CS 251 Spring 2020
Principles of Programming Languages Ben Wood

# Defining Racket: Pairs, Lists, and GC <br> +lists.rkt 

## Topics

- Compound values:
- Cons cell: pair of values
- List: ordered sequence of parts
- Programming with pairs and lists
- Implementation consideration: garbage collection (GC)


## Pairs: cons cells

Construct a cons cell holding 2 values: cons built-in function, takes 2 arguments

Access parts:
car built-in function, takes 1 argument returns first (left) part if argument is a cons cell
cdr built-in function, takes 1 argument returns second (right) part if argument is a cons cell
mnemonic: car precedes cdr in alphabetic order
Names due to the IBM 704 computer assembler language
(used for first Lisp implementation, 1950s)
contents of the address/decrement part of register number

## cons expressions build cons cells

Syntax: (cons e1 e2)

## Evaluation:

cons is a function, so why
define evaluation rules?

1. Evaluate e1 to a value v1.
2. Evaluate e2 to a value v2.
3. The result is a cons cell containing $\mathbf{v} \mathbf{1}$ as the left value and $\mathbf{v} 2$ as the right value: (cons v1 v2)


## cons cells are values

Syntax: (cons v1 v2)

```
-(cons 17 42)
-(cons 3.14159 #t)
-(cons (cons 3 4.5) (cons #f 5))
```

So is (cons 1742 ) a function application expression or a value?

$$
e::=v \mid \ldots
$$

## cons cell diagrams



Convention: put "small" values (numbers, booleans, characters) inside a box, and draw a pointers to "large" values (functions, strings, pairs) outside a box.


## car and cdr expressions

Syntax: (car e)

## Evaluation:

1. Evaluate $e$ to a cons cell.
2. The result is the left value in the cons cell.

$$
\frac{E \vdash e \downarrow(\text { cons v1 v2) }}{E \vdash(\operatorname{car} e) \downarrow \text { v1 }} \text { [car] }
$$

Syntax: ( $\operatorname{cdr}$ e)
Evaluation:

1. Evaluate $e$ to a cons cell.
2. The result is the right value in the cons cell.

$$
\frac{E \vdash e \downarrow(\text { cons v1 v2 })}{E \vdash(\operatorname{cdr} e) \downarrow \text { v2 }}[c d r]
$$

## Practice with car and cdr

Write expressions using car, cdr, and tr that extract the five leaves of this tree:

```
(define tr (cons (cons 17 (cons "cat" 6))
                                (cons #t (lambda (x) (* 2 x))))
```

```
tr \mapsto (cons (cons 17 (cons "cat" 6))
```

tr \mapsto (cons (cons 17 (cons "cat" 6))
(cons \#t (lambda (x) (* 2 x)))), ...

```
    (cons #t (lambda (x) (* 2 x)))), ...
```


"cat"

## Rule check

What is the result of evaluating this expression?
(car (cons (+ 2 3) (cdr 4)))

## Examples

(define (swap-pair pair)
(cons (cdr pair) (car pair)))
(define (sort-pair pair)
(if (< (car pair) (cdr pair)) pair
(swap pair)))

What are the values of these expressions?
(swap-pair (cons 1 2))
(sort-pair (cons 4 7))
(sort-pair (cons 8 5))

## Lists

A list is one of:

- The empty list: null
- A pair of the first element, $\mathrm{v}_{\text {first }}$, and a smaller list, $\mathrm{v}_{\text {rest }}$, containing the rest of the elements:

$$
\text { (cons } \left.\mathrm{V}_{\text {first }} \mathrm{V}_{\text {rest }}\right)
$$

A list of the numbers 7,2 , and 4 :
(cons 7 (cons 2 (cons 4 null)))

