

List Processing in OCAML

Given a list of integers ns , suppose we want to return a new list of the same length in which each element is one more than the corresponding element of ns . Here's one way to express this in Java (using the `IntList` class you've seen in CS111 and CS230).

```
public static IntList incList (IntList ns)
{
    if (IntList.isEmpty(ns))
        return IntList.empty();
    else
        return IntList.prepend(1 + IntList.head(ns), incList(IntList.tails(ns)));
}
```

What are the corresponding list manipulation operators in OCAML?

Java	OCAML
<code>empty()</code>	<code>[]</code>
<code>prepend(x,ys)</code>	<code>x::ys</code>
<code>head(xs)</code>	<code>List.hd(xs)</code>
<code>tail(xs)</code>	<code>List.tl(xs)</code>
<code>isEmpty(xs)</code>	<code>xs = []</code>

Also, in OCAML, one can write $[E_1;E_2;\dots;E_n]$ as an abbreviation for $E_1::E_2::\dots::E_n::[]$.

Here is an OCAML transliteration of the Java `incList` given above:

```
let rec incList ns =
  if ns = [] then
    []
  else
    (1 + List.hd(ns)) :: (incList (List.tl ns))
```

However, in practice, `List.hd` and `List.tl` are rarely used to process lists in OCAML. Instead, one normally uses the powerful pattern matching facilities OCAML provides:

```
let rec incList ns =
  match ns with
  [] -> []
  | (n::ns') -> (n+1)::(incList ns')
```

Here is a contrived example of pattern matching:

```
let rec process ps =
  match ps with
  [(c,d);(e,f)] -> [(d,f);(c,e)]
  | (p1::p2::p3::ps') -> (p3::p1::p2::ps')
  | _ -> ps

# process [];;
- : ('a * 'a) list = []
```

```

# process [(1,2)];;
- : (int * int) list = [(1, 2)]

# process [(1,2);(3,4)];;
- : (int * int) list = [(2, 4); (1, 3)]

# process [(1,2);(3,4);(5,6)];;
- : (int * int) list = [(5, 6); (1, 2); (3, 4)]

# process [(1,2);(3,4);(5,6);(7,8)];;
- : (int * int) list = [(5, 6); (1, 2); (3, 4); (7, 8)]

```

Patterns cannot contain duplicates, but can have **when** guards:

```

let condswap xs =
  match xs with
    x1::x2::x3::xs' when x1 = x3 -> x2 :: x1 :: x3 :: xs'
  | _ -> xs;;

# condswap [1;2;1;4];;
- : int list = [2; 1; 1; 4]

# condswap [1;2;3;4];;
- : int list = [1; 2; 3; 4]

```

Subpatterns can be named by **as** patterns:

```

let condswap xs =
  match xs with
    x1::x2::((x3::_) as xs'') when x1 = x3 -> x2 :: x1 :: xs''
  | _ -> xs;;
val condswap : 'a list -> 'a list = <fun>

```

In class, we will write the following functions:

```
val sum : int list -> int
```

`sum ns` returns the sum of all the integers in a list of integers *ns*.

```
# sum [];;  
- : int = 0  
# sum [3];;  
- : int = 3  
# sum [3;2;7;5];;  
- : int = 17
```

```
val range : int -> int -> int list
```

`range lo hi` returns a list of integers from *lo* up to *hi*, inclusive. The list is empty if *lo* > *hi*.

```
# range 3 7;;  
- : int list = [3; 4; 5; 6; 7]  
# range 5 5;;  
- : int list = [5]  
# range 6 5;;  
- : int list = []
```

val isMember : 'a * 'a list -> bool

isMember(x,ys) returns true if x is an element of the list ys (as determined by =) and false otherwise.

```
# isMember(3,[5;2;3;1;4]);;
- : bool = true
# isMember(6,[5;2;3;1;4]);;
- : bool = false
# isMember("be",["to";"be";"or";"not";"to";"be"]);;
- : bool = true
# isMember("two",["to";"be";"or";"not";"to";"be"]);;
- : bool = false
# isMember((2,"two"), [(3,"three");(1,"one");(2,"two");(4,"four")]);;
- : bool = true
# isMember((2,"too"), [(3,"three");(1,"one");(2,"two");(4,"four")]);;
- : bool = false
```

