Introduction to Racket, a dialect of LISP: Expressions and Declarations



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These slides build on Ben Wood's Fall '15 slides

LISP: designed by John McCarthy, 1958 published 1960





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LISP: implemented by Steve Russell, early 1960s





LISP: LISt Processing

- McCarthy, MIT artificial intelligence, 1950s-60s
 Advice Taker: represent logic as data, not just program
- Needed a language for:
 - Symbolic computation
 - Programming with logic
 - Artificial intelligence
 - Experimental programming
- So make one!

i.e., not just number crunching

Emacs: M-x doctor

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Scheme

- Gerald Jay Sussman and Guy Lewis Steele (mid 1970s)
- Lexically-scoped dialect of LISP that arose from trying to make an "actor" language.



- Described in amazing "Lambda the Ultimate" papers (<u>http://library.readscheme.org/page1.html</u>)
 - Lambda the Ultimate PL blog inspired by these: <u>http://lambda-the-ultimate.org</u>
- Led to Structure and Interpretation of Computer Programs (SICP) and MIT 6.001 (<u>https://mitpress.mit.edu/sicp/</u>)



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🔥 Racket

- Grandchild of LISP (variant of Scheme)

 Some changes/improvements, quite similar
- Developed by the PLT group (<u>https://racket-lang.org/people.html</u>), the same folks who created DrJava.
- Why study Racket in CS251?
 - Clean slate, unfamiliar
 - Careful study of PL foundations ("PL mindset")
 - Functional programming paradigm
 - Emphasis on functions and their composition
 - Immutable data (lists)
 - Beauty of minimalism
 - Observe design constraints/historical context

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Expressions, Values, and Declarations

- Entire language: these three things
- Expressions have evaluation rules:
 - How to determine the value denoted by an expression.
- For each structure we add to the language:
 - What is its syntax? How is it written?
 - What is its evaluation rule? How is it evaluated to a value (expression that cannot be evaluated further)?

Values

- Values are expressions that cannot be evaluated further.
- Syntax:
 - Numbers: 251, 240, 301
 - Booleans: #t, #f
 - There are more values we will meet soon (strings, symbols, lists, functions, ...)
- Evaluation rule:
 - Values evaluate to themselves.



Evaluation Derivation in English More Compact Derivation Notation An **evaluation derivation** is a ``proof " that an expression *E1* ↓ *V1 V* ↓ *V* [value rule] evaluates to a value using the evaluation rules. *E2* ↓ *V2* whereVis a value – [addition rule] $(+ 3 (+ 5 4)) \downarrow 12$ by the addition rule because: (number, boolean, etc.) (+ **E1 E2**) ↓ **V** • $3 \downarrow 3$ by the value rule Where V1 and V2 are numbers and side conditions of rules • $(+ 5 4) \downarrow 9$ by the addition rule because: V is the sum of V1 and V2. $-5 \downarrow 5$ by the value rule ↓ 3 [value] $-4 \downarrow 4$ by the value rule ↓ 5 **[value]** 5 and 4 are both numbers 4 ↓ 4 [value] - 9 is the sum of 5 and 4 - [addition] (+ 5 4) 1 9 • 3 and 9 are both numbers [addition] (+ 3 (+ 5 4))↓ 12 12 is the sum of 3 and 9 Expr/decl 13 Expr/decl 14

Errors Are Modeled by "Stuck" Derivations

How to evaluate	HOV
(+ #t (+ 5 4))?	(+
#t ↓ #t [value]	1
5 ↓ 5 [value]	2
$4 \downarrow 4$ [value]	(+
$(+ 5 4) \downarrow 9$ [addition]	5
Stuck here. Can't apply	#
(addition) rule because #t is not a number in	St
(+ #t 9)	(a
	#f
	(+

How to evaluate

(+ (+ 1 2) (+ 5 #f))?

- 1 ↓ 1 [value]
- 2 ↓ 2 [value]
- (+ 1 2) ↓ 3 [addition]

5 ↓ 5 **[value]**

#f ↓ #f [value]

Stuck here. Can't apply (addition) rule because #f is not a number in (+ 5 #f)

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Syntactic Sugar for Addition

The addition operator + can take any number of operands.

