

CS 251 Fall 2019 **Principles of Programming Languages** Ben Wood



Datatypes, Patterns, and Parametric Polymorphism

Topics

- Tuples and records
- Positional vs. nominal
- Datatypes
- Pattern matching
- Parametric polymorphic types (generics)
- Lists and options
- Equality types

Tuples

Syntax: (*e1*, ..., *en*)

Evaluation:

- 1. Evaluate e1 to v1, ..., and en to vn.
- 2. The result is (v1, ..., vn)

Type checking:

If e1 has type t1, ..., and en has type tn, then the pair expression has type ta * ... * tn

Tuple bindings

Syntax: val(x1, x2) = e

Type checking: If e has type $\pm 1 + \pm 2$, then #1 e has type ± 1 and #2 e has type ± 2

Evaluation:

- 1. Evaluate e to a pair of values (v1, v2) in the current dynamic environment
- 2. Extend the current dynamic environment by binding x1 to v1 and x2 to v2.

Tuple accessors

Syntax: <mark>#1 e</mark> #2 e

Type checking:

If e has type t1 * t2, then #1 e has type t1 and #2 e has type t2

Evaluation:

- Evaluate e to a pair of values v1 and v2 in the current dynamic environment
- 2. The result v1 if using #1; v2 if using #2

Examples

```
fun swap (pr : int*bool) =
  let val (x,y) = pr in (y,x) end
fun sum two pairs (pr1 : int*int, pr2 : int*int) =
  let val (x1, y1) = pr1
      val (x2, y2) = pr2
  in x1 + y1 + x2 + y2 end
fun div mod (x : int, y : int) =
  (x div y, x mod y)
fun sort pair (pr : int*int) =
 let val (x, y) = pr
  in
    if x < y then pr else (y, x)
  end
```

Records

Record values have fields (any name) holding values $\{f1 = v1, ..., fn = vn\}$

Record types have fields (any name) holding types {f1 : t1, ..., fn : tn}

Order of fields in a record value or type never matters

Building records:

 ${f1 = e1, ..., fn = en}$

Accessing components:

#myfieldname e

(Evaluation rules and type-checking as expected)

Example

{name = "N	Wendy",	id =	41123	- 12}	
Has type		in+	namo	ctring	
rias type	{±a :	INT,	name	string}	
Evaluates to	{id =	41111	, name	e = "Wendy	z"]

If an expression, e.g. variable \mathbf{x}_{i} has this type, then get fields with:

#id x #name x

No record type **declarations!**

- The same program could also make a

{id=true,ego=false} of type {id:bool,ego:bool}

By position vs. by name

(structural/positional)

(nominal)

(4,7,9) {f=4,g=7,h=9}

Common syntax decision

Common hybrid: function/method arguments

Tuples are sugar

<mark>(e1,...,en)</mark> desugars to

{1=e1,...,n=en}

<mark>t1*…*</mark>tn

desugars to

{1:t1,...,n:tn}

Records with contiguous fields 1...n printed like tuples Can write $\{1=4, 2=7, 3=9\}$, bad style

Lists

Racket: (cons 1 (cons 2 (cons 3 null)))

ML has a "no value" value written (), pronounced "unit," with type **unit**

What is the type of: (1, (2, (3, ())))

What is the type of: (1, (2, (3, (4, ()))))

Why is this a problem?

How to build bigger data types

Data type building blocks in any language

– Product types ("Each of"):

Value contains values of each of t1 t2 ... tn Value contains a t1 and a t2 and ... and a tn

- Sum types ("One of"):

Value contains values of one of t1 t2 ... tn Value is t1 xor a t2 xor ... xor a tn

– Recursive types ("Self reference"):
 A t value can refer to other t values

Datatype bindings

Algebraic Data Type

- Adds new type mytype to environment
- Adds constructors to environment: **TwoInts**, **Str**, **Pizza**
- Constructor: function that makes values of new type (or is a value of new type):
 - TwoInts : int * int -> mytype
 - Str : string -> mytype
 - Pizza : mytype

Datatypes: constructing values

- Values of type mytype produced by one of the constructors
- Value contains:
 - Tag: which constructor (e.g., TwoInts)
 - Carried value (e.g., (7,9))
- Examples:
 - TwoInts (3+4,5+4) evaluates to TwoInts (7,9)
 - Str if true then "hi" else "bye" evaluates to Str "hi"
 - Pizza isavalue

Datatypes: using values

- 1. Check what *variant* it is (what constructor made it)
- 2. Extract carried *data* (if that variant has any)

ML could create functions to get parts of datatype values

- Like to *pair?* or *cdr* in Racket
- Instead it does something much better...

Pattern matching



Case expression and pattern-matching

```
fun f x = (* f has type mytype -> int *)
  case x of
    Pizza => 3
    | TwoInts(i1,i2) => i1+i2
    | Str s => String.size s
```

All-in-one:

- Multi-branch conditional, picks branch based on variant.
- Extracts data and binds to branch-local variables.
- Type-check: all branches must have same type.
- Gets even better later.

Pattern matching

Syntax:

- case e0 of
 p1 => e1
 p2 => e2
 ...
 pn => en
- (For now), each pattern **pi** is:
 - a constructor name followed by the right number of variables:
 - $\mathbf{C} \text{ or } \mathbf{D} \mathbf{x} \text{ or } \mathbf{E} (\mathbf{x}, \mathbf{y}) \text{ or } \dots$
- Patterns are not expressions.
 - We do not evaluate them.
 - We match eO against their structure.
- Precise type-checking/evaluation rules later...

