

Big Ideas for CS 251

Theory of Programming Languages

Principles of Programming Languages

SOLUTIONS



CS251 Programming Languages
Spring 2019, Lyn Turbak

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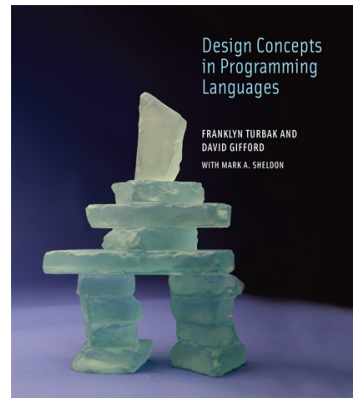
Programming Languages

- What is a PL?
- Why are new PLs created?
 - What are they used for?
 - Why are there so many?
- Why are certain PLs popular?
- What goes into the design of a PL?
 - What features must/should it contain?
 - What are the design dimensions?
 - What are design decisions that must be made?
- Why should you take this course? What will you learn?

Big ideas 2

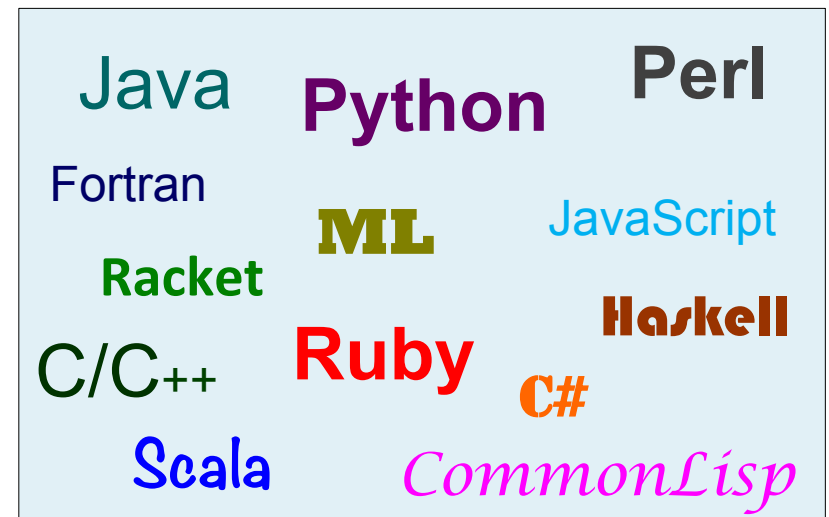
PL is my passion!

- First PL project in 1982 as intern at Xerox PARC
- Created visual PL for 1986 MIT masters thesis
- 1994 MIT PhD on PL feature (synchronized lazy aggregates)
- 1996 – 2006: worked on types as member of Church project
- 1988 – 2008: *Design Concepts in Programming Languages*
- 2011 – current: lead TinkerBlocks research team at Wellesley
- 2012 – current: member of App Inventor development team



Big ideas 3

General Purpose PLs



Big ideas 4

Domain Specific PLs (DSLs)



Big ideas 5

Programming Languages: Mechanical View

A computer is a machine. Our aim is to make the machine perform some specified actions. With some machines we might express our intentions by depressing keys, pushing buttons, rotating knobs, etc. For a computer, we construct a sequence of instructions (this is a "program") and present this sequence to the machine.

– Laurence Atkinson, *Pascal Programming*

Big ideas 6

Programming Languages: Linguistic View

A computer language ... is a novel formal medium for expressing ideas about methodology, not just a way to get a computer to perform operations. Programs are written for people to read, and only incidentally for machines to execute.

– Harold Abelson and Gerald J. Sussman

Big ideas 7

“Religious” Views

The use of COBOL cripples the mind; its teaching should, therefore, be regarded as a criminal offense. – Edsger Dijkstra

It is practically impossible to teach good programming to students that have had a prior exposure to BASIC: as potential programmers they are mentally mutilated beyond hope of regeneration. – Edsger Dijkstra

You're introducing your students to programming in C? You might as well give them a frontal lobotomy! – A colleague of mine

A LISP programmer knows the value of everything, but the cost of nothing. – Alan Perlis

I have never met a student who cut their teeth in any of these languages and did not come away profoundly damaged and unable to cope. ... I mean this reads to me very similarly to teaching someone to be a carpenter by starting them off with plastic toy tools and telling them to go sculpt sand on the beach. – John Haugeland, *on blocks languages*

A language that doesn't affect the way you think about programming, is not worth knowing. – Alan Perlis

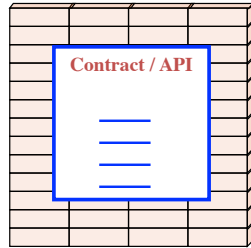
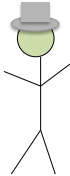
Big ideas 8

Which Programming/PL Hat do You Wear?