- For now, treat (+ E1 E2 ... En) as (+ (+ E1 E2) ... En)
 E.g., treat (+ 7 2 -5 8) as (+ (+ (+ 7 2) -5) 8)
- Treat (+ E) as **E** (or say if $E \downarrow V$ then $(+ E) \downarrow V$)
- Treat (+) as 0 (or say (+) \downarrow 0)
- This approach is known as **syntactic sugar**: introduce new syntactic forms that "**desugar**" into existing ones.
- In this case, an alternative approach would be to introduce more complex evaluation rules when + has a number of arguments different from 2.

Other Arithmetic Operators Relation Operators Similar syntax and evaluation for The following relational operators on numbers return - * / quotient remainder min max booleans: < <= = >= >except: • Second argument of /, quotient, remainder must be nonzero For example: • Result of / is a rational number (fraction) when both values are integers. (It is a floating point number if at least one value *E1* ↓ *V1* is a float.) *E2* ↓ *V2* • **quotient** and **remainder** take exactly two arguments; [less than] anything else is an error. (< *E1 E2*) ↓ *V* • (- E) is treated as (- 0 E) Where V1 and V2 are numbers and • (/ E) is treated as (/ 1 E) V is #t if V1 is less than V2 • (min E) and (max E) treated as E or #f if V1 is not less than V2 • (*) evaluates to 1. • (/), (-), (min), (max) are errors (i.e., stuck) Expr/decl 17 Expr/decl 18

Conditional (if) expressions

Syntax: (if Etest Ethen Eelse)

Evaluation rule:

- 1. Evaluate *Etest* to a value *Vtest*.
- If Vtest is not the value #f then return the result of evaluating Ethen otherwise

return the result of evaluating *Eelse*

Derivation-style rules for Conditionals



Your turn



Use evaluation derivations to evaluate the following expressions

(if (< 8 2) (+ #f 5) (+ 3 4))

(if (+ 1 2) (- 3 7) (/ 9 0))

(+ (if (< 1 2) (* 3 4) (/ 5 6)) 7)

(+ (if 1 2 3) #t)

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Expressions vs. statements

Conditional expressions can go anywhere an expression is expected:

Note: if is an *expression*, not a *statement*. Do other languages you know have conditional expressions in addition to conditional statements? (Many do! Java, JavaScript, Python, ...)

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Conditional expressions: careful!

Unlike earlier expressions, not all subexpressions of if expressions are evaluated!

(if (> 251 240) 251 (/ 251 0))

(if #f (+ #t 240) 251)

Design choice in conditional semantics

In the [if nonfalse] rule, *Vtest* is **not** required to be a boolean!

Etest↓Vtest Ethen↓Vthen	[if nonfalse]
(if Etest Ethen	$Eelse) \downarrow Vthen$

Where *Vtest* is not #f

This is a design choice for the language designer. What would happen if we replace the above rule by



This design choice is related to notions of "truthiness" and "falsiness" that you will explore in PS2.

Environments: Motivation

Want to be able to name values so can refer to them later by name. E.g.;

```
(define x (+ 1 2))
```

```
(define y (* 4 x))
```

```
(define diff (-y x))
```

```
(define test (< x diff))
```

```
(if test (+ (* x y) diff) 17)
```

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Environments: Definition

- An *environment* is a sequence of bindings that associate identifiers (variable names) with values.
 - Concrete example:

num \mapsto 17, absoluteZero \mapsto -273, true \mapsto #t

- Abstract Example (use *Id* to range over identifiers = names): *Id1* \mapsto *V1*, *Id2* \mapsto *V2*, ..., *Idn* \mapsto *Vn*
- Empty environment: Ø
- An environment serves as a context for evaluating expressions that contain identifiers.
- **Second argument** to evaluation, which takes both an expression and an environment.

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Addition: evaluation with environment

Syntax: (+ E1 E2)

Evaluation rule:

- 1. evaluate *E1 in the current environment* to a value *V1*
- 2. Evaluate *E2 in the current environment* to a value *V2*
- If *V1* and *V2* are both numbers then return the arithmetic sum of *V1 + V2*.
- 4. Otherwise, a type error occurs.

Variable references

Syntax: *Id*

Id: any identifier

Evaluation rule:

Look up and return the value to which $\boldsymbol{\mathit{Id}}$ is bound in the current environment.