Pattern matching rocks.

- 1. Cannot forget a case (inexhaustive pattern-match warning)
- 2. Cannot duplicate a case (redundant pattern type-checking error)
- 3. Cannot forget to test the variant correctly and get an error ((car null) in Racket)
- It's much more general.
 Supports elegant, concise code.

Useful examples

Enumerations, carrying other data

Alternate ways of identifying real-world things/people

Lists!

- A list is either:
 - The empty list; or
 - A pair of a list element and a list that holds the rest of the list.



Accessing Lists

val some_ints = Cons (1, Cons (2, Cons (3, Empty)))

```
fun length (xs : mylist) =
  case xs of
    Empty => 0
    Cons (x, xs') => 1 + length xs'
```

```
fun sum (xs : mylist) =
  case xs of
    Empty => 0
    Cons (x, xs') => x + sum xs'
```

Syntactic sugar for lists: build

The empty list is a value: []

A list of expressions/values is an expression/value:

[e1,e2,...,en] [v1,v2,...,vn]

If e1 evaluates to v
and e2 evaluates to a list [v1,...,vn],
then e1::e2 evaluates to [v,v1,...,vn]

Syntactic sugar for lists: access

val some_ints = [1,2,3]

note the space between int and list

fun length (xs : int list) =
 case xs of
 [] => 0
 | x::xs' => 1 + length xs'

fun sum (xs : int list) =
 case xs of
 [] => 0
 | x::xs' => x + sum xs'

Type-checking list operations

For any type t, type t list describes lists where all elements have type t

int list bool list int list list
(int * int) list (int list * int) list

[]: t list list for any type t SML uses type 'a list to indicate this ("quote a" or "alpha")

e1::e2 : t list if and only if: - e1 : t and - e2 : t list

More on 'a soon! (Nothing to do with 'a in Racket.)

Example list functions

(types?)

```
fun countdown (x : int) =
  if x=0
  then []
  else x :: countdown (x-1)
fun append (xs : int list, ys : int list) =
  case xs of
      [] => ys
    x::xs' => x :: append (xs', ys)
fun rev (xs : int list) =
  let fun revtail (acc : int list, xs : int list) =
        case xs of
            [] => acc
            x::xs' => revtail (x :: acc, xs')
  in
    revtail ([], xs)
  end
                                        Datatypes, Patterns, and Parametric
```

Example higher-order list functions

- These examples only work on lists of ints.
- Should be more general: work on any list
 - and any function for map...

Polymorphic types + type inference

The identity function: fun id (x : int) = x val id : int -> int

Omit the type:fun id x = xval id : 'a -> 'a

General!

- 'a is a *polymorphic type variable* stands in for *any type*
- "id takes an argument of any type and returns a result of that same type."

Polymorphic types + type inference

Works on *any* type of pair!

```
val pair = swap (4, "hello")
('a * 'b) is more general than (int * string).
```

Here, int *instantiates* 'a and string *instantiates* 'b.

Polymorphic datatypes

Lists that can hold elements of any one type.

A list of "alphas" is either:

- the empty list; or
- a pair of an "alpha" and a list of "alphas"

The type **int list** is an *instantiation* of the type 'a list, where the type variable 'a is *instantiated* with int.

Polymorphic list functions

(types?)

```
fun append (xs, ys) =
 case xs of
     [] => ys
    | x::xs' => x :: append (xs', ys)
fun rev (xs) =
 let fun revtail (acc : int list, xs : int list) =
        case xs of
            [] => acc
          x::xs' => revtail (x :: acc, xs')
  in revtail [] xs end
fun map (f, xs) =
 case xs of
     [] => []
    x::xs' => f x :: map (f, xs')
```

Polymorphic list functions

(type?)

```
fun map (f, xs) =
   case xs of
    [] => []
    | x::xs' => f x :: map (f, xs')
```

- Type inference system chooses most general type.
- Polymorphic types show up commonly with higherorder functions.
- Polymorphic function types often give you a good idea of what the function does.

Exceptions

An exception binding introduces a new kind of exception

exception MyFirstException
exception MySecondException of int * int

The raise primitive raises (a.k.a. throws) an exception

raise MyFirstException
raise (MySecondException (7,9))

A handle expression can handle (a.k.a. catch) an exception

- If doesn't match, exception continues to propagate

Actually...

Exceptions are a lot like datatype constructors...

- Declaring an exception adds a constructor for type exn
- Can pass values of exn anywhere (e.g., function arguments)
 - Not too common to do this but can be useful
- handle can have multiple branches with patterns for type exn, just like a case expression.

• See examples in exnopt.sml

Options

datatype 'a option = NONE | SOME of 'a

t option is a type for any type t

Building:

- NONE has type 'a option (much like [] has type 'a list)
- SOME e has type t option if e has type t (much like e::[])

Accessing:

• Pattern matching with case expression

Good style for functions that don't always have a meaningful result. See examples in exnopt.sml

Parametric Polymorphism and the power of what you cannot do.

Type 'a means "some type, but don't know what type"

What can a function of type 'a list -> int do?
 fun f (xs : 'a list) : int = ...
'a -> 'a ?
 fun g (x : 'a) : 'a = ...

Equality Types

So if we cannot inspect values of type 'a in any way, how do we write a general contains function?

fun contains (xs : 'a list, x : 'a) : bool = ...

eqtypes (equality types):

Special category of types that support comparison. Accompanying eqtype variables with double quotes

Mostly accurate:

fun contains (xs : ''a list, x : ''a) : bool = \dots