

Control

CS251 Handout #41
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What is Control?

In program execution, control is characterized by two components:

1. the expression/statement currently being evaluated:

- CS111: the red control dot.
- CS240: the program counter.
- CS251: the argument to `eval` in the substitution model

2. The **continuation** = all pending operations to be performed when the value of current expression is returned:

- CS111: the pending frames in the Java Execution Model.
- CS240: the stack of procedure call activation frames.
- CS251: the context surrounding the current expression in the substitution model

We will call the pair of (1) and (2) a **control point**. All computation is an iteration through control points.

Control Point Example 1

<i>Expression</i>	<i>Continuation</i>
$(/ (+ (* 6 5) (- 7 3)) 2)$	k_{top}
$\Rightarrow (+ (* 6 5) (- 7 3))$	$k_1 = (\lambda (v_1) (k_{top} (/ v_1 2)))$
$\Rightarrow (* 6 5)$	$k_2 = (\lambda (v_2) (k_1 (+ v_2 (- 7 3))))$
$\Rightarrow (- 7 3)$	$k_3 = (\lambda (v_3) (k_1 (+ 30 v_3)))$
$\Rightarrow (+ 30 4)$	k_1
$\Rightarrow (/ 34 2)$	k_{top}
$\Rightarrow 17$	

Notes:

- Continuations are modeled as single-argument functions.
- k_{top} designates the top-level continuation (eg, prints result).
- The above assumes left-to-right evaluation of arguments. (MIT Scheme evaluates them right-to-left.)

Control Point Example 2: Recursive Factorial

```
(def (fact-rec n)
  (if (= n 0)
      1
      (* n (fact-rec (- n 1)))))
```

Expression

\Rightarrow (fact-rec 3)

\Rightarrow (fact-rec 2)

\Rightarrow (fact-rec 1)

\Rightarrow (fact-rec 0)

\Rightarrow (* 1 1)

\Rightarrow (* 2 1)

\Rightarrow (* 3 2)

\Rightarrow 6

Continuation

k_{top}

$k_1 = (\lambda (v_1) (k_{top} (* 3 v_1)))$

$k_2 = (\lambda (v_2) (k_1 (* 2 v_2)))$

$k_3 = (\lambda (v_3) (k_2 (* 1 v_3)))$

k_2

k_1

k_{top}

Control Point Example 3: Iterative Factorial

```
(def (fact-iter n) (fact-tail n 1))  
  
(def (fact-tail num ans)  
  (if (= num 0)  
      ans  
      (fact-tail (- num 1) (* num ans)))))
```

<i>Expression</i>	<i>Continuation</i>
\Rightarrow (fact-iter 3)	k_{top}
\Rightarrow (fact-tail 3 1)	k_{top}
\Rightarrow (fact-tail 2 3)	k_{top}
\Rightarrow (fact-tail 1 6)	k_{top}
\Rightarrow (fact-tail 0 6)	k_{top}
\Rightarrow 6	

Note: A function call is **tail recursive** if it does not alter continuation

Control Aspects of Familiar Constructs

- Evaluating nested subexpressions requires choosing an order and remembering what to do next.
 - Argument evaluation order is left-to-right in most language.
 - Evaluation order unspecified in Scheme (right-to-left in MIT-Scheme).
- Sequencing of statements in imperative language.
- Conditionals allow branches in control flow.
- Loops/tail recursion specify iterations.
- Function/procedure call and return:
 - In many execution models (e.g., C, Pascal, Java), calling a procedure pushes an activation frame on the call stack and returning from a procedure pops the activation from from the call stack.
 - In **properly tail-recursive languages** (e.g. Scheme, most ML implementations) stack is pushed by subexpression evaluation and procedure calls act like gotos that pass arguments (see Guy Steele's *The Expensive Procedure Call Myth or Lambda: The Ultimate Goto*).