CS111 Big idea #1: Abstraction

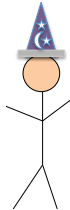
Function & Data Abstraction
User / Client



Function & Data Abstraction
Implementer



Programming Language
Designer



Big ideas 9

Programming Paradigms

- **Imperative** (e.g. C, Python): Computation is step-by-step execution on a stateful abstract machine involving memory slots and mutable data structures.
 - **Functional, function-oriented** (e.g. Racket, ML, Haskell): Computation is expressed by composing functions that manipulate immutable data.
 - **Object-oriented** (e.g. Simula, Smalltalk, Java): Computation is expressed in terms of stateful objects that communicate by passing messages to one another.
 - **Logic-oriented** (e.g. Prolog): Computation is expressed in terms of declarative relationships.
- Note:** In practice, most PLs involve multiple paradigms. E.g.
- Python supports functional features (map, filter, list comprehensions) and objects
 - Racket and ML have imperative features.

Big ideas 10

Paradigm Example: Quicksort

```
void qsort(int a[], int lo, int hi) {
    int h, l, p, t;

    if (lo < hi) {
        l = lo;
        h = hi;
        p = a[hi];

        do {
            while ((l < h) && (a[l] <= p))
                l = l+1;
            while ((h > l) && (a[h] >= p))
                h = h-1;
            if (l < h) {
                t = a[l];
                a[l] = a[h];
                a[h] = t;
            }
        } while (l < h);

        a[hi] = a[l];
        a[l] = p;

        qsort(a, lo, l-1);
        qsort(a, l+1, hi);
    }
}
```

```
quicksort :: Ord a => [a] -> [a]
quicksort [] = []
quicksort (p:xs) =
    (quicksort lesser)
    ++ [p]
    ++ (quicksort greater)
  where
    lesser = filter (< p) xs
    greater = filter (>= p) xs
```



Functional Style (in Haskell)



Imperative Style
(in C; Java would be similar)

Big ideas 11

PL Dimensions

PLs differ based on decisions language designers make in many dimensions. E.g.:

- **First-class values:** what values can be named, passed as arguments to functions, returned as values from functions, stored in data structures. Which of these are first-class in your favorite PL: arrays, functions, variables?
- **Naming:** Do variables/parameters name expressions, the values resulting from evaluating expressions, or mutable slots holding the values from evaluating expressions? How are names declared and referenced? What determines their scope?
- **State:** What is mutable and immutable; i.e., what entities in the language (variables, data structures, objects) can change over time.
- **Control:** What constructs are there for control flow in the language, e.g. conditionals, loops, non-local exits, exception handling, continuations?
- **Data:** What kinds of data structures are supported in the language, including products (arrays, tuples, records, dictionaries), sums (options, oneofs, variants), sum-of-products, and objects.
- **Types:** Are programs statically or dynamically typed? What types are expressible?

Big ideas 12

Why study PL?

- Crossroads of CS
- Approach problems as a *language designer*.
 - “A good programming language is a conceptual universe for thinking about programming” -- Alan Perlis
 - Evaluate, compare, and choose languages
 - Become better at learning new languages
 - Become a better programmer by leveraging powerful features (first-class functions, tree recursion, sum-of-product datatypes, pattern matching)
 - You probably won’t design a general-purpose PL, but might design a DSL
 - view API design as language design
- Ask:
 - Why are PLs the way they are?
 - How could they (or couldn’t they) be better?
 - What is the cost-convenience trade-off for feature X?

Big ideas 13

Administrivia

- Schedule, psets, quizzes, lateness policy, etc.: see <http://cs.wellesley.edu/~cs251/>.
- Do (most of) PS0 tonight
 - Fill out “get to know you” Introze introduction.
 - Review course syllabus and policies (we’ll go over these tomorrow)
 - Read Wed slides on “big-step semantics” of Racket
 - Install Dr. Racket
- PS1 is available; due next Friday. Start it this week!
- Credit/non is a **bad idea** for 251. Talk to me first!
- Visit me in office hours before next Friday!

