## Computer Science 240

Assignment for Lab 6

1. Write a Boolean function for F :

ABC F
$000 \quad 1$
$001 \quad 0$
010 1
$011 \quad 1$
$100 \quad 0$
$101 \quad 1$
$110 \quad 1$
1110
$\mathrm{F}=\mathrm{A}^{\prime} \mathrm{B}^{\prime} \mathrm{C}^{\prime}+\mathrm{A}^{\prime} \mathrm{BC}^{\prime}+\mathrm{A}^{\prime} \mathrm{BC}+\mathrm{AB}^{\prime} \mathrm{C}+\mathrm{ABC}^{\prime}$
2. Draw a transistor circuit (use transistors, not loge gate symbols) to implement $\mathrm{F}=\mathrm{A}^{\prime} \mathrm{B}+\mathrm{C}$

2. Draw a circuit which implements the following function $G$, using logic gates for AND, OR, and NOT .

Do not simplify G before drawing the circuit.
You may use 1, 2, or 3-input gates of type AND, OR, and NOT.

$$
\mathrm{G}=\mathrm{A}\left(\mathrm{BC}+\mathrm{B}^{\prime}+\mathrm{C}^{\prime}\right)+\mathrm{B}\left(\mathrm{AB}+\mathrm{A}^{\prime} \mathrm{B}\right)
$$


3. Give the truth table for G. In the truth table, include the outputs of each of the gates in your circuit. For example:

| A | B | C | BC | $\left(\mathrm{BC}+\mathrm{B}^{\prime}+\mathrm{C}^{\prime}\right)$ | $\mathrm{A}\left(\mathrm{BC}+\mathrm{B}^{\prime}+\mathrm{C}^{\prime}\right)$ | AB | $\mathrm{A}^{\prime} \mathrm{B}$ | $\mathrm{B}\left(\mathrm{AB}+\mathrm{A}^{\prime} \mathrm{B}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 0 | 1 | 0 | 0 | 1 | 1 |
| 0 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | 1 |
| 1 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 |
| 1 |  |  |  |  |  |  |  |  |
| 1 | 0 | 1 | $\left.\mathrm{C}^{\prime}\right)+\mathrm{B}\left(\mathrm{AB}+\mathrm{A}^{\prime} \mathrm{B}\right)$ |  |  |  |  |  |
| 1 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 0 |
| 1 | 1 | 0 | 0 | 1 | 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 |

4. Use the identities of Boolean algebra to show that $G$ is equivalent to $F=A+B$. Show all your work, and list the identity used for each step.

| $\mathrm{G}=$ | $\mathrm{A}\left(\mathrm{BC}+\mathrm{B}^{\prime}+\mathrm{C}^{\prime}\right)+\mathrm{B}\left(\mathrm{AB}+\mathrm{A}^{\prime} \mathrm{B}\right)$ |  |
| :--- | :--- | :--- |
|  | $\mathrm{F}=\mathrm{A}+\mathrm{B}$ |  |
|  | $\mathrm{A}\left(\mathrm{BC}+(\mathrm{BC})^{\prime}\right)$ |  |
| $\mathrm{A}(1)$ |  | DeMorgan's |
| A | Inverse |  |
| A |  | Identity |
| A | $+\mathrm{B}\left(\left(\mathrm{A}+\mathrm{A}^{\prime}\right) \mathrm{B}\right)$ |  |
| Distributive |  |  |
| A | $+\mathrm{B}((1) \mathrm{B}))$ | Inverse |
| A | +BB | Identity |