Altering the Normal Flow of Control

Sometimes want to alter the normal flow of control:

- to immediately stop execution of the program, due to a user request (typing Control-C) or encountering an error. E.g. halt opcode in assembly language; `error` in HOFL, Scheme;
- to return an answer immediately without processing all pending computations. E.g. encountering a zero when finding the product of elements in a list, array, or tree.
- to handle an unusual situation that may need to be handled differently in different contexts (an exception). E.g., division by zero, out-of-bounds array access, unbound variables in environment lookup.

Altering normal flow of control can be very convenient and efficient, but can lead to “spaghetti code”. Dijkstra’s *Goto Considered Harmful* and the structured programming movement of the 1970s advocated control constructs with one control input and one control output.

Non-local Exits: `return`

In C, C++, and Java, `return` can force early exit of a function/method.

Example (Java): calculating array product. Want to return early if encounter a zero. Also suppose that encountering any negative number should cause the result to be -1.

```
public static int arrayProd (int[] a)
{
    int prod = 1;
    for (int i = 0; i < a.length; i++) {
        if (a[i] == 0)
            return 0;    // Non-local exit from loop
        else if (a[i] < 0) then
            return -1;    // Non-local exit from loop
        else
            prod = a[i] * prod;
    }
    return prod;
}
```


Non-local Exits: break

Java has labeled `break` statements for breaking out of a loop and `continue` statement to jump to end of loop. C's unlabeled `break` and `continue` work on innermost enclosing loop.

```
public static int sumArrayProds (int[][] a)
{
    int sum = 0;
    outer:for (int i = 0; i < a.length; i++) {
        int prod = 1;
        inner:for (int j = 0; i < a[i].length; j++) {
            if (a[i][j] < 0)    // return current sum
                break outer;  // on negative num
            else if (a[i][j] == 0)
                prod = 0; break inner;
            // Alternatively: continue outer;
            else
                prod = a[i][j] * prod;
        }
        sum = sum + prod;
    }
    return sum;
}
```

Non-Local Exits: goto

In Pascal, can only express non-local exits via goto:

```
function product (outer_lst: intlist): integer;
  label 17; {labels are denoted by numbers 0 to 9999}
  function inner (lst: intlist): integer
    begin
      if lst = nil then
        inner := 1
      else if lst^.head = 0 then
        begin
          product := 0; {sets return value of function}
          goto 17; {control jumps to label 17}
        end;
      else
        inner := lst^.head * inner(lst^.tail)
      end;
    end;
begin
  product := inner (outer_lst);
  17: {end of program}
end;
```

Non-Local Exits: `label` and `jump`

We will study non-local exits in Scheme by extending it with the following `label` and `jump` constructs:

- `(label I_{cp} E_{body})` evaluates E_{body} in a lexical environment in which the name I_{cp} is bound to a first-class control point that represents the continuation of the entire `label` expression. `label` returns the value of E_{body} unless `jump` is called on I_{cp} , in which case the value supplied to `jump` is returned.
- `(jump E_{cp} E_{val})` returns the value of E_{val} to the control point that is the value of E_{cp} . `jump` signals an error if E_{cp} is not a control point.

label and jump: Simple Examples

```
(+ 1 (label exit (* 2 (- 3 (/ 4 1)))))
```

```
(+ 1 (label exit (* 2 (- 3 (/ 4 (jump exit 5))))))
```

```
(+ 1 (label exit  
      (* 2 (- 3 (/ 4 (jump exit (+ 5 (jump exit 6))))))))
```

```
(+ 1 (label exit1  
      (* 2 (label exit2  
            (- 3 (/ 4 (+ (jump exit2 5)  
                          (jump exit1 6))))))))
```

label and jump: List Product

```
(define product
  (lambda (outer-list)
    (label return
      (letrec ((inner (lambda (lst)
                        (if (null? lst)
                            1
                            (if (= (car lst) 0)
                                (jump return 0)
                                (* (car lst)
                                   (inner (cdr lst))))))))
        (inner outer-list)))))
```

label and jump: List Product Alternative

```
(define product
  (lambda (outer-list)
    (label return
      (foldr (lambda (x ans)
                (if (= x 0)
                    (jump return 0)
                    (* x ans)))
              1
              outer-list))))
```

Unlike the previous version, a `jump` is performed here on the way out of the recursion rather than on the way in.

