Transistors (more in lab)

## If Base voltage is high:

Current may flow freely
from Collector to Emitter.
If Base voltage is low:
Current may not flow
from Collector to Emitter.


Five basic gates: define with truth tables


## Gateway to computer science




## NAND is universal.



All Boolean functions can be implemented using only NANDs. Build NOT, AND, OR, NOR, using only NAND gates.

## Larger gates

Build a 4-input AND gate using any number of 2-input gates.


## XOR: Exclusive OR



Truth table:

Output = 1 if exactly one input $=1$.

Build from earlier gates:

Often used as a one-bit comparator.

Video game designers, Halloween costumers extraordinaire, sci-fi/fantasy screenwriters, I have an idea...

## Circuit simplification

Is there a simpler circuit that performs the same function?


Start with an equivalent Boolean expression, then simplify with algebra.
$F(A, B, C)=$

Check the answer with a truth table.

## Circuit derivation: code detectors

AND gate + NOT gates = code detector, recognizes exactly one input code.


Design a 4-input code detector to output 1 if $A B C D=1001$, and 0 otherwise.


Design a 4-input code detector to accept two codes ( $A B C D=1001, A B C D=1111$ ) and reject all others. (accept $=1$, reject $=0$ )

## Circuit derivation: sum-of-products form

logical sum (OR)
of products (AND)
of inputs or their complements (NOT)

Draw the truth table and design a sum-of-products circuit for a 4-input code detector to accept two codes ( $\mathrm{ABCD}=1001, \mathrm{ABCD}=1111$ ) and reject all others.
How are the truth table and the sum-of-products circuit related?

## Voting machines

A majority circuit outputs 1 if and only if a majority of its inputs equal 1.
Design a majority circuit for three inputs. Use a sum of products.

| A | B | C | Majority |
| :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 |

Triply redundant computers in spacecraft

- Space program also hastened Integrated Circuits.