Big ideas 14

PL Parts

Syntax: *form* of a PL

- What a P in a given L look like as symbols?
- Concrete syntax vs abstract syntax trees (ASTs)

Semantics: *meaning* of a PL

- *Dynamic Semantics*: What is the behavior of P? What actions does it perform? What values does it produce?
 - Evaluation rules: what is the result or effect of evaluating each language fragment and how are these composed?
- *Static Semantics*: What can we tell about P before running it?
 - Scope rules: to which declaration does a variable reference refer?
 - Type rules: which programs are well-typed (and therefore legal)?

Pragmatics: *implementation* of a PL (and PL environment)

- How can we evaluate programs in the language on a computer?
- How can we optimize the performance of program execution?

Big ideas 15

Syntax (Form) vs. Semantics (Meaning) in Natural Language

Furiously sleep ideas green colorless.

Colorless green ideas sleep furiously.

Little white rabbits sleep soundly.

Big ideas 16

Concrete Syntax: Absolute Value Function

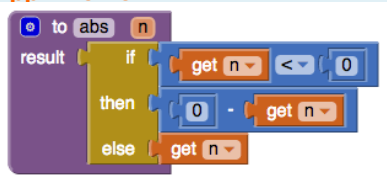
Logo: to abs :n ifelse :n < 0 [output (0 - :n)] [output :n] end

Javascript: function abs (n) {if (n < 0) return -n; else return n;}

Java: public static int abs (int n) {if (n < 0) return -n; else return n;}

Python:
 def abs(n):
 if n < 0:
 return -n
 else:
 return n

App Inventor:



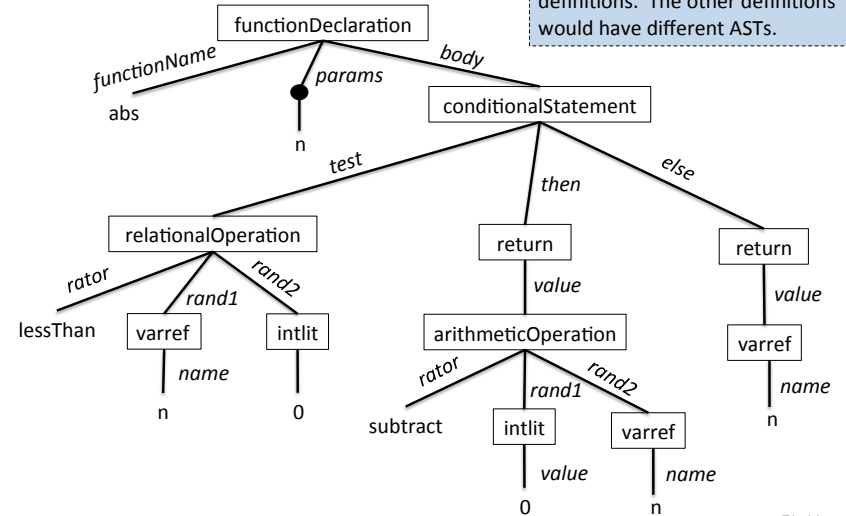
Scheme/Racket: (define abs (lambda (n) (if (< n 0) (- n) n)))

PostScript: /abs {dup 0 lt {0 swap sub} if} def

Big ideas 17

Abstract Syntax Tree (AST): Absolute Value Function

This AST abstracts over the concrete syntax for the Logo, JavaScript, and Python definitions. The other definitions would have different ASTs.



Big ideas 18

Dynamic Semantics Example 1

What is the meaning of the following expression?

$(1 + 11) * 10$

Some possible answers:

- 120 (regular interpretation of numbers, operators)
- 1000 (binary numbers, regular operators)
- 0 (“+” means “minus”, “*” means “plus”)
- 111...1 (30 1s; “+” means “convert to string and concatenate”; * means “repeated concatenation”)
- 13 (number of characters in string)
- 5 (number of nodes in AST)
- 3 (number of leaves in AST)

Big ideas 19

Dynamic Semantics Example 2

What is printed by the following program?

```
a = 1;
b = a + 20;
print(b);
a = 300
print(b);
count = 0;

fun inc() { count = count + 1; return count; }
fun dbl(ignore, x) { return x + x; }
print(dbl(inc(), inc()))
```

Here are some possible answers. What execution models give rise to these answers?

