

# Closures implement lexical scope.

Closures allow functions to use any binding in the environment where the function is defined, regardless of where it is applied.

#### Anonymous function definition expressions

Syntax:  $(1 \text{ ambda } (x1 \dots xn) e)$ 



- parameters: x1 through xn are identifiers
- **body:** e is any expression

#### **Evaluation:**

1. The result is a *function closure*, (E, (lambda (x1...xn)e)), holding the current environment, E, and the function.

#### [closure]

 $E \vdash (lambda (x1 ... xn) e) \downarrow \langle E, (lambda (x1 ... xn) e) \rangle$ 

#### Note:

- An anonymous function definition is an expression.
- A function closure is a new kind of value. Closures are not expressions.
- This is a *definition*, not a call. The body, *e*, is not evaluated now.
- lambda from the λ-calculus.

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#### **Function application (call)**

Syntax: (*e0 e1 ... en*)

#### **Evaluation:**

- 1. Under the current dynamic environment, E, evaluate e0 through en to values v0, ..., vn.
- 2. If v0 is a function closure of n arguments,  $\langle E', (lambda (x1...xn) e) \rangle$  then

The result is the result of evaluating the closure body, e, under the closure environment, E', extended with argument bindings:  $x1 \mapsto v1$ , ...,  $xn \mapsto vn$ .

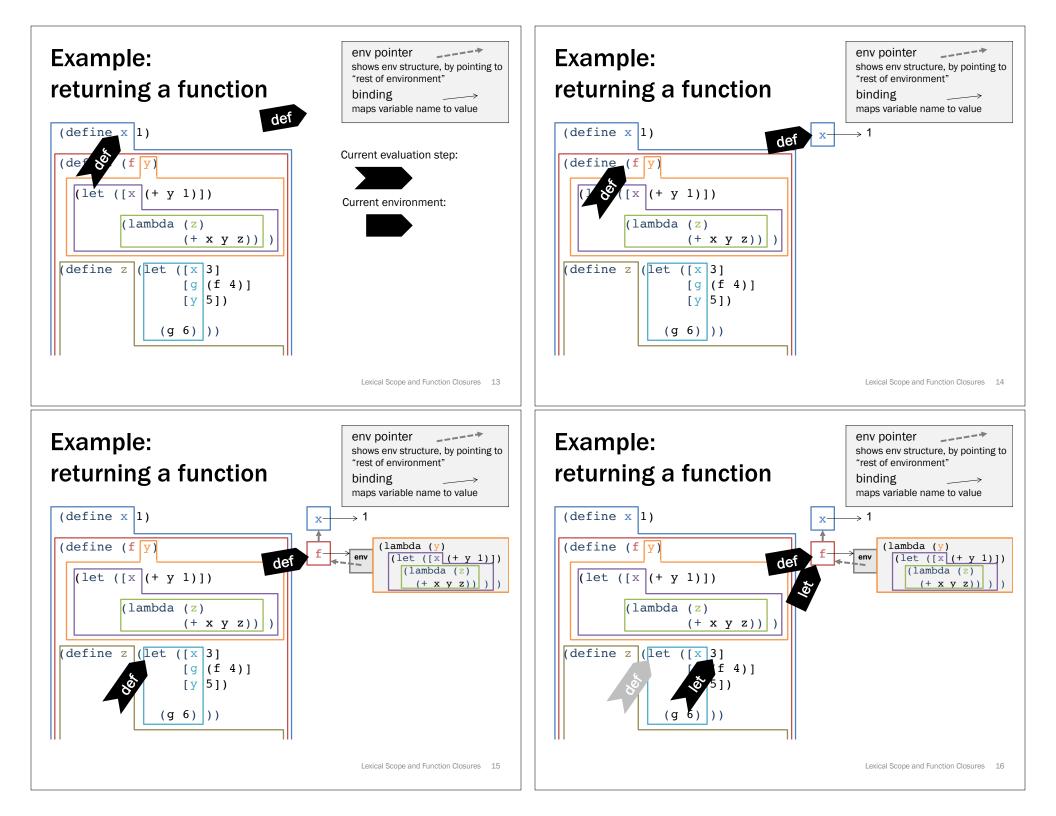
Otherwise, there is a type error.

