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# Programming Languages

**CS 251**  
*Fall 2021*

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# Probabilistic Programming

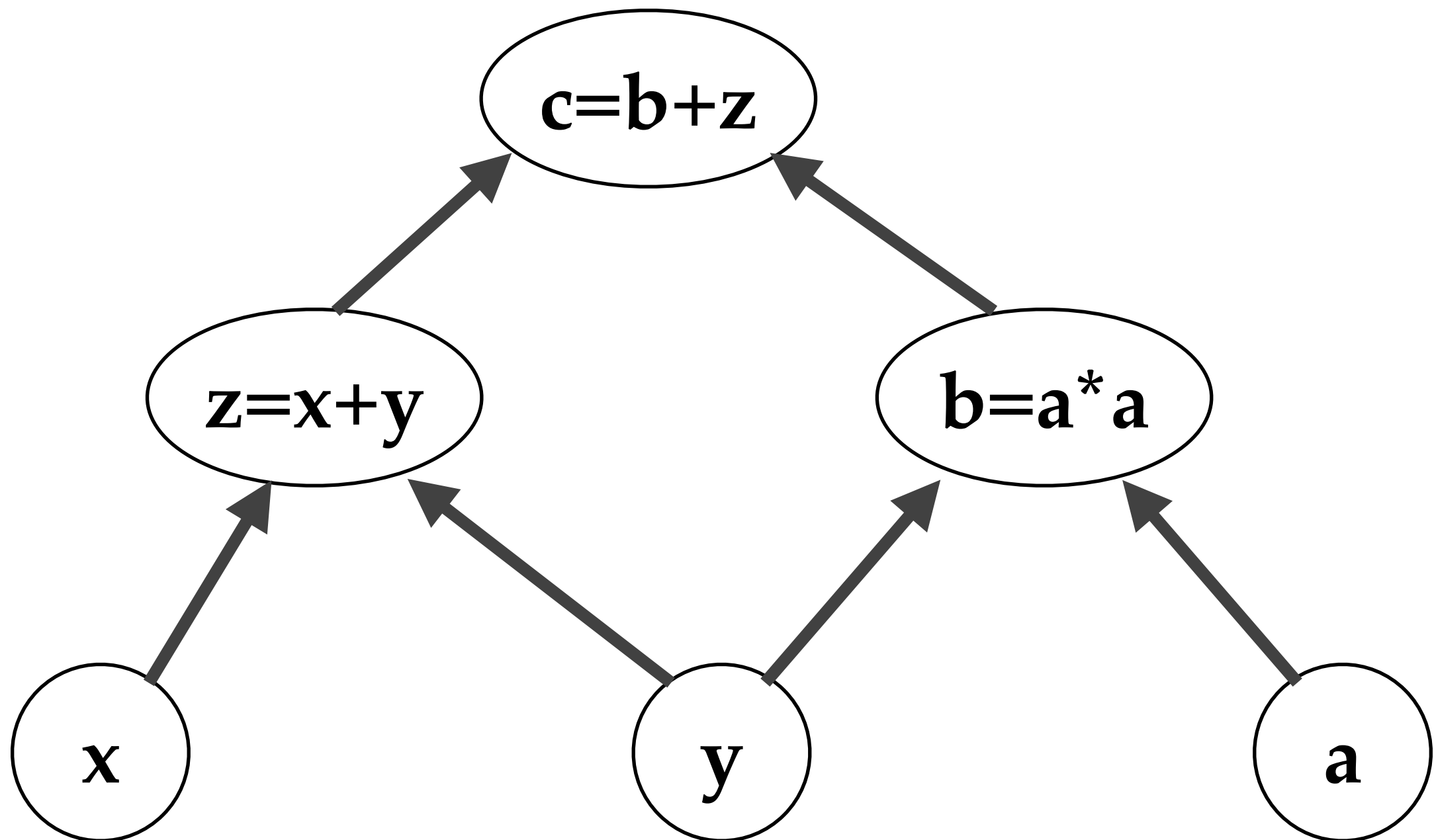
# Computation Graphs

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A **computation graph** is a directed graph where nodes represent operations and variables and edges define the order of computation.

# Computation Graphs

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# Probabilistic Programming Languages

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Probabilistic programming languages are useful for problems that require reasoning under uncertainty.

Key concept: the programs are probability models.

# Probability Model

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A probability model is a formal representation of a problem that involves non-determinism (randomness).

