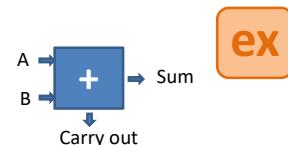
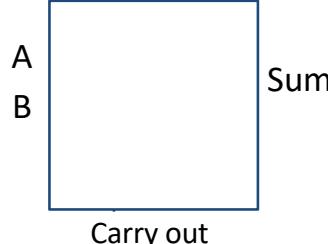
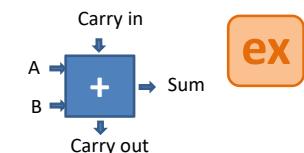
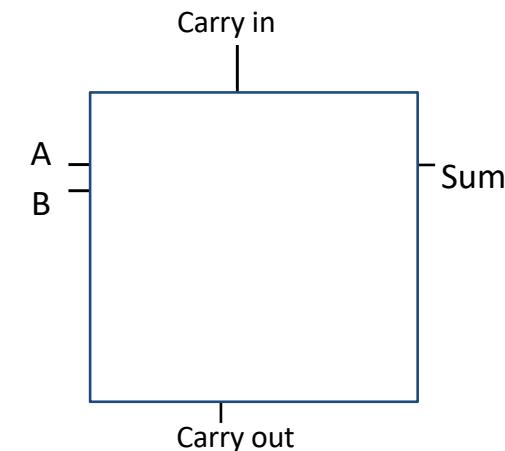


## Addition: 1-bit *half* adder



| A | B | Carry out | Sum |
|---|---|-----------|-----|
| 0 | 0 |           |     |
| 0 | 1 |           |     |
| 1 | 0 |           |     |
| 1 | 1 |           |     |

## Addition: 1-bit *full* adder



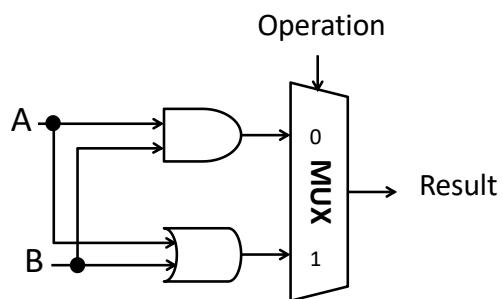
| Carry in | A | B | Carry out | Sum |
|----------|---|---|-----------|-----|
| 0        | 0 | 0 |           |     |
| 0        | 0 | 1 |           |     |
| 0        | 1 | 0 |           |     |
| 0        | 1 | 1 |           |     |
| 1        | 0 | 0 |           |     |
| 1        | 0 | 1 |           |     |
| 1        | 1 | 0 |           |     |
| 1        | 1 | 1 |           |     |

## 1-bit ALU for bitwise operations

ex

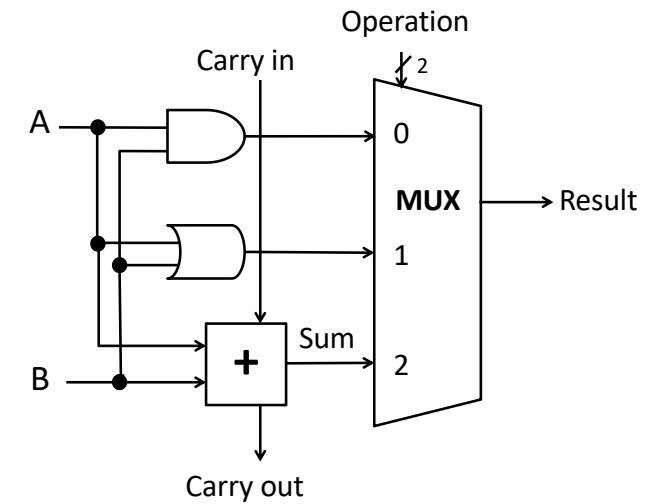
Build an n-bit ALU from n 1-bit ALUs.

Each bit  $i$  in the result is computed from the corresponding bit  $i$  in the two inputs.



| Op | A | B | Result |
|----|---|---|--------|
| 0  | 0 | 0 |        |
| 0  | 0 | 1 |        |
| 0  | 1 | 0 |        |
| 0  | 1 | 1 |        |
| 1  | 0 | 0 |        |
| 1  | 0 | 1 |        |
| 1  | 1 | 0 |        |
| 1  | 1 | 1 |        |

## 1-bit ALU



## ALU conditions

Extra ALU outputs  
describing properties of result.