21	21	21	21
21	21	320	320
4	2	3	2

Big ideas 20

Semantics Example 3 Solutions

Suppose `a` is an array (or list) containing the three integer values 10, 20, and 30 in the following languages. What is the meaning of the following expressions/statements in various languages (the syntax might differ from what's shown).

	<code>a[1]</code>	<code>a[3]</code>	<code>a[2] = "foo"</code>	<code>a[3] = 17</code>
Java	20	dynamic index out of bounds error	static type error	dynamic index out of bounds error
C	20	returns value in memory slot after <code>a[2]</code>	static type error	Stores 17 in memory slot after <code>a[2]</code>
Python	20	dynamic list index out of range error	stores "foo" in third slot of <code>a</code>	dynamic list index out of range error
JavaScript	20	"undefined" value	stores "foo" in third slot of <code>a</code>	Stores 17 in <code>a[3]</code>
Pascal	20	static index out of bounds error	static type error	static index out of bounds error
App Inventor	10	30	stores "foo" in second slot of <code>a</code>	Stores 17 in third slot of <code>a</code>

How do you determine the answers? **Try in implementation; consult documentation**

Big ideas 21

Static Semantics Example 1: Type Checking Solutions

Which of the following Java examples can be well-typed (i.e., pass the type checker)? How do you know? What assumptions are you making?

Green indicates statically well-typed; Red indicates static type error.

A `2 * (3 + 4)`

B `2 < (3 + 4)`

C `2 < True`

D Assume `a,b,c` are ints
`if (a < b) {`
`c = a + b;`
`}`
`else {`
`c = a * b;`
`}`

E Assume `a,b` are ints; can't find type for `c`
`if (a < b) {`
`c = a + b;`
`}`
`else {`
`c = a > b;`
`}`

F A can't both be bool for test and int for +/*
`if (a) {`
`c = a + b;`
`}`
`else {`
`c = a * b;`
`}`

G `public boolean f(int i, boolean b) {`
`return b && (i > 0);`
`}`

H `public int g(int i, boolean b) {`
`return i * (b ? 1 : -1);`
`}`

I `public int p(int w) {`
`if (w > 0) { return 2*w; }`
`}` No else clause, so no return of in when `w <= 0`

J Return type needs to be boolean, not int
`public int q(int x) { return x > 0; }`

K Assume `g` has type from above: `g : (int, boolean) -> int`
`public int r(int y) { return g(y, y>0); }`

L If `f` has type `(int, boolean) -> boolean`, not well-typed; But *would* be well typed if `f : (int) -> boolean`
`public boolean s(int z) { return f(z); }`

Big ideas 22

Static Semantics Example 2: Detecting Loops Solutions

Which of these Python programs has inputs for which it loops forever?

```
def f(x):
    return x+1
No ∞ loop on any input
```

```
def g(x):
    while True:
        pass
    return x
∞ loop on all inputs
```

```
def h(x):
    while x > 0:
        x = x+1
    return x
No ∞ loop for x <= 0.
∞ loop for x > 0, assuming arbitrarily large numbers.
In practice, will either run out of memory when x gets too big, or will wrap to negative and halt.
```

```
def g2(x):
    return g2(x)
∞ recursion on all inputs.
In practice, runs out of stack space in Python. Similar Racket program is true ∞ loop due to proper tail recursion.
```

```
def h2(x):
    if x <= 0:
        return x
    else:
        return h2(x+1)
No ∞ loop for x <= 0.
∞ recursion for x > 0.
In practice, runs out of stack space in Python. Similar Racket program will loop, but run out memory when x gets too big.
```



```
def collatz(x):
    while x != 1:
        if (x % 2) == 0:
            x = x/2
        else:
            x = 3*x + 1
    return 1
Although this terminates for all x > 0 that have been tested, no one knows the answer for all x. This a famous open problem in mathematics. Solve it and win a Fields medal!
```

Big ideas 23

Static Semantics and Uncomputability

It is generally **impossible** to answer any interesting question about static program analysis!

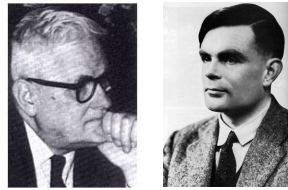
This is a consequence of **Rice's Theorem** (see CS235).

For example, will this program ever:

- halt on certain inputs
- encounter an array index out of bounds error?
- throw a `NullPointerException`?
- access a given object again?
- send sensitive information over the network?
- divide by 0?
- run out of memory, starting with a given amount available?
- try to treat an integer as an array?

