CS240 Laboratory 2 Digital Logic

- Circuit equivalence
- Boolean Algebra/Universal gates
- Linux, C, Emacs
- Bitbucket, Mercurial

Circuit Equivalence

Two boolean functions with same truth table = **equivalent**

When there is an equivalent circuit that uses fewer gates, transistors, or chips, it is preferable to use that circuit in the design

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A	В	A'B'	A'B	F	AE	3 A'	A'B	A' B'	Q
0	0	1	0	1	0 0) 1	0	1	1
0	1	0	1	1	0 1	. 1	0	0	1
1	0	0	0	0	1 0) ()	0	0	0
1	1	0	0	0	1 1	0	0	0	0
T	T	U	U	U	1 1	U U	U	U	C

F and Q are equivalent because they have the same truth table.

Identities of Boolean Algebra

-	Identity law	1A = A 0 + A = A
-	Null law	0A = 0 $1 + A = 1$
-	Idempotent law	AA = A A + A = A
-	Inverse law	AA' = 0 A + A' = 1
-	Commutative law	AB = BA $A + B = B + A$
-	Associative law	(AB)C = A(BC) $(A + B) + C = A + (B + C)$
-	Distributive law	A + BC = (A + B)(A + C) $A(B + C) = AB + AC$
-	Absorption law	A(A + B) = A $A + AB = A$
-	De Morgan's law	(AB)' = A' + B' (A + B)' = A'B'

Example:

F = A'B' + A'B = A'(B' + B) distributive = A'(1) inverse = A' identity Q = A' + A'B + A'B' = A' + A'B' absorption = A' absorption

Universal Gates

Any Boolean function can be constructed with NOT, AND, and OR gates

NAND and NOR = **universal gates**

DeMorgan's Law shows how to make AND from NOR (and vice-versa)

AB = (A' + B')' (AND from NOR) A + B = (A'B')' (OR from NAND) $A = \bigcirc F = A = \bigcirc F = F$ $A = \bigcirc F = A = \bigcirc$

NOT from a NOR



OR from a NOR



To implement a function using only NOR gates:

- apply DeMorgan's Law to each AND in the expression until all ANDs are converted to NORs
- use a NOR gate for any NOT gates, as well.
- remove any redundant gates (NOT NOT, may remove both)

Implementing the circuit using only NAND gates is similar.

Example: Q = (AB)'B'= (A' + B')B'= ((A'+B')' + B)' NOTE: you can use a NOR gate to produce A' and you can do the same for B'

Simplifying Circuits or Proving Equivalency

General rule to simplify circuits or prove equivalency:

- 1. Distribute if possible, and if you can't, apply DeMorgan's Law so that you can.
- 2. Apply other identities to remove terms, and repeat step 1.

EXAMPLE: Is (A'B)'(AB)' + A'B' equivalent to (AB)'?

$$F = (A'B)'(AB)' + A'B'$$

= (A + B') (A' + B') + A'B'
= AA' + AB' + A'B + B'B' + A'B'
= 0 + AB' + A'B + B' + A'B'
= AB' + A'B + A'B'
= B' (A+ A') + A'B
= B' (A+ A') + A'B
= B' + (A + B')'
= (B(A + B'))'
= (AB + BB')'
= (AB + 1)'
= (AB)'

-- can't distribute DeMorgan's distributive inverse and idempotent identity distributive inverse identity DeMorgan's DeMorgan's distributive inverse identity

Demo LogicWorks