Wellesley CS 240

Integer Representation

Representation of integers: unsigned and signed Modular arithmetic and overflow Sign extension Shifting and arithmetic

Multiplication

Casting

modular arithmetic, overflow

x+y in *n*-bit unsigned arithmetic is

in math

unsigned overflow =

Unsigned addition overflows if and only if

sign-magnitude



Most-significant bit (MSB) is sign bit

0 means non-negative 1 means negative

Remaining bits are an unsigned magnitude

8-bit sign-magnitude: Anything weird here?

00000000 represents _____

01111111 represents

Example: 4 - 3! = 4 + (-3)

Arithmetic?

10000101 represents

00000100 +10000011

10000000 represents

Zero?

n-bit two's complement numbers:

minimum =

8-bit representations 00001001

1111111

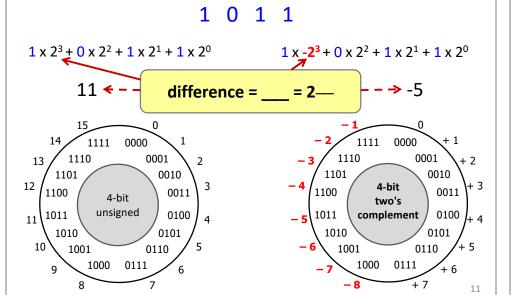
10000001

00100111

maximum =

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4-bit unsigned vs. 4-bit two's complement

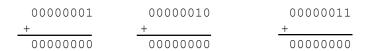


Another derivation



How should we represent 8-bit negatives?

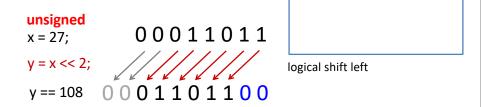
- For all positive integers x,
 we want the representations of x and -x to sum to zero.
- We want to use the standard addition algorithm.

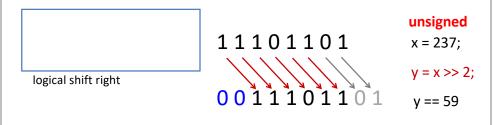


Find a rule to represent –x where that works...

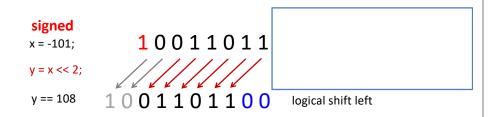
16

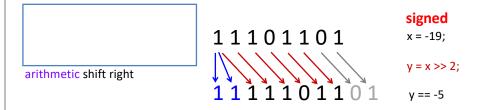
unsigned shifting and arithmetic





two's complement shifting and arithmetic





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shift-and**-add**



Available operations

```
x \ll k implements x * 2^k
x + y
```

Implement y = x * 24 using only <<, +, and integer literals

What does this function compute?



```
unsigned puzzle(unsigned x, unsigned y) {
  unsigned result = 0;
  for (unsigned i = 0; i < 32; i++) {
    if (y & (1 << i)) {
      result = result + (x << i);
    }
  }
  return result;
}</pre>
```

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