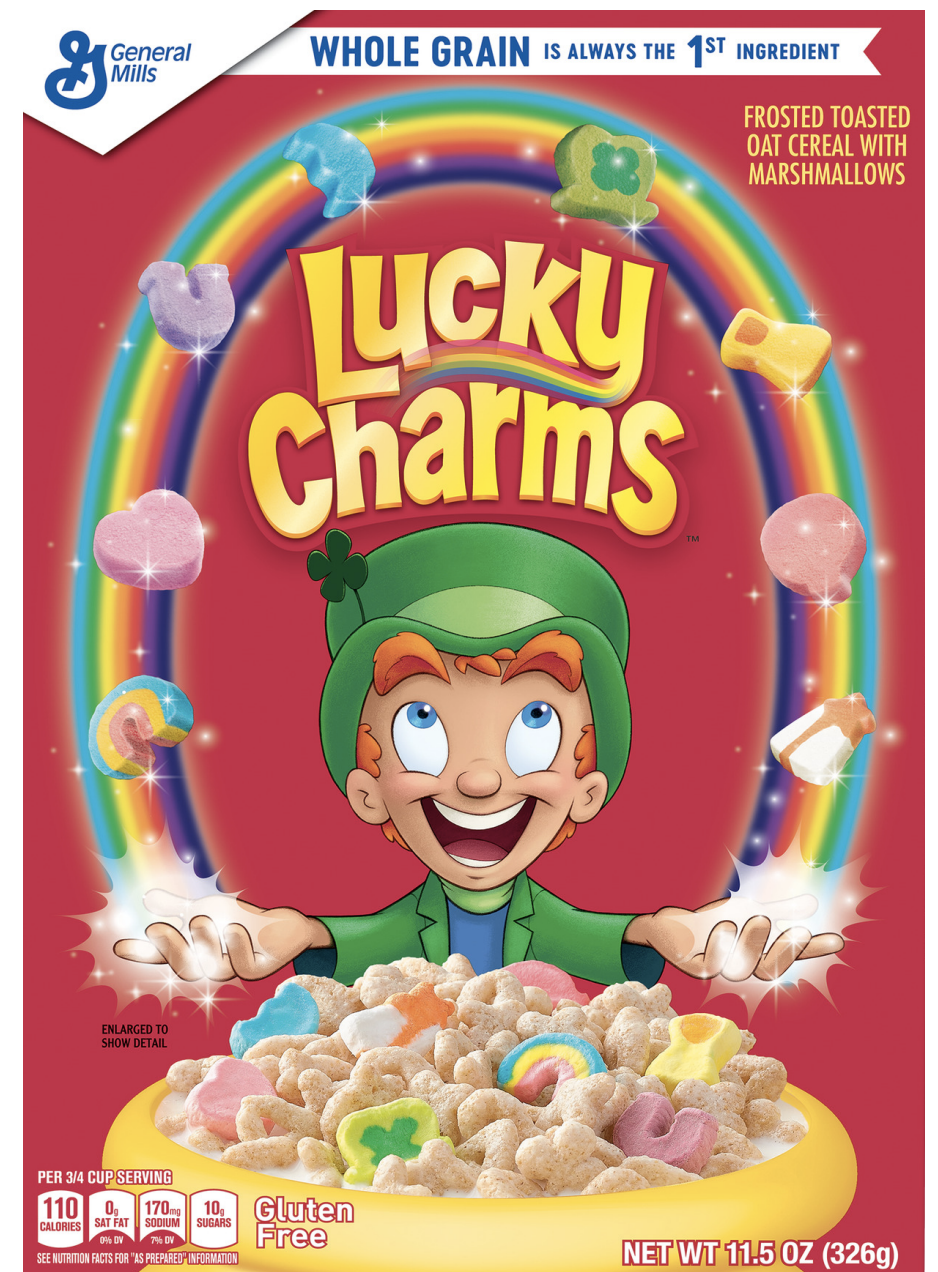
Three key parts: sample space, events, and probabilities for the events.

# Cereal Sampling

Imagine that we draw a single piece of Lucky Charms cereal.



Source: [www.village-bakery.com](http://www.village-bakery.com)



Source: <https://www.walmart.com>



# Cereal sampling

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Imagine that we draw two pieces of Lucky Charms cereal out of a bowl.

## Events:

Picking a horseshoe  
+ a rainbow

Picking a rainbow +  
a letter

Picking two letters

...



Source: [www.village-bakery.com](http://www.village-bakery.com)



# Cereal Sampling

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Sample space (set of all outcomes):

horseshoe + rainbow

rainbow + a letter

two letters

two rainbows

two horseshoes

horseshoe + letter

....

# Cereal Sampling

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## Probabilities:

$$p(\text{horseshoe}) = 0.1$$

$$p(\text{rainbow}) = 0.2$$

$$p(\text{letter}) = 0.7$$

$$p(\text{shooting star}) = 0.0$$

$$p(\text{balloon}) = 0.0$$

...

The probability of the sample space  
always sums to 1.

# Probabilistic Programming Languages

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Key concept: the programs are probability models.

PPLs have stochastic elements whose values are sampled on every run of the program. The meaning of the program is the probability of every possible execution of the program.

# Probabilistic Programming Languages

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Two main modes: **prediction** and **inference**. Prediction uses observed causes to guess unseen results; inference uses observed results to try to understand unseen causes.

# Probabilistic Programs as Computation Graphs

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From a computation graph point-of-view, **prediction** is the forward propagation of data through the graph, while **inference** is the backwards propagation of data.

# Figaro

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Figaro is a probabilistic programming language that uses Scala syntax.