val removeDups : 'a list -> 'a list

removeDups xs returns a list containing one occurrence of each element in xs. The order of elements in the returned list is unspecified.

```
# removeDups [5;4;5;3;4;2;3;4;5;1;3;5;4;2;5];;
- : int list = [1; 3; 4; 2; 5] (* order doesn't matter *)
# removeDups ["do";"be";"do";"be";"do"];;
- : string list = ["be"; "do"] (* order doesn't matter *)
# removeDups ['a';'b';'r';'a';'c';'a';'d';'a';'b';'r';'a'];;
- : char list = ['c'; 'd'; 'b'; 'r'; 'a'] (* order doesn't matter *)
# removeDups [];;
- : 'a list = []
```

val isSorted : 'a list -> bool
isSorted xs returns true if the list xs is sorted from low to high according to <=, and false otherwise.

```
# isSorted [];;
- : bool = true
# isSorted [3];;
- : bool = true
# isSorted [3;1;4;2];;
- : bool = false
# isSorted [1;2;3;4];;
- : bool = true
# isSorted [false;true];;
- : bool = true
# isSorted [true;false];;
- : bool = false
# isSorted ['a';'b';'c'];;
- : bool = true
# isSorted ['c';'a';'b'];;
- : bool = false
# isSorted ["one";"two";"three"];;
- : bool = false
# isSorted ["one";"three";"two"];;
- : bool = true
# isSorted [(1,"bar");(2,"baz");(3,"foo")];;
- : bool = true
# isSorted [(1,"bar");(3,"baz");(2,"foo")];;
- : bool = false
# isSorted [(1,"foo");(2,"bar");(3,"baz")];;
- : bool = true
# isSorted [[];[1];[1;2];[1;3;2];[1;3;4];[1;4];[2]];;
- : bool = true
# isSorted [[];[1];[1;2;3];[1;2];[1;3;4];[1;4];[2]];;
- : bool = false
```

```
val squares : int list -> int list
```

`squares ns` returns a list of the squares of the corresponding integers in the list *ns*.

```
# squares [3;1;5;4;2];;  
- : int list = [9; 1; 25; 16; 4]  
# squares [3];;  
- : int list = [9]  
# squares [];;  
- : int list = []
```

```
val evens : int list -> int list
```

`evens ns` returns a list of the even integers in the list *ns* in the same relative order that they appear in *ns*.

```
# evens [3;1;4;2;5;8;9;6];;  
- : int list = [4; 2; 8; 6]  
# evens [3;1;5;9];;  
- : int list = []  
# evens [6;256;100];;  
- : int list = [6; 256; 100]  
# evens [];;  
- : int list = []
```

```
val flatten : 'a list list -> 'a list
```

`flatten xss` returns a list containing all of the elements of the lists in the list of list `xss` in the same order. Use the infix `@` operator or prefix `List.append` operator to append two lists. Note that OCAML provides `flatten` via `List.flatten`.

```
# flatten [[4;2];[3;1;5;8];[7];[6;0;9]];;
- : int list = [4; 2; 3; 1; 5; 8; 7; 6; 0; 9]
# flatten [["foo"];["bar";"baz"];["quux"]];;
- : string list = ["foo"; "bar"; "baz"; "quux"]
# flatten [["foo"]];;
- : string list = ["foo"]
# flatten [];;
- : 'a list = []
```

```
val reverse : 'a list -> 'a list
```

`reverse xs` returns a list containing the elements of the list `xs` in reverse order. Note that OCAML provides this function via `List.rev`.

```
# reverse [3;1;5;4;2];;
- : int list = [2; 4; 5; 1; 3]
# reverse ["foo";"bar";"baz"];;
- : string list = ["baz"; "bar"; "foo"]
# reverse ["foo"];;
- : string list = ["foo"]
# reverse [];;
- : 'a list = []
```

`val zip : 'a list * 'b list -> ('a * 'b) list`

`zip (xs,ys)` returns a list of pairs containing the corresponding elements of the lists `xs` and `ys`.