Big ideas 24

The Church-Turing Thesis and Turing-Completeness



- **Church-Turing Thesis:** Computability is the common spirit embodied by this collection of formalisms.
- This thesis is a claim that is widely believed about the intuitive notions of **algorithm** and **effective computation**. It is not a theorem that can be proved.
- Because of their similarity to later computer hardware, Turing machines (CS235) have become the gold standard for effectively computable.
- We'll see in CS251 that Church's lambda-calculus formalism is the foundation of modern programming languages.
- A consequence: programming languages all have the "same" computational "power" in term of what they can express. All such languages are said to be **Turing-complete**.

Big ideas 25

Expressiveness and Power

- About:
 - ease
 - elegance
 - clarity
 - modularity
 - abstraction
 - ...
- Not about: computability
- Different problems, different languages
 - Facebook or web browser in assembly language?

Big ideas 26

Pragmatics: Raffle App In App Inventor

<http://ai2.appinventor.mit.edu>

The screenshot shows the App Inventor web interface. On the left is the 'Designer Window' showing a mobile app preview with a 'Pick Winner' button. On the right is the 'Blocks Editor' with two event-driven code blocks. The first block is 'when Texting1.MessageReceived' with sub-blocks for 'number', 'messageText', 'do', 'add items to list', 'list', 'get global numbers', and 'item'. The second block is 'when Button1.Click' with sub-blocks for 'do', 'set PhoneCall1.PhoneNumber to', 'pick a random item list', 'get global numbers', and 'call PhoneCall1.MakePhoneCall'. Below the blocks editor are two text boxes: a yellow one with the text 'To enter the raffle, text me now with an empty message: 339-225-0287' and a red one with the text 'How hard is this to do in more traditional development environments for Android/iOS?'. At the bottom left, there is a 'Non-visible components' list containing 'PhoneCall1' and 'Texting1'.

Big ideas 27

Pragmatics: Metaprogramming

PLs are implemented in terms of **metaprograms** = programs that manipulate other programs.

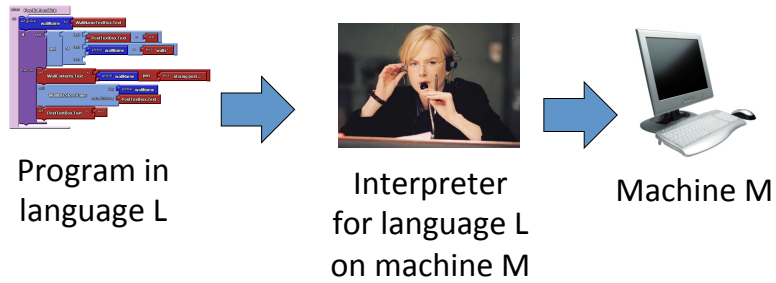
This may sound weird, but programs are just trees (ASTs), so a metaprogram is just a program that manipulates trees (think a more complex version of CS230 binary tree programs).

Implementation strategies:

- **Interpretation:** interpret a program P in a source language S in terms of an implementation language I.
- **Translation (compilation):** translate a program P in a source language S to a program P' in a target language T using a translator written in implementation language I.
- **Embedding:** express program P in source language S in terms of data structures and functions in implementation language I.

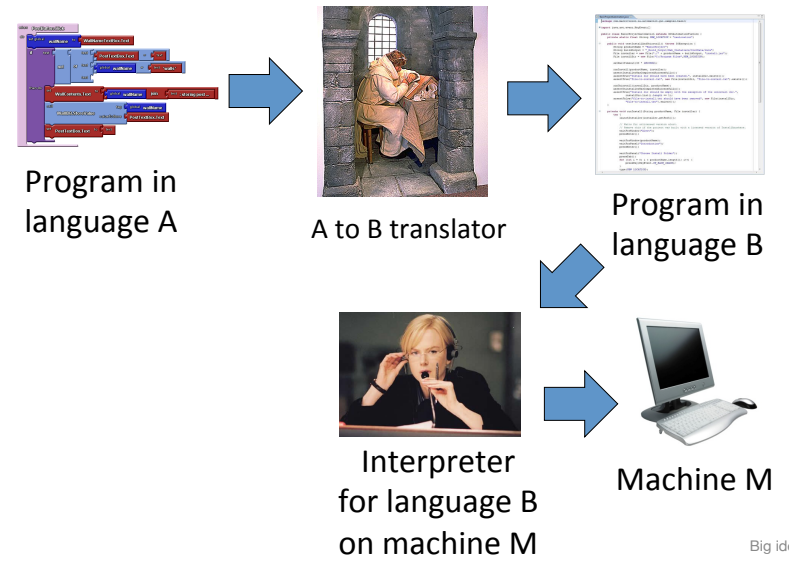
Big ideas 28

Metaprogramming: Interpretation



Big ideas 29

Metaprogramming: Translation



Big ideas 30

Metaprogramming: Bootstrapping Puzzles

How can a Racket interpreter be written in Racket?