Control Points Introduced by `label` are First-Class

```
(define fact
  (lambda (n)
    (let ((loop 'later) ; don't care about initial value
          (ans 1))
      (begin
        (label top (set! loop (lambda ()
                                (jump top 'ignore))))
        (if (= n 0)
            ans
            (begin
              (set! ans (* n ans))
              (set! n (- n 1))
              (loop)))))))
```

First-class Control Points are Strange and Powerful

```
(let ((g (lambda (x) x)))
  (letrec ((fact (lambda (n)
                    (if (= n 0)
                        (label base
                          (begin
                            (set! g (lambda (y)
                                      (begin
                                        (set! g (lambda (z) z))
                                        (jump base y))))))
                        1)))
            (* n (fact (- n 1))))))

(+ (g 1)
  (+ (fact 3) ; Cont. = ( $\lambda (v)$  (+ 1 (+ v ...)))
    (+ (g 10)
      (+ (fact 4) ; Cont. = ( $\lambda (v)$  (+ 1 (+ 60 (+ 10 (+ v ...))))
        (g 100))))))
```


Scheme's `call-with-current-continuation`

Off-the-shelf Scheme does not support `label` and `jump`. But it does support `call-with-current-continuation` (sometimes abbreviated `cwcc`) which encapsulates both `label` and `jump` and can be used to implement many advanced control constructs.

`(call-with-current-continuation E_{proc})`
behaves like:

```
(let ((body-proc  $E_{proc}$ ))  
  (label return  
    (body-proc (lambda (val)  
                  (jump return val))))))
```

Example of call-with-current-continuation

```
(define product
  (lambda (outer-list)
    (call-with-current-continuation
      (lambda (return)
        (letrec
          ((inner (lambda (lst)
                     (cond ((null? lst) 1)
                           ((= 0 (car lst)) (return 0))
                           (else (* (car lst)
                                     (inner (cdr lst))))
                     ))))
          (inner outer-list))))))
```

Continuation Passing Style (CPS)

The constructs we have seen so far rely on implicit continuations. It is possible to model non-local control flow by passing explicit continuations in a style known as **continuation-passing style (CPS)**.

For example, here is a CPS version of recursive factorial:

```
(define fact-rec-cps
  (lambda (n k) ; k is the explicit continuation
    (if (= n 0)
        (k 1)
        (fact-rec-cps (- n 1)
                      (lambda (v) (k (* n v)))))))

(fact-rec-cps 3 (lambda (v) v))

(fact-rec-cps 4 (lambda (v) (+ 1 (* 2 v))))
```

Exception Handling

Want to be able to “signal” exceptional situations and handle them differently in different contexts.

Many languages provide exception systems:

- Java's `throw` and `try/catch`
- OCaml's `raise` and `try/with`
- Common Lisp's `throw` and `catch`

raise, handle, and trap

We study exception handling in Scheme extended with:

- $(\text{raise } I_{tag} E)$ Evaluate E to value V and raise exception with tag I_{tag} and value V .
- $(\text{handle } I_{tag} E_{handler} E_{body})$ First evaluate $E_{handler}$ to a one-argument handler function $V_{handler}$. Then try to evaluate E_{body} to value V_{body} . If no exception is raised, return V_{body} . If an exception is raised with tag I_{tag} and value $V_{exception}$, then the `handle` expression's value is $(V_{handler} V_{body})$ (**termination semantics**).
- $(\text{trap } I_{tag} E_{handler} E_{body})$ is evaluated like $(\text{handle } I_{tag} E_{handler} E_{body})$ except that if an exception is raised with tag I_{tag} and value $V_{exception}$, the call to `raise` returns with the value of the application $(V_{handler} V_{body})$ (**resumption semantics**).

`handle/trap` effectively bind $V_{handler}$ in a *dynamically scoped* exception handler namespace, and $(\text{raise } I_{tag} E)$ looks up I_{tag} in this namespace.