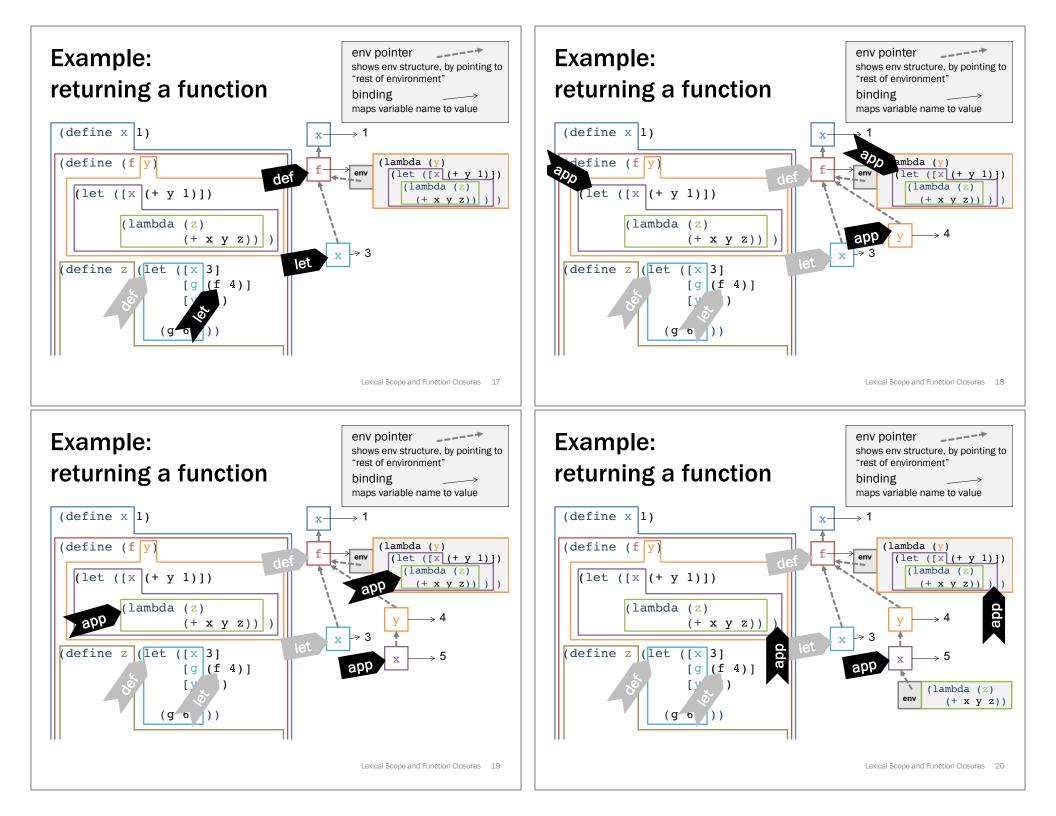
### Function application (call) Syntax: (e0 e1 ... en) Evaluation: $E \vdash e0 \downarrow (E', (lambda (x1 ... xn) e))$ $E \vdash e1 \downarrow v1$ ... $E \vdash en \downarrow vn$ $x1 \vdash v1, ..., xn \vdash vn, E' \vdash e \downarrow v$ $E \vdash (e0 e1 ... en) \downarrow v$ [apply]

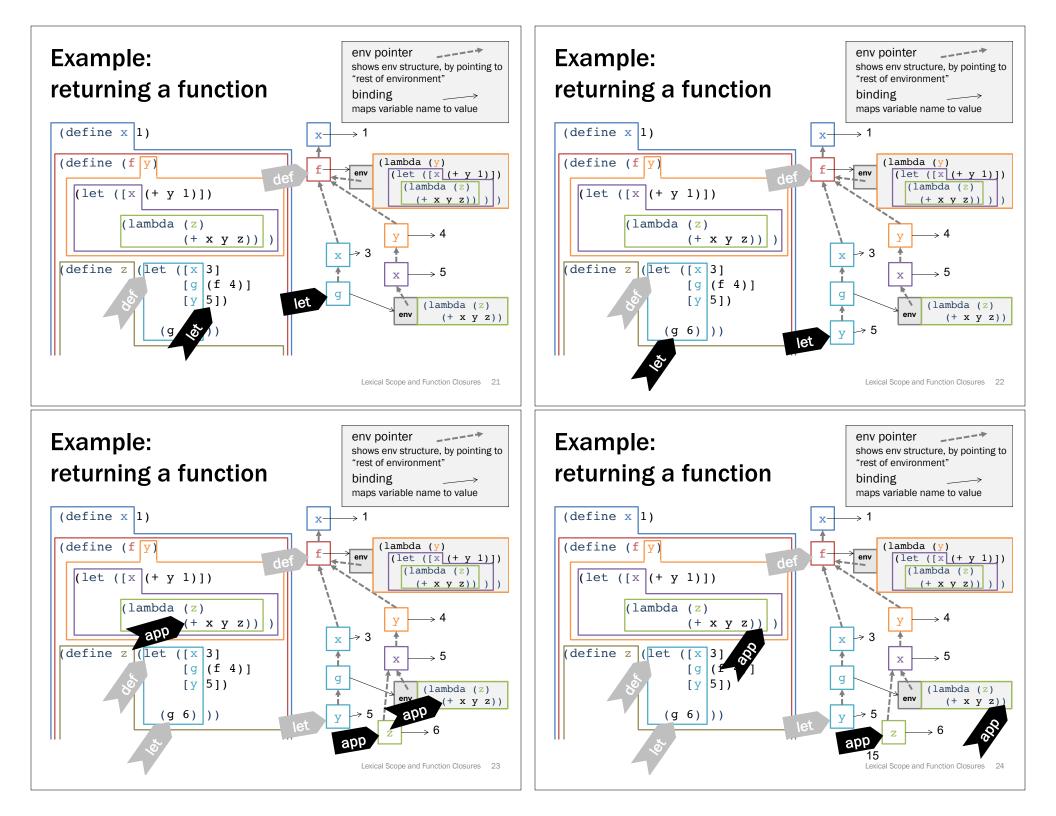
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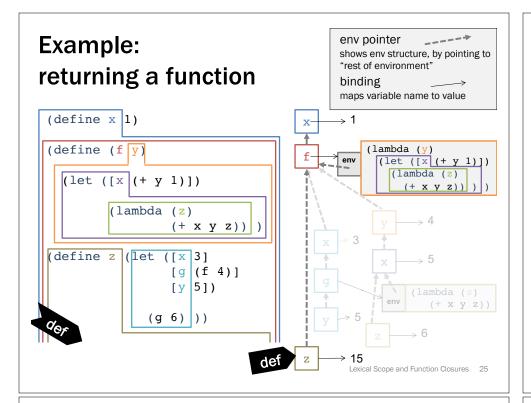
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Neek









