



Currying and Partial Application

and other tasty closure recipes

More idioms for closures

- Function composition
- Currying and partial application
- Callbacks (e.g., reactive programming, **later**)
- Functions as data representation (**later**)

Function composition

```
fun compose (f,g) = fn x => f (g x)
```

Closure “remembers” f and g

```
:( 'b -> 'c) * ('a -> 'b) -> ('a -> 'c)
```

REPL prints something equivalent

ML standard library provides infix operator o

```
fun sqrt_of_abs i = Math.sqrt(Real.fromInt(abs i))  
fun sqrt_of_abs i = (Math.sqrt o Real.fromInt o abs) i  
val sqrt_of_abs = Math.sqrt o Real.fromInt o abs
```

Right to left.

Pipelines (left-to-right composition)

“Pipelines” of functions are common in functional programming.

```
infix |>  
fun x |> f = f x  
  
fun sqrt_of_abs i =  
  i |> abs |> Real.fromInt |> Math.sqrt
```

(F#, Microsoft's ML flavor, defines this by default)

Currying

- Every ML function takes exactly one argument
- Previously encoded n arguments via one n -tuple
- Another way:
Take one argument and return a function that takes another argument and...
 - Called “currying” after logician Haskell Curry

Example

```
val sorted3 = fn x => fn y => fn z =>
              z >= y andalso y >= x

val t1 = ((sorted3 7) 9) 11
```

- Calling `(sorted3 7)` returns a closure with:
 - Code `fn y => fn z => z >= y andalso y >= x`
 - Environment binds `x` to 7
- Calling *that* closure on 9 returns a closure with:
 - Code `fn z => z >= y andalso y >= x`
 - Environment binds `x` to 7, `y` to 9
- Calling *that* closure on 11 returns `true`

Function application is left-associative

```
val sorted3 = fn x => fn y => fn z =>
              z >= y andalso y >= x

val t1 = ((sorted3 7) 9) 11
```

means

```
e1 e2 e3 e4
(((e1 e2) e3) e4)
```

```
val t1 = sorted3 7 9 11
```

Callers can just think
“multi-argument function with spaces instead of a tuple expression”
Does not interchange with tupled version.

Function definitions are sugar (again)

```
val sorted3 = fn x => fn y => fn z =>
              z >= y andalso y >= x

val t1 = ((sorted3 7) 9) 11
```

```
fun f p1 p2 p3 ... = e
desugars to
fun f p1 = fn p2 => fn p3 => ... => e
```

```
fun sorted3 x y z = z >= y andalso y >= x
```

Callees can just think
“multi-argument function with spaces instead of a tuple pattern”
Does not interchange with tupled version.

Final version

```
fun sorted3 x y z = z >= y andalso y >= x
val t1 = sorted3 7 9 11
```

As elegant syntactic sugar (fewer characters than tupling) for:

```
val sorted3 = fn x => fn y => fn z =>
              z >= y andalso y >= x
val t1 = ((sorted3 7) 9) 11
```

Function application is left-associative.

Types are right-associative:

```
sorted3 : int -> int -> int -> bool
```

means

```
sorted3 : int -> (int -> (int -> bool))
```

Curried foldl

```
fun foldl f acc xs =
  case xs of
  [] => acc
  | x::xs' => foldl f (f(x,acc)) xs'
fun sum xs = foldl (fn (x,y) => x+y) 0 xs
```

Partial Application

```
fun foldl f acc xs =
  case xs of
  [] => acc
  | x::xs' => foldl f (f(acc,x)) xs'
fun sum_inferior xs = foldl (fn (x,y) => x+y) 0 xs
val sum = foldl (fn (x,y) => x+y) 0
```

foldl (fn (x,y) => x+y) 0
evaluates to a closure that, when called with a list xs, evaluates
the case-expression with:

f bound to the result of foldl (fn (x,y) => x+y)
acc bound to 0

Unnecessary function wrapping

```
fun f x = g x (* bad *)
val f = g (* good *)

(* bad *)
fun sum_inferior xs = fold (fn (x,y) => x+y) 0 xs

(* good *)
val sum = fold (fn (x,y) => x+y) 0

(* best? *)
val sum = fold (op+) 0
```

Treat infix operator
as normal function.

Iterators and partial application

```
fun exists predicate xs =
  case xs of
    [] => false
  | x::xs' => predicate x
           orelse exists predicate xs'

val no = exists (fn x => x=7) [4,11,23]
val hasZero = exists (fn x => x=0)
```

For this reason, ML library functions of this form are usually curried

– `List.map`, `List.filter`, `List.foldl`, ...

The Value Restriction ☹️

If you use partial application to *create a polymorphic function*, it may not work due to the **value restriction**

- Warning about “type vars not generalized”
 - And won't let you call the function
- This should surprise you; you did nothing wrong ☺️ but you still must change your code.
- See the code for workarounds
- Can discuss a bit more when discussing type inference

More combining functions

- What if you want to curry a tupled function or vice-versa?
- What if a function's arguments are in the wrong order for the partial application you want?

Naturally, it is easy to write higher-order wrapper functions

– And their types are neat logical formulas

```
fun other_curry1 f = fn x => fn y => f y x
fun other_curry2 f x y = f y x
fun curry f x y = f (x,y)
fun uncurry f (x,y) = f x y
```