



## Derivation Exercise

How to execute the Racket factorial program given these parts?

- factorial-in-Racket program
- Racket-to-Python-translator-in-Python program
- Python-interpreter-in-C program
- C-to-x86-translator-in-x86 program
- x86 computer (i.e., x86 interpreter machine)

**Warning: cannot start the following way:**

- factorial machine (I)
  - factorial-in-Racket program
  - Racket interpreter machine (I)
  - ....

**Why not?**

**The derivation would need to begin:**

- factorial machine (I)
  - factorial-in-Racket program
  - Racket interpreter machine (I)
    - Racket-interpreter-in-L program
    - ...
    - L interpreter machine
    - ...



**But the parts don't include Racket-interpreter-in-L program for any L!**

**What to do? Explore translating the factorial-in-Racket program to a factorial-in-L program for some L for which we \*can\* make an interpreter machine!**



## Derivation Exercise: Solution

How to execute the Racket factorial program given these parts?

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- Racket-to-Python-translator-in-Python program
- Python-interpreter-in-C program
- C-to-x86-translator-in-x86 program
- x86 computer (i.e., x86 interpreter machine)

**SOLUTION:**

- factorial machine (I)
  - factorial-in-Python program (T)
    - ◇ factorial-in-Racket program
    - ◇ Racket-to-Python translation machine (I)
      - Racket-to-Python-translator-in-Python program
      - Python interpreter machine (I)
        - ◆ Python-interpreter-in-x86 program (T)
          - Python-interpreter-in-C program
          - C-to-x86-translator machine (I)
            - C-to-x86-translator-in-x86 program
            - x86 computer (= x86 interpreter machine)
        - ◆ x86 computer (= x86 interpreter machine)
  - Python interpreter machine (I)
    - # Derivation already given above; no need to rederive it!
    - # A reused derivation is a lemma, which corresponds to
    - # a helper function in programming