## PL design quiz

Java methods and C functions do not need closures because they \_\_\_\_\_

- a. cannot refer to names defined outside the method/function
- b. are not first class values
- c. do not use lexical scope
- d. are not anonymous (i.e., they are named)

```
Which, if any, are correct? Why?
```

# Debrief

- 1. Closures implement lexical scope.
- 2. Function bodies can use bindings from the environment where they were defined, not where they were applied.
- 3. The environment is not a stack.
  - Multiple environments (branches) may be live simultaneously.
  - CS 240's basic stack model will not suffice.
  - General case: heap-allocate the environment.
     GC will clean up for us!

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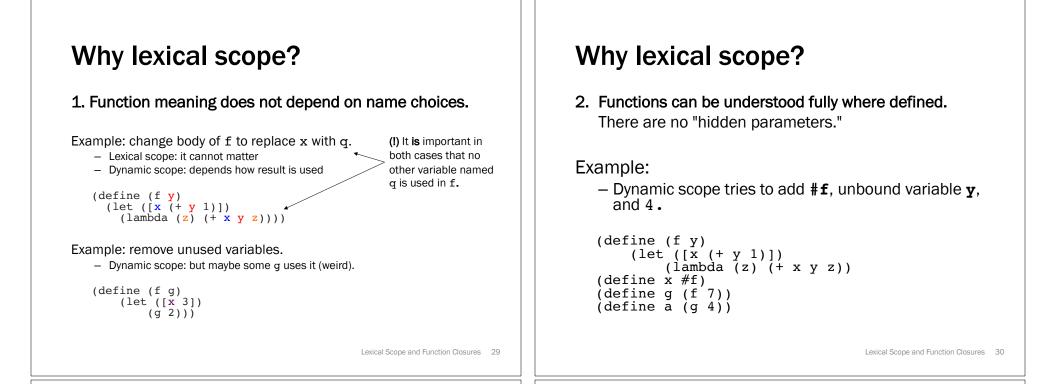
## Why lexical scope?

Lexical scope: use environment where function is defined.

Dynamic scope: use environment where function is applied.

History has shown that lexical scope is almost always better.

Here are some precise, technical reasons (not opinion).



#### Why lexical scope?

```
3a. Closures automatically "remember" the data they need.
More examples, idioms later.
```

```
(define (greater-than-x x)
  (lambda (y) (> y x)))
```

```
(define (no-negs xs)
  (filter (greater-than-x -1) xs))
```

```
(define (all-greater xs n)
  (filter (lambda (x) (> x n)) xs))
```

#### Why lexical scope?

3b. Closures are a useful way to avoid recomputation.

These functions filter lists of lists by length.

```
(define (all-shorter-than-1 lists mine)
  (filter (lambda (xs) (< (length xs) (length mine))) lists))</pre>
```

```
(define (all-shorter-than-2 lists mine)
  (let ([len (length mine)])
     (filter (lambda (xs) (< (length xs) len)) lists)))</pre>
```

How many times is the length function called?

### **Dynamic scope?**

- Lexical scope is definitely the right default for variables.
  - Nearly all modern languages
- Early LISP used dynamic scope.
  - Even though inspiration (lambda calculus) has lexical scope.
  - Later "fixed" by Scheme (Racket's parent) and other languages.
  - Emacs Lisp still uses dynamic scope.
- Dynamic scope is very occasionally convenient:
  - Racket has a special way to do it.
  - Perl has something similar.
  - Most languages are purely lexically scoped.
  - Exception raise/handle, throw/catch is like dynamic scope.

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#### **Remember when things evaluate!**

A function body is not evaluated until the function is called.

A function body is **evaluated every time** the function is called.

# A binding evaluates its expression **when the binding is evaluated**, not every time the variable is used.

As with lexical/dynamic scope, there are other options here that Racket does **not** use. We will consider some later.

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## **Relevant PL design dimensions**

in the Racket language:

- scope: lexical (static)
  - vs. dynamic
- parameter passing: pass-by-value (call-by-value)
   vs. by-reference, by-name, by-need
- evaluation order: eager (strict)

• vs. lazy

in our semantics of the Racket language:

- environments and closures
  - vs. substitution
- big-step operational semantics
  - vs. small-step

More on all of these dimensions (and alternatives) later!

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