**Zero Flag:** ex

1 if result is 00...0 else 0

**Sign Flag:** ex

1 if result is negative else 0

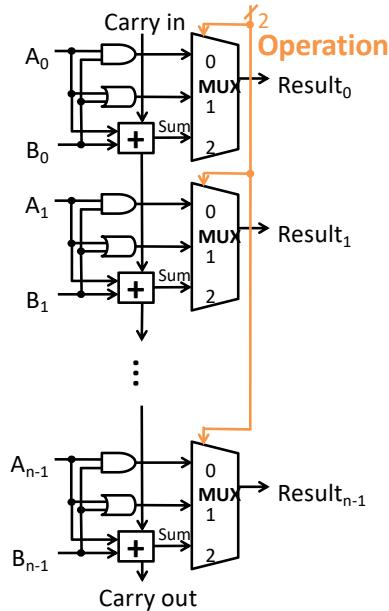
**Carry Flag:**

1 if carry out else 0

**(Signed) Overflow Flag:**

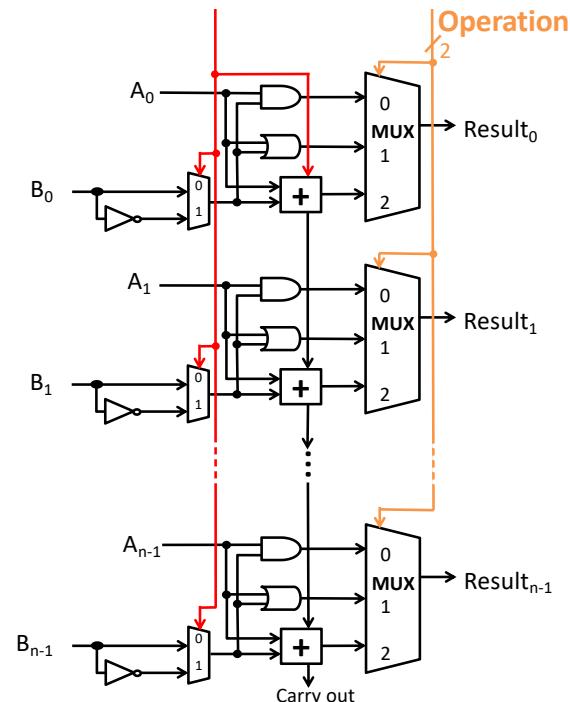
1 if signed overflow else 0

Implement these.

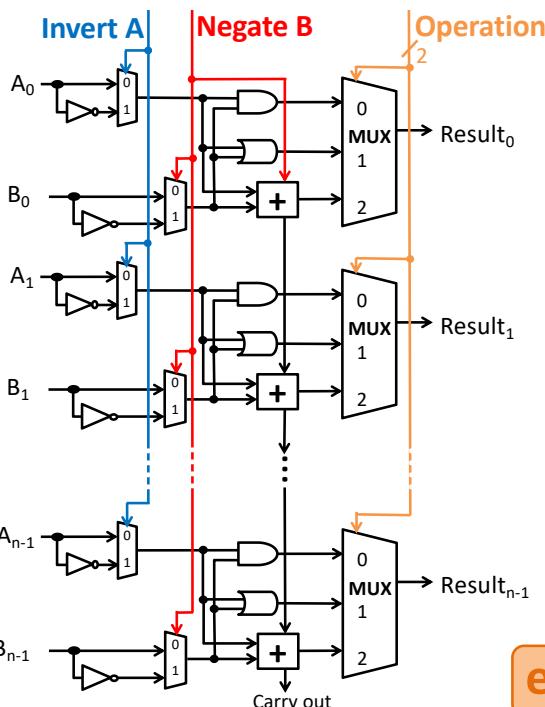


## Add subtraction

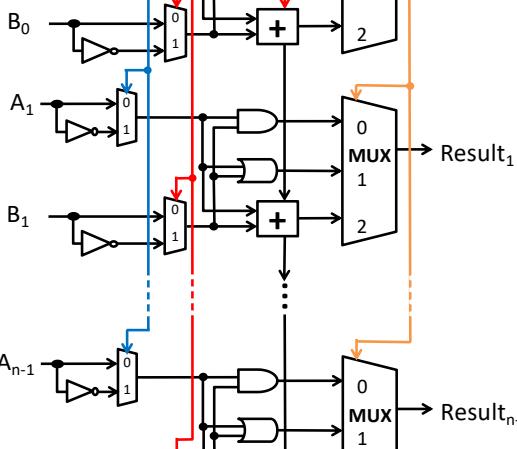
How can we control ALU inputs  
or add minimal new logic  
to compute  $A-B$ ?



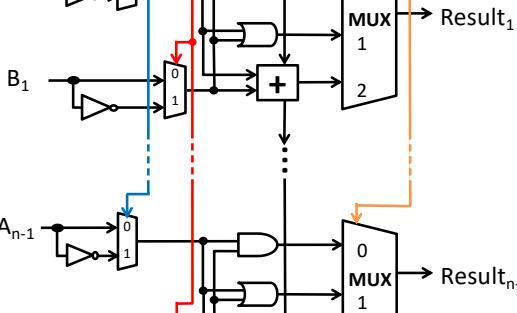
**A NAND B**



**A NOR B**



**A<B**



**A==B**

How can we control ALU inputs  
or add minimal new logic  
to compute each?

ex