Exception Handling Examples 1

```
(define test
  (lambda ()
    (let ((raiser (lambda (x)
                     (if (< x 0)
                         (raise negative x)
                         (if (even? x)
                             (raise even x)
                             x))))))
      (+ (raiser 1) (+ (raiser -3) (raiser 4))))))
```

What is the value of the following, where *handler_1* and *handler_2* range over {*handle*, *trap*}? First assume left-to-right argument evaluation, then right-to-left.

```
(handler_1 negative (lambda (v) (- v)))
(handler_2 even (lambda (v) (* v v)))
(test))
```

Exception Handling Examples 2

What are the value of the following expressions, where *handler* ranges over {*handle*, *trap*}?

; Expression 1

```
(handler a (lambda (x) (+ 4000 x)))  
  (handler b (lambda (x) (+ 300 (raise a (+ x 4)))))  
    (handler a (lambda (x) (+ 20 x)))  
      (+ 1 (raise b 2))))
```

; Expression 2

```
(handler c (lambda (x) (* x 10)))  
  (+ 1 (raise c (+ 2 (raise c 4)))))
```

Exception Handling In OCaml

OCaml's `raise` and `try/with` uses termination semantics.

In `raise E`, E must evaluate to an exception packet created by an exception constructor (where exceptions are effectively an extensible datatype).

`try Ebody with clauses` evaluates E_{body} and returns its value unless an exception is raised, in which case the matching clause in *clauses* is evaluated and its value is returned as the value of `try`.

OCaml Exception Example

```
exception Neg of int
exception Even of int

let raiser x =
  if x < 0 then
    raise (Neg x)
  else if (x mod 2) = 0 then
    raise (Even x)
  else
    x

let test () = (raiser 1) + (raiser -3) + (raiser 4)

let innerTest () = try test() with
  Neg y -> raiser(7 + -y)
  | Even z -> 3 * z

let outerTest () = try innerTest() with
  Neg y -> -y
  | Even z -> z * z
```

Can translate this example into Java using `throw` and `try/catch`.

Implementing raise

$(\text{raise } I_{tag} E) \rightsquigarrow (\text{raise-tag } 'I_{tag} E)$

```
(define raise-tag
  (lambda (tag value)
    (let ((handler
          ;; Look up handler in current handler env.
          ;; Handlers are dynamically scoped!
          (env-lookup tag (get-handler-env))))
      (if (unbound? handler)
          (error (string-append "Unhandled exception "
                                (symbol->string tag)
                                ": "))
          (handler value)))))
```

Implementing handle and trap 1

```
(define with-handler
  (lambda (tag make-handler try-thunk)
    (begin
      (let ((old-env (get-handler-env)))
        (begin
          ;; Remember handler in dynamic environment
          (set-handler-env! (env-bind tag
                                      (make-handler old-env)
                                      (get-handler-env)))

          ;; Evaluate try-thunk
          (let ((try-value (try-thunk)))
            ;; In normal case, pop handler
            (begin
              (set-handler-env! old-env) ; reinstate old handler env.
              try-value))))))))) ; Return value
```

Implementing handle and trap 2

(trap tag handler body) desugars to

```
(let ((*handler* handler) ; only evaluate once
      (*thunk* (lambda () body))) ; avoid capturing *handler*
    (with-handler 'tag
      (lambda (old-env)
        (lambda (value) (*handler* value))) ; ignores old-env
      *thunk*)))
```

(handle tag handler body) desugars to

```
(let ((*handler* handler) ; only evaluate once
      (*thunk* (lambda () body))) ; avoid capturing *handler*
    (call-with-current-continuation
      (lambda (handle-cont)
        (with-handler 'tag
          (lambda (old-env)
            (lambda (value)
              ;; Invoking HANDLE-CONT returns directly to
              ;; appropriate handle, ignoring current continuation.
              (begin
                (set-handler-env! old-env) ; reinstall old-env
                (handle-cont (*handler* value))))))
          *thunk*))))))
```