- Look-up proceeds by searching from the most-recently added bindings to the least-recently added bindings (front to back in our representation)
- If *Id* is not bound in the current environment, evaluating it is "stuck" at an *unbound variable error*.

Examples:

- Suppose env is num → 17, absZero → -273, true → #t, num → 5
- In *env*, num evaluates to 17 (more recent than 5), absZero evaluates to -273, and true evaluates to #t. Any other name is stuck.

define Declarations

Syntax: (define Id E) define: keyword Id: any *identifier* E: any expression

This is a **declaration**, not an **expression**! We will say a **declarations** are **processed**, not **evaluated**

Processing rule:

- 1. Evaluate *E* to a value *V* in the current environment
- Produce *a new environment* that is identical to the current environment, with the additional binding *Id* → *V* at the front. Use this new environment as the current environment going forward.

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Environments: Example

```
env0 = Ø (can write as . in text)

(define x (+ 1 2))

env1 = x → 3, Ø (abbreviated x → 3; can write as x -> 3 in text)

(define y (* 4 x))

env2 = y → 12, x → 3 (most recent binding first)

(define diff (- y x))

env3 = diff → 9, y → 12, x → 3

(define test (< x diff))

env4 = test → #t, diff → 9, y → 12, x → 3

(if test (+ (* x 5) diff) 17)

environment here is still env4

(define x (* x y))

env5 = x → 36, test → #t, diff → 9, y → 12, x → 3

Note that binding x → 36 "shadows" x → 3, making it inaccessible Functional 30
```

Evaluation Assertions & Rules with Environments

The **evaluation assertion** notation *E* **#** *env* **\downarrow ***V* means "Evaluating expression *E* in environment *env* yields value *V*".

<i>Id</i> # <i>env</i> ↓ <i>V</i> [varref]	E1 # env ↓ V1
Where <i>Id</i> is an identifier and $Id \mapsto V$ is the first binding in <i>env</i> for <i>Id</i> Only this rule actually	<i>E2 # env</i> ↓ <i>V2</i> (+ <i>E1 E2</i>) <i># env</i> ↓ <i>V</i> [addition]
uses env; others just pass it along	Where V1 and V2 are numbers and
<i>V</i> # <i>env</i> ↓ <i>V</i> [value]	V is the sum of V1 and V2 . Rules for other arithmetic and relational ops are similar.
where V is a value (number, boolean, etc.)	E1 # env ↓ V1
E1 # env ↓ # f	<i>E2</i> # <i>env</i> ↓ <i>V2</i> [if nonfalse]
<i>E3</i> # <i>env</i> ↓ <i>V3</i> [if false]	(if E1 E2 E3) # env ↓ V2
(if E1 E2 E3) # env ↓ V3	Where V1 is not #f Expr/decl 3

Example Derivation with Environments

```
Suppose env4 = test \mapsto #t, diff \mapsto 9, y \mapsto 12, x \mapsto 3
```

```
test #env4 \ #t [varref]

\begin{array}{c} x # env4 \downarrow 3 [varref] \\
5 # env4 \downarrow 5 [value] \\
(* x 5) # env4 \downarrow 15 \\
\end{array}
[multiplication]

\begin{array}{c} diff # env4 \downarrow 9 [varref] \\
(+ (* x 5) diff) # env4 \downarrow 24 \\
\end{array}
[addition]

(if test (+ (* x 5) diff) 17) # env4 \downarrow 24 \\
\end{array}
[if nonfalse]
```



Formalizing definitions

The declaration assertion notation (define Id E) # $env \Downarrow env'$ means ``Processing the definition (define Id E) in environment env yields a new environment env'''. We use a different arrow, \Downarrow , to emphasize that definitions are not evaluated to values, but processed to environments.

