



Datatypes, Patterns, and Parametric Polymorphism

https://cs.wellesley.edu/~cs251/s20/ Datatypes, Patterns, and Parametric Polymorphism

Topics

- Tuples and records
- · Positional vs. nominal
- Datatypes
- Pattern matching
- Parametric polymorphic types (generics)
- Lists and options
- Equality types

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Polymorphism

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Tuples

Syntax: (e1, ..., en)

Evaluation:

- 1. Evaluate e1 to v1, ..., and en to vn.
- 2. The result is (v1, ..., vn)

Type checking:

If e1 has type t1, ..., and en has type tn, then the pair expression has type ta * ... * tn

Tuple bindings

Syntax: val(x1, x2) = e

Type checking:

If e has type t1 * t2, then #1 e has type t1 and #2 e has type t2

Evaluation:

- 1. Evaluate e to a pair of values (v1, v2) in the current dynamic environment
- 2. Extend the current dynamic environment by binding x1 to v1 and x2 to v2.

Poor style.

Tuple accessors

#1 e #2 e Syntax:

Type checking:

If e has type t1 * t2. then #1 e has type t1 and #2 e has type t2

Evaluation:

- 1. Evaluate e to a pair of values v1 and v2 in the current dynamic environment
- 2. The result v1 if using #1; v2 if using #2

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Examples

```
fun swap (pr:int*bool) =
  let val (x,y) = pr in (y,x) end
fun sum two pairs (prl:int*int, pr2:int*int) =
  let val (x1,y1) = pr1
     val(x2,y2) = pr2
 in x1 + y1 + x2 + y2 end
fun div mod (x:int, y:int) =
  (x div y, x mod y)
fun sort pair (pr : int*int) =
  let val (x,y) = pr
 in
    if x < y then pr else (y,x)
  end
```

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Records

Record values have fields (any name) holding values

$${f1 = v1, ..., fn = vn}$$

Record types have fields (any name) holding types {f1 : t1, ..., fn : tn}

Order of fields in a record value or type never matters Building records:

$${f1 = e1, ..., fn = en}$$

Accessing components:

#myfieldname e

(Evaluation rules and type-checking as expected)

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Example

```
\{name = "Wendy", id = 41123 - 12\}
Has type
             {id : int, name : string}
Evaluates to
             {id = 41111, name = "Wendy"}
```

If an expression, e.g. variable x, has this type, then get fields with:

#id x #name x

No record type **declarations!**

 The same program could also make a {id=true,ego=false} of type {id:bool,ego:bool}



By position vs. by name

(structural/positional)

(nominal)

$$\{f=4,g=7,h=9\}$$

Common syntax decision

Common hybrid: function/method arguments

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Tuples are sugar

```
(e1,...,en)
desugars to
{1=e1,...,n=en}

t1*...*tn
desugars to
{1:t1,...,n:tn}
```

Records with contiguous fields 1...n printed like tuples Can write $\{1=4, 2=7, 3=9\}$, bad style

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LO

How can we build lists?

Racket: (cons 1 (cons 2 (cons 3 null)))

ML has a "no value" value written (), pronounced "unit," with type **unit**

What is the type of: (1, (2, (3, ())))

What is the type of: (1, (2, (3, (4, ()))))

Why is this a problem?

How to build bigger data types

Data type building blocks in any language

- Product types ("Each of"):
 Value contains values of each of t1 t2 ... tn
 Value contains a t1 and a t2 and ... and a tn
- Sum types ("One of"):
 Value contains values of one of t1 t2 ... tn
 Value is t1 xor a t2 xor ... xor a tn
- Recursive types ("Self reference"):
 A t value can refer to other t values

Datatype bindings

Algebraic Data Type

- Adds new type mytype to environment
- Adds constructors to environment: TwoInts, Str, Pizza
- Constructor: function that makes values of new type (or is a value of new type):

```
- TwoInts : int * int -> mytype
- Str : string -> mytype
- Pizza : mytype
```

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Datatypes: constructing values

- Values of type mytype produced by one of the constructors
- Value contains:
 - Tag: which constructor (e.g., TwoInts)
 - Carried value (e.g., (7,9))
- Examples:
 - TwoInts (3+4,5+4) evaluates to TwoInts (7,9)
 - Str if true then "hi" else "bye" evaluates to Str "hi"
 - Pizza is a value

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Datatypes: using values

- 1. Check what *variant* it is (what constructor made it)
- 2. Extract carried *data* (if that variant has any)

ML could create functions to get parts of datatype values

- Like to pair? or cdr in Racket
- Instead it does something **much** better...

Pattern matching



Case expression and pattern-matching

```
fun f x = (* f has type mytype -> int *)
  case x of
    Pizza => 3
    | TwoInts(i1,i2) => i1+i2
    | Str s => String.size s
```

All-in-one:

- Multi-branch conditional, picks branch based on variant.
- Extracts data and binds to branch-local variables.
- Type-check: all branches must have same type.
- Gets even better later.

Pattern matching

Syntax:

```
case e0 of
    p1 => e1
    | p2 => e2
    ...
    | pn => en
```

- (For now), each pattern **pi** is:
 - a constructor name followed by the right number of variables:
 - C or D x or E (x,y) or ...
- Patterns are not expressions.
 - We do not evaluate them.
 - We match e0 against their structure.
- Precise type-checking/evaluation rules later...

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Pattern matching rocks.

- 1. Cannot forget a case (inexhaustive pattern-match warning)
- 2. Cannot duplicate a case (redundant pattern type-checking error)
- 3. Cannot forget to test the variant correctly and get an error ((car null) in Racket)
- 4. It's much more general.

 Supports elegant, concise code.

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ML has built-in lists with nicer syntax.

Wait 2 slides.