## List diagrams

These $n$ cons cells form the "spine" of the list


The slash means this slot contains null


## list as sugar

- (list) desugars to null
- (list e1 ...) desugarsto (cons e1 (list ...))

```
Example: (list (+ 1 2) (* 3 4) (< 5 6))
desugars to
    (cons (+ 1 2) (list (* 3 4) (< 5 6)))
desugarsto (cons (+ 1 2) (cons (* 3 4) (list (< 5 6))))
desugarsto (cons (+ 1 2) (cons (* 3 4) (cons (< 5 6) (list))))
desugarsto (cons (+ 1 2) (cons (* 3 4) (cons (< 5 6) null)))
```


## Quoted notation (only the basics) <br> Read Racket docs for more.

Symbols are values: ' a
where $\boldsymbol{a}$ is any valid identifier or other primitive value number and boolean symbols identical to values: '\#f is \#f

Atoms: symbols, numbers, booleans, null
Quoted notation of cons/list values:

- A cons cell (cons 12 ) is displayed '(1-2)
- null is displayed ' ()
- A cons cell(cons 1 null) is displayed '(1)
- A cons cell(cons 1 (cons 2 null)) is displayed '(12)
- (list 123 ) is displayed '( $\left.\begin{array}{ll}1 & 2\end{array}\right)$
- '(cons 12) is the same as (list 'cons '1 '2)
- (cons (cons 1 2) (cons 34)) is displayed '((1 . 2) 3 . 4)


## List practice: notation

(define LOL
(list (list 17 19)
(list 2342 57)
(list 115 (list 111230235251 301) 240 342)))

1. Draw the diagram for the value bound to LOL.
2. Write the printed representation of the value bound to LOL.
3. Give expressions using LOL (and no number values) that evaluate to the following values: 19, 23,57, 251, ' (235 251301 )
4. Write the the result of evaluating:
```
    (+ (length LOL)
    (length (third LOL))
        (length (second (third LOL))))
```


## append

```
(define L1 (list 8 3))
(define L2 (list 7 2 4))
```

The append function takes two lists as arguments and returns a list of all the elements of the first list followed by all the elements of the second list.


## List practice: representation

(define L1
(define
L2 2 $\left(\begin{array}{lll}7 & 2 & 4\end{array}\right)$ )

For each of the following three lists:

1. Draw the diagram for its value.
2. Indicate the number of cons cells created for its value. (Don't count pre-existing cons cells.)
3. Write the quoted notation for its value.
4. Determine the list length of its value.
```
(define L3 (cons L1 L2))
(define L4 (list L1 L2))
(define L5 (append L1 L2))
```


## List practice: lists.rkt

- Recursive list functions


## limplementation: memory management

Who cleans up all those cons cells when we're done with them?
(car (cons 1 (cons 2 (cons 3 null))))
subexpression result
$\downarrow$


## CS 240-style machine model



## Implementation: memory management

Who cleans up all those cons cells when we're done with them?

```
(car (cons 1 (cons 2 (cons 3 null)))) \downarrow 1
```

Garbage:
cells that will never be used again, but still occupy storage space.


## Garbage Collection (GC)

- A cell or object is garbage once the remainder of evaluation will never access it.
- Garbage collection:

Reclaim space used by garbage.

- Required/invented to implement Lisp.
- Immutability $\Rightarrow$ fresh copies
- Rapid allocation, rapid garbage creation


## GC: Reachability

Goal: Reclaim storage used for all garbage cells.
Reality? (let ([garbage (list 1 2 3)])
(if e (length garbage) 0)
Achievable goal: Reclaim storage used for all unreachable cells.

- All unreachable cells are garbage.
- Some garbage cells are reachable.

A cell is reachable if it is:
roots $\left\{{ }^{-}\right.$a subexpression of the expression currently being evaluated; or
roots [. bound in the current environment*; or
recursive $\{$ - bound in the environment of any reachable closure; or
heap $[$ - the referent of the car or cdr of any reachable cons cell. cases
*roughly

## GC: Reachability

Who cleans up all those cons cells when we're done with them?
(car (cons 1 (cons 2 (cons 3 null)))) $\downarrow 1$
Garbage: unreachable cells

You will read more about GC on the next assignment.