E # env	$\downarrow v$		[dofir	
(define I	d E) # env	, Id \mapsto V	, env	
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Threading environments through definitions

-[define]

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2 # Ø ↓ 2 [value]	
3 # Ø ↓ 3 [value]	
$(+ 2 3) \# \emptyset \downarrow 5$	
(define a (+ 2 3)) # \emptyset ↓ a \mapsto 5	
$a # a \mapsto 5 \downarrow 5 [varret]$	
a # a \mapsto 5 \downarrow 5 [varref] [multiplication]	
$(* a a) # a \mapsto 5 \downarrow 25$	

(define b (* a a)) # a \mapsto 5 \Downarrow b \mapsto 25, a \mapsto 5

a # b \mapsto 25, a \mapsto 5 \downarrow 5 [varref] (- b a) # b \mapsto 25, a \mapsto 5 \downarrow 20 [subtraction]

 $b \# b \mapsto 25$, $a \mapsto 5 \downarrow 25$ [varref]

Racket Identifiers

- Racket identifiers are case sensitive. The following are four different identifiers: ABC, Abc, aBc, abc
- Unlike most languages, Racket is very liberal with its definition of legal identifers. Pretty much any character sequence is allowed as identifier with the following exceptions:
 - Can't contain whitespace
 - Can't contain special characters () [] { } ", ' `; # | \
 - Can't have same syntax as a number
- This means variable names can use (and even begin with) digits and characters like <u>!@\$%^&*.-+</u> :<=>?/ E.g.:
 - myLongName, my_long_name, my-long-name
 - is_a+b<c*d-e?</pre>
 - 76Trombones
- Why are other languages less liberal with legal identifiers?

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Small-step vs. big-step semantics

The evaluation derivations we've seen so far are called **a big-step semantics** because the derivation $e \# env2 \downarrow v$ explains the evaluation of e to v as one "big step" justified by the evaluation of its subexpressions.

An alternative way to express evaluation is a **small-step semantics** in which an expression is simplified to a value in a sequence of steps that simplifies subexpressions. You do this all the time when simplifying math expressions, and we can do it in Racket, too. E.g;

(- (* (+ 2 3) 9) (/ 18 6)) $\Rightarrow (- (* 5 9) (/ 18 6))$ $\Rightarrow (- 45 (/ 18 6))$ $\Rightarrow (- 45 3)$ $\Rightarrow 42$

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Small-step semantics: intuition

Scan left to right to find the first redex (nonvalue subexpression that can be reduced to a value) and reduce it:

$$(-(*(+23)) 9) (/186))$$

 $\Rightarrow (-(*59) (/186)) [addition]$
 $\Rightarrow (-45(/186)) [multiplication]$
 $\Rightarrow (-453) [division]$
 $\Rightarrow 42 [subtraction]$

Small-step semantics: reduction rules

There are a small number of reduction rules for Racket. These specify the redexes of the language and how to reduce them.

The rules often require certain subparts of a redex to be (particular kinds of) values in order to be applicable.

- $Id \rightarrow V$, where $Id \mapsto V$ is the first binding for Idin the current environment* [varref]
- $(+ V1 V2) \Rightarrow V$, where V is the sum of numbers V1 and V2 [addition]

There are similar rules for other arithmetic/relational operators

(if Vtest Ethen Eelse) \Rightarrow Ethen, if Vtest is not #f [if nonfalse]

(if #f Ethen Eelse) \Rightarrow Eelse [if false]

* In a more formal approach, the notation would make the environment explicit. E.g., $E \# env \Rightarrow V$

Small-step semantics: conditional example

(+ (if {(< 1 2)} (* 3 4) (/ 5 6)) 7)
=> (+ {(if #t (* 3 4) (/ 5 6))} 7) [less than]
⇒ (+ {(* 3 4)} 7) [if nonfalse]
⇒ {(+ 12 7)} [multiplication]

 \Rightarrow 19 [addition]

Notes for writing derivations in text:

- \circ You can use => for \Rightarrow
- $\,\circ\,$ Use curly braces {...} to mark the redex
- Use square brackets to name the rule used to reduce the redex *from the previous line to the current line.*

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Small-step semantics: errors as stuck expressions

Similar to big-step semantics, we model errors (dynamic type errors, divide by zero, etc.) in small-step semantics as expressions in which the evaluation process is stuck because no reduction rule is matched. For example:



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Small-step semantics: your turn



Use small-step semantics to evaluate the following expressions:

- (if (< 8 2) (+ #f 5) (+ 3 4))
- (if (+ 1 2) (- 3 7) (/ 9 0))
- (+ (if (< 1 2) (* 3 4) (/ 5 6)) 7)
- (+ (if 1 2 3) #t)



Racket Documentation

Racket Guide:

https://docs.racket-lang.org/guide/

Racket Reference: https://docs.racket-lang.org/reference