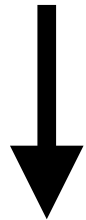
*This is another example of a domain-specific language embedded in a general-purpose language.*



# Elements

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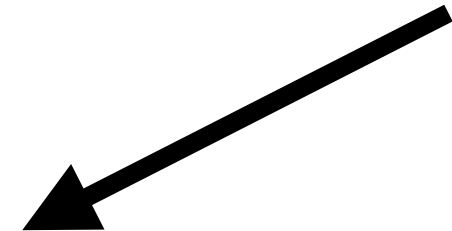
Scala variable



Figaro element



True with  
20% chance



```
val sunnyToday = Flip(0.2)
```

Flip(0.2) is an instance of Element[Boolean].

# Elements

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```
val sunnyToday = Flip(0.2)
```

**Scala:**

**Variable**

**Value**

`sunnyToday`

`Flip(0.2)`

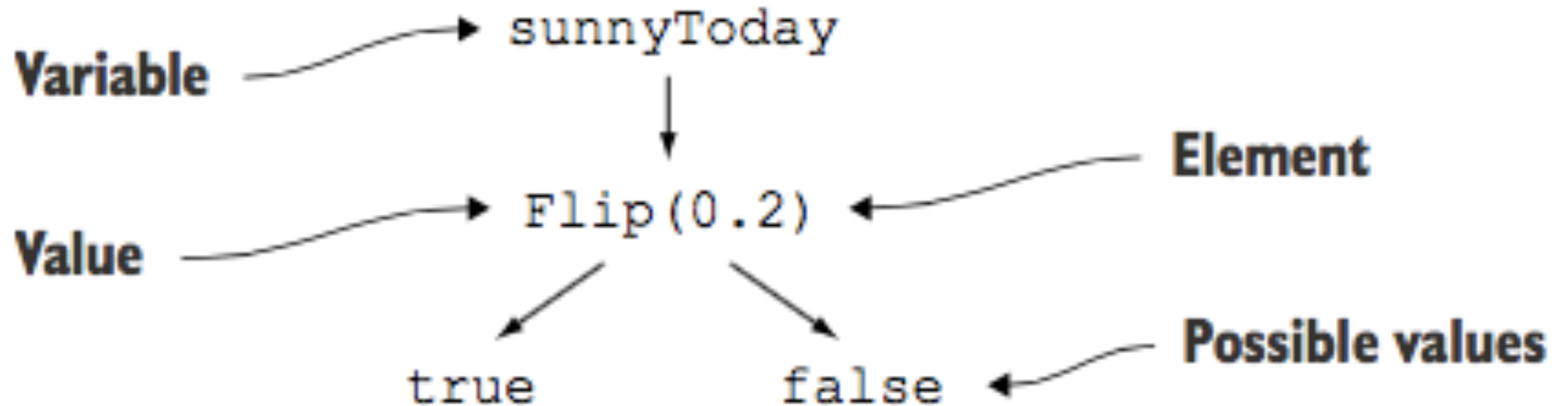
`true`

`false`

**Figaro:**

**Element**

**Possible values**



# Morning greeting application

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Every morning, I wake up, lean out my window, and shout a greeting.

When the weather is good, I usually say, “Hello world!” or “Howdy, universe!”.

When the weather is bad, I’m grumpier. Sometimes I say, “Hello world!”, but sometimes I say, “Oh no, not again.”

Today's weather		
Sunny	0.2	
Not sunny	0.8	
Today's greeting		
If today's weather is sunny	"Hello, world!"	0.6
	"Howdy, universe!"	0.4
If today's weather isn't sunny	"Hello, world!"	0.2
	"Oh no, not again"	0.8
Tomorrow's weather		
If today's weather is sunny	Sunny	0.8
	Not sunny	0.2
If today's weather isn't sunny	Sunny	0.05
	Not sunny	0.95
Tomorrow's greeting		
If tomorrow's weather is sunny	"Hello, world!"	0.6
	"Howdy, universe!"	0.4
If tomorrow's weather isn't sunny	"Hello, world!"	0.2
	"Oh no, not again"	0.8

# Morning greeting application

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Let's see how we would model two days of my morning routine.

There are three tasks that we want our model to be able to do:

1. Predict the greeting today
2. Given an observation of the greeting, infer the weather
3. Learn from an observation of today's greeting in order to predict tomorrow's greeting.

# Elements

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An **element** is a language construct that represents a process that probabilistically produces a value.

The value of an element isn't known until the computation graph is run.

Figaro elements let you specify the probabilistic process used to sample a value more explicitly.



# Probabilistic Programming Languages

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Figaro is one of the newest, most powerful probabilistic programming languages, partly because of its strong interface with Scala.

Older statistical modeling languages:

STAN, BayesianLab

Others include:

Church, WebPPL

# Applications

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Probabilistic programming languages are relatively new (~2000), and we're still figuring out useful applications for them.

## Example applications:

- ♦ evaluating online game players (Microsoft)
- ♦ identifying nuclear test treaty violations (Stuart Russell)
- ♦ identifying malware (Charles River Analytics)
- ♦ modeling language learning and conversation dynamics (lots of folks, including me!)