The length of the resulting list is the length of the shorter of `xs` and `ys`.

```
# zip ([1;2;3],[ 'a'; 'b'; 'c']);;  
- : (int * char) list = [(1, 'a'); (2, 'b'); (3, 'c')]  
# zip ([1;2;3;4;5],[ 'a'; 'b'; 'c']);;  
- : (int * char) list = [(1, 'a'); (2, 'b'); (3, 'c')]  
# zip ([1;2;3],[ 'a'; 'b'; 'c'; 'd'; 'e']);;  
- : (int * char) list = [(1, 'a'); (2, 'b'); (3, 'c')]  
# zip ([],[ 'a'; 'b'; 'c']);;  
- : ('a * char) list = []  
# zip ([1;2;3],[]);;  
- : (int * 'a) list = []
```

`val unzip : ('a * 'b) list -> 'a list * 'b list`

`unzip ps` takes a list of pairs `ps` and returns a pair of lists, the first of which contains all the first components of `ps`, and the second of which contains all the second components of `ps`.

```
# unzip [(1, 'a'); (2, 'b'); (3, 'c')];;  
- : int list * char list = ([1; 2; 3], [ 'a'; 'b'; 'c'])  
# unzip [(2, 'b')];;  
- : int list * char list = ([2], [ 'b'])  
# unzip [];;  
- : 'a list * 'b list = ([], [])
```

```
val mapcons : 'a * 'a list list -> 'a list list
```

`mapcons (x,zss)` returns a list containing the result of prepending `x` to each list in the list of lists `zss`.

```
# mapcons (5,[[4;1];[3];[2;1;3];[]]);;
- : int list list = [[5; 4; 1]; [5; 3]; [5; 2; 1; 3]; [5]]
# mapcons ("foo", [[]]);;
- : string list list = [["foo"]]
# mapcons ("foo", []);;
- : string list list = []
```

```
val subsets : 'a list -> 'a list list
```

Assume that `xs` is a list without duplicates, and thus represents a set of elements. `subsets xs` returns a list of lists containing all subsets of `xs`. The elements of each subset must appear in the same relative order as in `xs`, but the order of the subsets themselves is unspecified. *Hint:* `mapcons` is helpful here.

```
# subsets [];;
- : 'a list list = [[]]
# subsets [4];;
- : int list list = [[]; [4]]
# subsets [3;4];;
- : int list list = [[]; [4]; [3]; [3; 4]]
# subsets [2;3;4];;
- : int list list = [[]; [4]; [3]; [3; 4]; [2]; [2; 4]; [2; 3]; [2; 3; 4]]
# subsets [1;2;3;4];;
- : int list list =
[[]; [4]; [3]; [3; 4]; [2]; [2; 4]; [2; 3]; [2; 3; 4];
 [1]; [1; 4]; [1; 3]; [1; 3; 4]; [1; 2]; [1; 2; 4]; [1; 2; 3]; [1; 2; 3; 4]]
# subsets ['a';'b';'c';'d'];;
- : char list list =
[[]; ['d']; ['c']; ['c'; 'd']; ['b']; ['b'; 'd']; ['b'; 'c'];
 ['b'; 'c'; 'd']; ['a']; ['a'; 'd']; ['a'; 'c']; ['a'; 'c'; 'd']; ['a'; 'b'];
 ['a'; 'b'; 'd']; ['a'; 'b'; 'c']; ['a'; 'b'; 'c'; 'd']]
```

```
val decimal : int list -> int
```

Assume that *bs* is a list of zeroes and ones. `decimal bs` returns an integer that is the decimal representation of the number represented in binary by *bs*.

```
# decimal [0];;
- : int = 0
# decimal [1];;
- : int = 1
# decimal [1;0];;
- : int = 2
# decimal [1;0;0];;
- : int = 4
# decimal [1;0;1];;
- : int = 5
# decimal [1;0;1;0];;
- : int = 10
# decimal [1;0;1;1];;
- : int = 11
# decimal [1;0;1;1;0];;
- : int = 22
# decimal [1;0;1;1;1];;
- : int = 23
# decimal [1;0;1;1;1;0];;
- : int = 46
```