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Useful examples

Enumerations, carrying other data

Alternate ways of identifying real-world things/people

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Building (our own) list datatype

A list is either:

- The empty list; or
- A pair of a list element and a list that holds the rest of the list.

Nicer syntax, but same structure as our lists!

Accessing (our own) lists

```
val some ints = Cons (1, Cons (2, Cons (3, Empty)))
         fun length (xs : mylist) =
           case xs of
                Empty => 0
              | Cons (x, xs') \Rightarrow 1 + length xs'
         fun sum (xs : mylist) =
           case xs of
                Empty => 0
               Cons (x, xs') \Rightarrow x + sum xs'
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```

ML lists: creating

The empty list is a value: []

A list of expressions/values is an expression/value:

```
[e1,e2,...,en] [v1,v2,...,vn]
```

If e1 evaluates to v and e2 evaluates to a list [v1,..., vn], then e1::e2 evaluates to [v,v1,...,vn]

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ML lists: accessing

```
val some ints = [1,2,3]
 note the space between int and list
fun length (xs : int list) =
  case xs of
      [] => 0
    | x::xs' => 1 + length xs'
fun sum (xs : int list) =
  case xs of
      [] => 0
    | x::xs' => x + sum xs'
```

ML lists: type-checking

```
For any type t.
type t list describes lists where all elements have type t.
                 bool list int list list
   int list
   (int * int) list (int list * int) list
[]: t list list for any type t
   ML syntax: 'a list ("quote a" or "alpha")
e1::e2 : t list if and only if:
   - e1 : t
                     and
   - e2 : t list
More 'a soon! (Nothing to do with 'a in Racket.)
```

Polymorphism

(type?)

Example list functions

```
(types?)
```

```
fun countdown (x:int) =
  if x=0
  then []
  else x :: countdown (x-1)
fun append (xs:int list, ys:int list) =
  case xs of
      [] => ys
    x::xs' \Rightarrow x :: append (xs', ys)
fun rev (xs : int list) =
  let fun revtail (acc : int list, xs : int list) =
        case xs of
            [] => acc
           x::xs' => revtail (x :: acc, xs')
    revtail ([], xs)
  end
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```

Example higher-order list functions

```
fun map (f : int -> int, xs : int list) =
 case xs of
      [] => []
    | x::xs' => f x :: map (f, xs')
```

- These examples only work on lists of ints.
- Should be more general: work on any list

- and any function for map...

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Polymorphic types + type inference

```
The identity function: fun id (x : int) = x
  val id : int -> int
```

```
Omit the type:
                fun id x = x
  val id : 'a -> 'a
```

General!

- a is a polymorphic type variable that stands in for any type
- "id takes an argument of any type and returns a result of that same type."
- ∀'a, id : 'a -> 'a

Polymorphic types + type inference

```
fun swap pair =
    let val (x,y) = pair in (y,x) end
val swap : ('a * 'b) -> ('b * 'a)
```

Works on any type of pair!

```
val pair = swap (4, "hello")
('a * 'b) is more general than (int * string).
```

Here, int *instantiates* 'a and string *instantiates* 'b.

Polymorphic datatypes

Lists that can hold elements of any one type.

A list of "alphas" is either:

- the empty list; or
- a pair of an "alpha" and a list of "alphas"

The type **int list** is an *instantiation* of the type 'a list, where the type variable 'a is *instantiated* with int.

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Polymorphic list functions

(types?)

```
fun append (xs, ys) =
    case xs of
      [] => ys
      | x::xs' => x :: append (xs', ys)

fun rev (xs) =
    let fun revtail (acc : int list, xs : int list) =
        case xs of
        [] => acc
        | x::xs' => revtail (x :: acc, xs')
    in revtail [] xs end

fun map (f, xs) =
    case xs of
      [] => []
      | x::xs' => f x :: map (f, xs')
```

Polymorphic list functions

(type?)

```
fun map (f, xs) =
  case xs of
    [] => []
    | x::xs' => f x :: map (f, xs')
```

- Type inference system chooses most general type.
- Polymorphic types show up commonly with higherorder functions.
- Polymorphic function types often give you a good idea of what the function does.

Exceptions

An exception binding introduces a new kind of exception

```
exception MyFirstException
exception MySecondException of int * int
```

The raise primitive raises (a.k.a. throws) an exception

```
raise MyFirstException
raise (MySecondException (7,9))
```

A handle expression can handle (a.k.a. catch) an exception

- If doesn't match, exception continues to propagate

Actually...

Exceptions are a lot like datatype constructors...

- Declaring an exception adds a constructor for type exn
- Can pass values of exn anywhere (e.g., function arguments)
 - Not too common to do this but can be useful
- handle can have multiple branches with patterns for type exn, just like a case expression.
- · See examples in exnopt.sml

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Options

```
datatype 'a option = NONE | SOME of 'a
```

t option is a type for any type t

Building:

- NONE has type 'a option (much like [] has type 'a list)
- SOME e has type t option if e has type t (much like e::[])

Accessing:

· Pattern matching with case expression

Good style for functions that don't always have a meaningful result. See examples in exnopt.sml

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Special case of what should

be more general feature...

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Parametric Polymorphism and the power of what you cannot do.

Type 'a means "some type, but don't know what type"

What can a function of type 'a list -> int do?

```
fun f (xs : 'a list) : int = ...
```

```
fun q(x : 'a) : 'a = ...
```

Equality Types

So if we cannot inspect values of type 'a in any way, how do we write a general contains function?

```
fun contains (xs : 'a list, x : 'a) : bool = ...
```

eqtypes (equality types):

Special category of types that support comparison. Accompanying eqtype variables with double quotes

Mostly accurate:

```
= : (''a * ''a) -> bool
fun contains (xs : ''a list, x : ''a) : bool = ...
```