## CS240 Lab 3: Combinational and Arithmetic Logic

## Pre-lab Assignment



## Question 1

Assume you have 3 inputs, $\mathbf{S}, \mathbf{A 1}$ and $\mathbf{A 0}$, and an output $\mathbf{Q}$.
When $\mathbf{S}=0, \mathbf{Q}=\mathbf{A} \mathbf{0}$
When $\mathbf{S}=1, \mathbf{Q}=\mathbf{A} 1$
Give the truth table for $\mathbf{Q}$ :

| $\mathbf{S}$ | $\mathbf{A 1}$ | $\mathbf{A 0}$ | $\mathbf{Q}$ |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 0 |  |
| 0 | 0 | 1 |  |
| 0 | 1 | 0 |  |
| 0 | 1 | 1 |  |
| 1 | 0 | 0 |  |
| 1 | 0 | 1 |  |
| 1 | 1 | 0 |  |
| 1 | 1 | 1 |  |

Write the unsimplified sum-of-products boolean algebra expression for $\mathbf{Q}$ :

$$
\mathbf{Q}=
$$

$\qquad$
Write a simplified version of the expression above using only 4 operations (one of which is NOT):
Q =

Draw a circuit that produces $\mathbf{Q}$ :

S stands for "select." Knowing this, describe in English what this circuit does:
$\square$

## Question 2

Assume you have 2 inputs, A1 and A0, and 4 outputs/functions, Q0, Q1, Q2, and Q3

- Q0 is only true when A1A0 = 00
- Q1 is only true when A1A0 $=01$
- Q2 is only true when A1A0 = 10
- Q3 is only true when A1A0 = 11

Give the truth table:

| A1 | A0 | Q3 | Q2 | Q1 | Q0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 |  |  |  |  |
| 0 | 1 |  |  |  |  |
| 1 | 0 |  |  |  |  |
| 1 | 1 |  |  |  |  |
| 0 | 0 |  |  |  |  |
| 0 | 1 |  |  |  |  |
| 1 | 0 |  |  |  |  |
| 1 | 1 |  |  |  |  |

Write a boolean algebra expression for each of Q0, Q1, Q2, and Q3:
$\square$



Draw a circuit that produces each of the functions from a single set of inputs A1 and A0:

Each input combination of $\mathbf{A 1}$ and $\mathbf{A 0}$ represents a 2-bit binary number. How is this related to the outputs?
$\square$

## Question 3

Complete the truth table for two functions, Sum and CarryOut, which represent the result when adding two individual bits $\mathbf{A}$ and $\mathbf{B}$ :

| A | B | Sum | Carry <br> Out |
| :---: | :---: | :---: | :---: |
| 0 | 0 |  |  |
| 0 | 1 |  |  |
| 1 | 0 |  |  |
| 1 | 1 |  |  |

Draw a circuit which produces Sum and CarryOut from inputs $\mathbf{A}$ and $\mathbf{B}$ (this circuit is known as a half adder). You should use exactly one AND gate and one XOR (exclusive or) gate.
$\square$

Give the truth table for a full adder (which incorporates a carry-in bit to the sum of $\mathbf{A}$ and B):

| A | B | Carry <br> In | Sum | Carry <br> Out |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 |  |  |
| 0 | 0 | 1 |  |  |
| 0 | 1 | 0 |  |  |
| 0 | 1 | 1 |  |  |
| 1 | 0 | 0 |  |  |
| 1 | 0 | 1 |  |  |
| 1 | 1 | 0 |  |  |
| 1 | 1 | 1 |  |  |

## Question 4

A circuit for the full adder is:


Circle the two half adders on the diagram above.

Explain what each half adder is doing, in relation to adding the three bits A, B, and Carryln:

## Explain what the OR gate is doing to produce the CarryOut:

$\square$