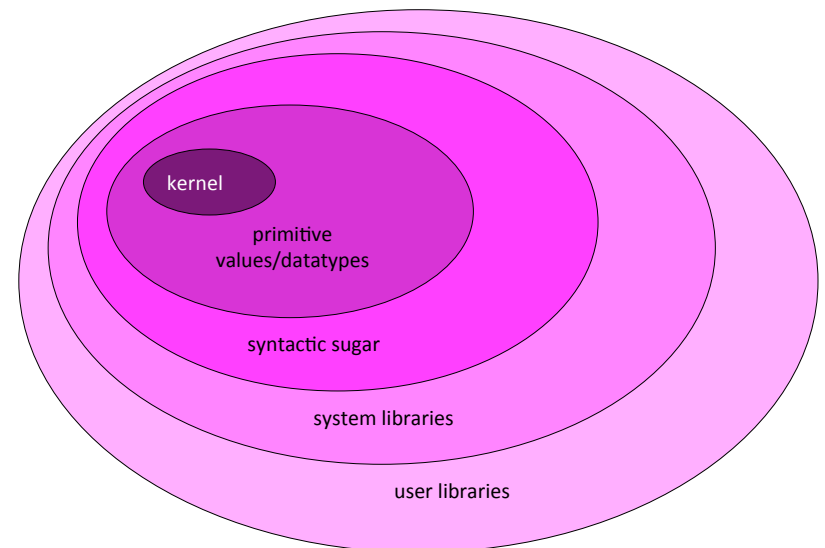
How can a Java compiler be written in Java?

How can gcc (a C-to-x86 compiler) be written in C?



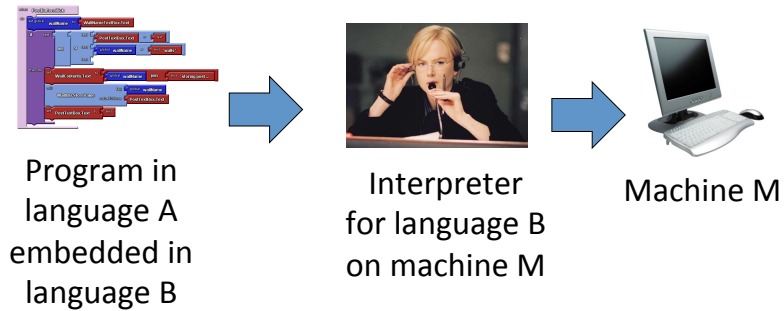
Big ideas 31

Metaprogramming: Programming Language Layers



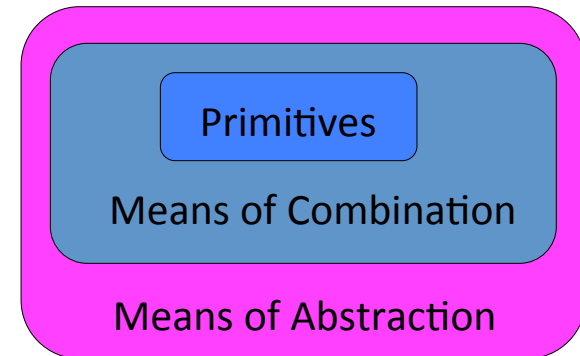
Big ideas 32

Metaprogramming: Embedding



Big ideas 33

Programming Language Essentials



Think of the languages you know. What means of abstraction do they have?

Big ideas 34

Why? Who? When? Where? Design and Application

- Historical context
- Motivating applications
 - Lisp: symbolic computation, logic, AI, experimental programming
 - ML: theorem-proving, case analysis, type system
 - C: Unix operating system
 - Simula: simulation of physical phenomena, operations, objects
 - Smalltalk: communicating objects, user-programmer, pervasiveness
- Design goals, implementation constraints
 - performance, productivity, reliability, modularity, abstraction, extensibility, strong guarantees, ...
- Well-suited to what sorts of problems?

Big ideas 35