<image/> <image/> <image/> <image/> <section-header><section-header><section-header><section-header><section-header><section-header><section-header><section-header><section-header><section-header><section-header><section-header></section-header></section-header></section-header></section-header></section-header></section-header></section-header></section-header></section-header></section-header></section-header></section-header>	 Topics Lexical vs dynamic scope Closures implement lexical scope. Design considerations: why lexical scope? Relevant design dimensions
https://cs.wellesley.edu/~cs251/s20/ Lexical Scope and Function Closures 1	Lexical Scope and Function Closures 2
A question of scope (warmup)	A question of scope
<pre>(define x l) (define f (lambda (y) (+ x y))) (define z (let (x 2) (y 3) (f (+ x y))) What is the argument value passed to this function application?</pre>	$(define * 1) \\ (define f (lambda (y) (+ * y))) \\ (define z \\ (let (x 2) \\ (y 3)) \\ (f (+ * y)))) $ What is the value of x when this function body is evaluated for this function application?



Closures implement lexical scope.

Closures allow functions to use any binding in the environment where the function is defined, regardless of where it is applied.

Anonymous function definition expressions

Syntax: $(1 \text{ ambda } (x1 \dots xn) e)$



- parameters: x1 through xn are identifiers
- **body:** e is any expression

Evaluation:

1. The result is a *function closure*, (E, (lambda (x1...xn)e)), holding the current environment, E, and the function.

[closure]

 $E \vdash (lambda (x1 ... xn) e) \downarrow \langle E, (lambda (x1 ... xn) e) \rangle$

Note:

- An anonymous function definition is an expression.
- A function closure is a new kind of value. Closures are not expressions.
- This is a *definition*, not a call. The body, *e*, is **not** evaluated now.
- lambda from the λ -calculus.

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Function application (call)

Syntax: (*e0 e1 ... en*)

Evaluation:

- 1. Under the current dynamic environment, E, evaluate e0 through en to values v0, ..., vn.
- 2. If v0 is a function closure of n arguments, $\langle E', (lambda (x1...xn) e) \rangle$ then

The result is the result of evaluating the closure body, e, under the closure environment, E', extended with argument bindings: $x1 \mapsto v1$, ..., $xn \mapsto vn$.

Otherwise, there is a type error.

Function application (call) Syntax: (e0 e1 ... en) Evaluation: $E \vdash e0 \downarrow (E', (lambda (x1 ... xn) e))$ $E \vdash e1 \downarrow v1$... $E \vdash en \downarrow vn$ $x1 \rightarrowtail v1, ..., xn \leftrightarrow vn, E' \vdash e \downarrow v$ $E \vdash (e0 e1 ... en) \downarrow v$ [apply]

Functions 11

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Neek









PL design quiz

Java methods and C functions do not need closures because they _____

- a. cannot refer to names defined outside the method/function
- b. are not first class values
- c. do not use lexical scope
- d. are not anonymous (i.e., they are named)

```
Which, if any, are correct? Why?
```

Debrief

- 1. Closures implement lexical scope.
- 2. Function bodies can use bindings from the environment where they were defined, not where they were applied.
- 3. The environment is not a stack.
 - Multiple environments (branches) may be live simultaneously.
 - CS 240's basic stack model will not suffice.
 - General case: heap-allocate the environment.
 GC will clean up for us!

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Why lexical scope?

Lexical scope: use environment where function is defined.

Dynamic scope: use environment where function is applied.

History has shown that lexical scope is almost always better.

Here are some precise, technical reasons (not opinion).



Why lexical scope?

3a. Closures automatically "remember" the data they need.

```
(define (greater-than-x x)
  (lambda (y) (> y x)))
(define (no-negs xs)
  (filter (greater-than-x -1) xs))
```

```
(define (all-greater xs n)
  (filter (lambda (x) (> x n)) xs))
```

Why lexical scope?

3b. Closures are a useful way to avoid recomputation.

These functions filter lists of lists by length.

```
(define (all-shorter-than-1 lists mine)
  (filter (lambda (xs) (< (length xs) (length mine))) lists))</pre>
```

```
(define (all-shorter-than-2 lists mine)
 (let ([len (length mine)])
   (filter (lambda (xs) (< (length xs) len)) lists)))</pre>
```

How many times is the length function called during all-shorter...?

Dynamic scope?

Lexical scope is definitely the right default for variables.

- Nearly all modern languages

Early LISP used dynamic scope.

- Even though inspiration (lambda calculus) has lexical scope.
- $-\;$ Later "fixed" by Scheme (Racket's parent) and other languages.
- Emacs Lisp still uses dynamic scope.

Dynamic scope is very occasionally convenient:

- Racket has a special way to do it.
- Perl has something similar.
- Most languages are purely lexically scoped.
- Exception raise/handle, throw/catch is like dynamic scope.

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Remember when things evaluate!

A function body is **not evaluated until** the function is called.

A function body is evaluated every time the function is called.

A function call's **arguments are evaluated before the called function's body**.

A binding evaluates its expression when the binding is evaluated, not every time the variable is used.

As with lexical/dynamic scope, there are other options here that Racket does **not** use. We will consider some later.

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Relevant PL design dimensions

in the Racket language:

- scope: lexical (static)
 - vs. dynamic
- parameter passing: pass-by-value (call-by-value)
 vs. by-reference, by-name, by-need
- evaluation order: eager (strict)

• vs. lazy

in our definitions of the Racket language (subset):

- environments and closures
 - vs. substitution
- big-step operational semantics
 - vs. small-step

More on all of these dimensions (and alternatives) later!

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