside) Bad uses of conditional move

Expensive Computations

```
val = Test(x) ? Hard1(x) : Hard2(x);
```

Risky Computations

```
val = p ? *p : 0;
```

Computations with side effects

```
val = x > 0 ? x*=7 : x+=3;
```

switch statement

```
long switch_eg (long x, long y, long z) {  
    long w = 1;  
    switch(x) {  
        case 1:  
            w = y * z;  
            break;  
        case 2:  
            w = y - z; // fall-through  
        case 3:  
            w += z;  
            break;  
        case 5:  
        case 6:  
            w -= z;  
            break;  
        default:  
            w = 2;  
    }  
    return w;  
}
```

Fall through cases

Multiple case labels

Missing cases use default

Lots to manage:
use a *jump table*.

switch jump table structure

C code:

```
switch(x) {  
    case 1: <some code>  
        break;  
    case 2: <some code>  
    case 3: <some code>  
        break;  
    case 5:  
    case 6: <some code>  
        break;  
    default: <some code>  
}
```

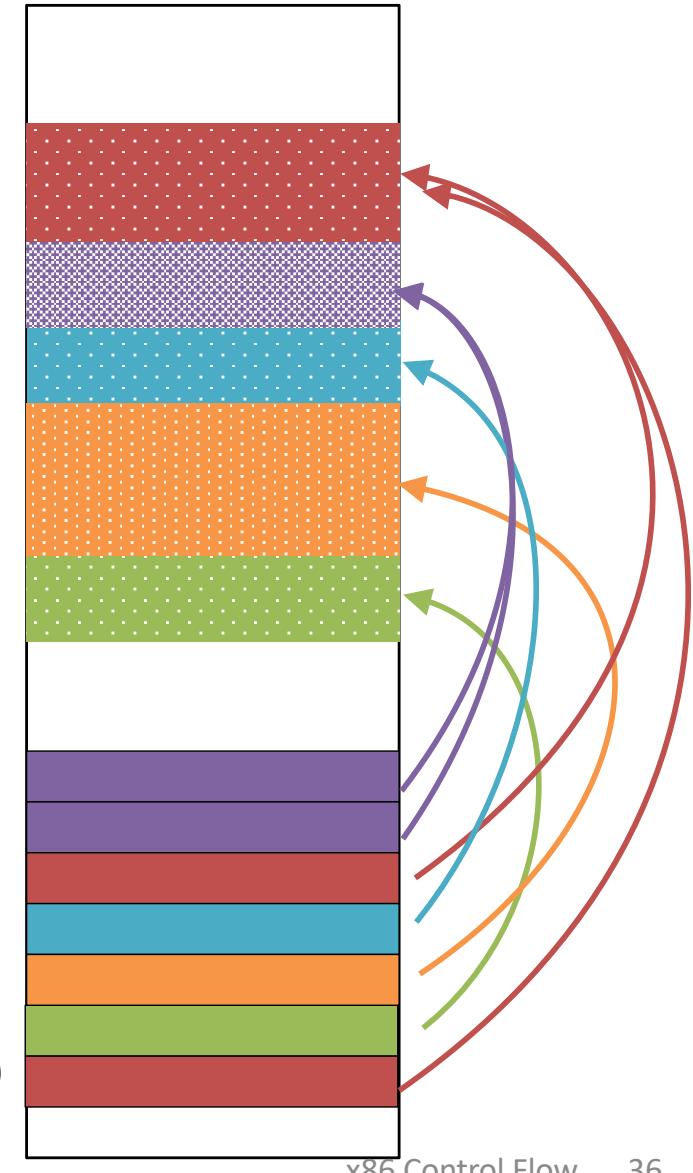
Code
Blocks

Jump
Table

Translation sketch:

```
if (0 <= x && x <= 6)  
    addr = jumptable[x];  
    goto addr;  
else  
    goto default;
```

Memory



switch jump table assembly declaration

read-only data

(not instructions)

```
.section .rodata      8-byte alignment
.align 8
.L4:
.quad .L8 # x == 0
.quad .L3 # x == 1
.quad .L5 # x == 2
.quad .L9 # x == 3
.quad .L8 # x == 4
.quad .L7 # x == 5
.quad .L7 # x == 6
```

“quad” = q suffix = 8-byte value

```
switch(x) {
    case 1:          // .L3
        w = y * z;
        break;
    case 2:          // .L5
        w = y - z;
    case 3:          // .L9
        w += z;
        break;
    case 5:
    case 6:          // .L7
        w -= z;
        break;
    default:         // .L8
        w = 2;
}
```

switch case dispatch

```
long switch_eg(long x, long y, long z) {  
    long w = 1;  
    switch(x) {  
        . . .  
    }  
    return w;  
}
```

Jump if above (unsigned, but...)

```
switch_eg:  
    movl $1, %eax  
    cmpq $6, %rdi  
    ja .L8  
    jmp * .L4(, %rdi, 8)
```

indirect jump

Jump table

```
.section .rodata  
.align 8  
.L4:  
.quad .L8 # x == 0  
.quad .L3 # x == 1  
.quad .L5 # x == 2  
.quad .L9 # x == 3  
.quad .L8 # x == 4  
.quad .L7 # x == 5  
.quad .L7 # x == 6
```

Reg.	Use
%rdi	x
%rsi	y
%rdx	z
%rax	w

switch cases

```

switch(x) {
    case 1:      // .L3
        w = y * z;
        break;
    case 2:      // .L5
        w = y - z;
    case 3:      // .L9
        w += z;
        break;
    case 5:      // .L7
    case 6:      // .L7
        w == z;
        break;
    default:     // .L8
        w = 2;
}
return w;

```

.L3:	movq %rsi, %rax	
	imulq %rdx, %rax	
retq	"inlined"	
.L5:	movq %rsi, %rax	
	subq %rdx, %rax	
.L9:	addq %rdx, %rax	
	retq	
.L7:	subq %rdx, %rax	
	retq	
.L8:	movl \$2, %eax	
	retq	

Aside: `movl` is used because 2 is a small positive value that fits in 32 bits. High order bits of `%rax` get set to zero automatically. It takes *fewer bytes* to encode a literal `movl` vs a `movq`.

switch machine code

Assembly Code

```
switch_eg:  
    . . .  
    cmpq    $6, %rdi  
    ja     .L8  
    jmp    * .L4( ,%rdi,8)
```

Disassembled Object Code

```
00000000004004f6 <switch_eg>:  
    . . .  
4004fd: 77 2b          ja 40052a <switch_eg+0x34>  
4004ff: ff 24 fd d0 05 40 00  jmpq *0x4005d0(,%rdi,8)
```

Inspect jump table contents using GDB.

Examine contents as 7 addresses

	<i>Address of code for case 0</i>	<i>Address of code for case 1</i>
(gdb) x/7a 0x4005d0		
0x4005d0: 0x40052a <switch_eg+52>	←	0x400506 <switch_eg+16>
0x4005e0: 0x40050e <switch_eg+24>		0x400518 <switch_eg+34>
0x4005f0: 0x40052a <switch_eg+52>		0x400521 <switch_eg+43>
0x400600: 0x400521 <switch_eg+43>	←	← <i>Address of code for case 6</i>

Would you implement this with a jump table?

```
switch(x) {  
    case 0:      <some code>  
                 break;  
    case 10:     <some code>  
                 break;  
    case 52000:  <some code>  
                 break;  
    default:    <some code>  
                 break;  
}
```



x86 Control Flow

(Part A, Part B)

Condition codes, comparisons, and tests

[Un]Conditional jumps and conditional moves

Translating if-else, loops, and switch statements