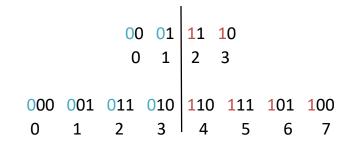
But first ... WELLESLEY Recall: sum of products CS 240 Foundations of Computer Systems logical sum (OR) of products (AND) of inputs or their complements (NOT). **Combinational Logic** СМ Construct with: В • 1 code detector per 1-valued output row 0 0 0 0 • 1 large OR of all code detector outputs 0 0 1 0 Karnaugh maps 0 0 1 Is it minimal? Building blocks: encoders, decoders, multiplexers 1 **1** 1 0 0 0 0 1 **1** bstraction 0 1 1 1 1 1 1 **1** https://cs.wellesley.edu/~cs240/ Combinational Logic 1 Combinational Logic 2

Gray Codes = reflected binary codes

Alternate binary encoding designed for electromechanical switches and counting.



How many bits change when incrementing?

Combinational Logic 3

Karnaugh Maps: find (minimal) sums of products											
					gray code		CD				
Α	в	С	D	F(A, B, C,		der 🦳	≻ 00	01	11	10	
0	0	0	0	0	,	*					
0	0	0	1	0		00	0	0	0	0	
0	0	1	0	0							
0	0	1	1	0		01	0	0	0	1	
0	1	0	0	0	AB						
0	1	0	1	0		11	1	1	0	1	
0	1	1	0	1							
0	1	1	1	0		10	1	1	1	1	
1	0	0	0	1							
1	0	0	1	1 1.	Cover exactly the 1s by drawing a (minimum) number of						
1	0	1	0	1	maximally sized rectangles whose dimensions (in cells)						
1	0	1	1	1	are powers of 2. (They may overlap or wrap around!) For each rectangle, make a <i>product</i> of the inputs (or complements) that are 1 for all cells in the rectangle.						
1	1	0	0	1 2.							
1	1	0	1	1							
1	1	1	0	1	(minterms)						
1	1	1	1	0 3.	Take the <i>sum</i> of these products.						
									Combinat	ional Logic	4

